
Applications of stochastic surface walking method in molecular crystal structure prediction

Cheng Shang

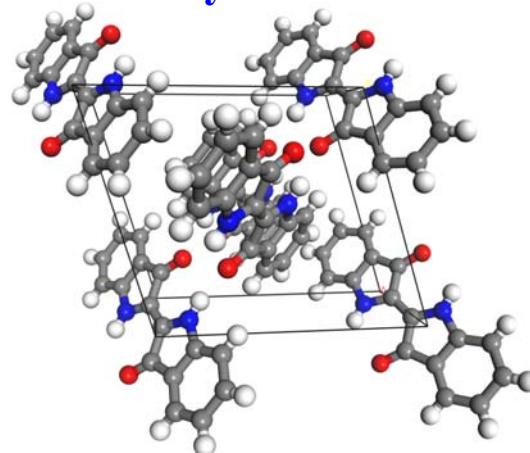
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Workshop of “Bridging-Time Scale Techniques and their Applications
in Atomistic Computational Science”
at Max Planck Institute for the Physics of Complex Systems
12-15 Sep, 2016, Dresden

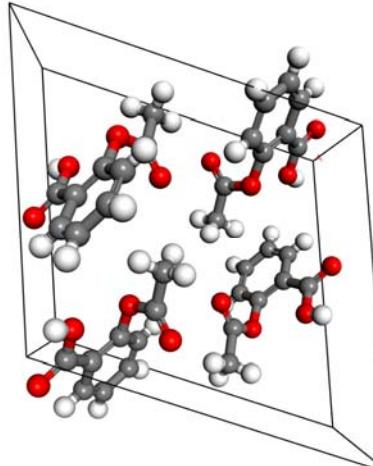
◆ Solid form of organic compound

Dye



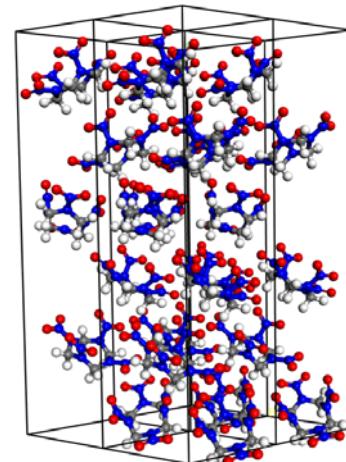
(Indigo dye)

Drug



(Aspirin)

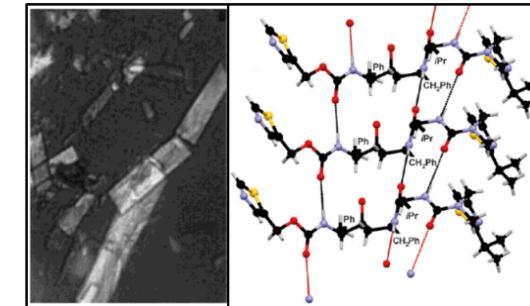
Dynamite



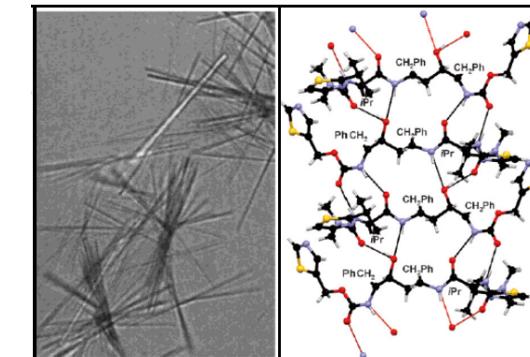
(HMX)

◆ HIV Treatment Ritonavir

Synthesized phase



Stable phase

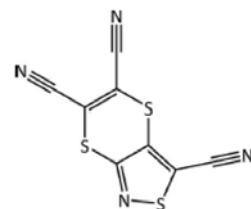


◆ CCDC Crystal Structure Prediction Blind Test

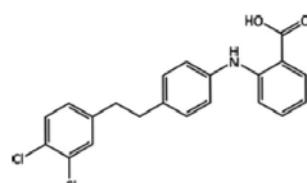
(The Cambridge Crystallographic Data Centre)



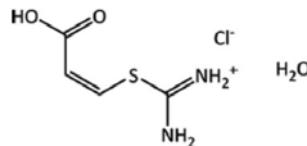
(XXII)



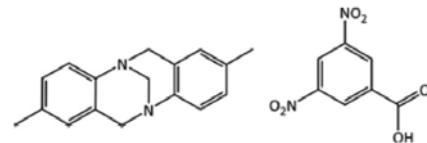
(XXIII)



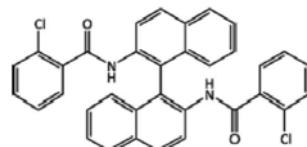
(XXIV)



(XXV)



(XXVI)



| Team | Members | Generation method |
|------|--|------------------------------|
| 1 | Chadha,* Singh | MC simulated annealing |
| 2 | Cole,* McCabe, Read, Reilly, Shields | CSD analogues |
| 3 | Day*, Bygrave, Campbell, Case, Gee, McMahon, Nyman, Pulido, Taylor, Yang | Quasi-random search (Sobol') |
| 4 | Dzyabchenko | Grid search |
| 5 | van Eijck | Random search |
| 6 | Elking, Fusti-Molnar | Random generation |
| 7 | de Jong, van den Ende,* de Gelder, de Klerk, Bylsma, de Wijs, Meekes, Cuppen | Random search |
| 8 | Lund, Pagola, Orendt, Ferraro, Facelli* | Genetic algorithm |
| 9 | Obata, Goto* | Grid search |
| 10 | Hofmann,* Kuleshova | Random search |
| 11 | Lv, Wang, Ma* | Random search |
| 12 | Curtis, Li, Schober, Cosburn, Lohani, Vacarro, Oberhofer, Reuter, Bhattacharya, Vázquez-Mayagoitia, Ghiringhelli, Marom* | Genetic algorithm |
| 13 | Mohamed | MC simulated annealing |
| 14 | Neumann, Kendrick, Leusen | MC parallel tempering |
| 15 | Sugden, Gatsiou, Vasileiadis, Adjiman,* Pantelides* | Quasi-random search (Sobol') |
| 16 | Pickard,* Monserrat, Misquitta, Needs | Random search |
| 17 | Jankiewicz, Metz, Podeszwa,* Szalewicz | Grid search |
| 18 | S. L. Price,* Hylton, L. S. Price, Guo, Watson, Iuzzolino | Quasi-random search (Sobol') |
| 19 | Metz, Hylton, S. L. Price, Szalewicz* | Quasi-random search (Sobol') |
| 20 | Vogt, Schneider, Metz, Tuckerman,* Szalewicz* | Random search |
| 21 | Zhu,* Oganov, Masunov | Evolutionary algorithm |
| 22 | Boese | Re-ranking 10 |
| 23 | Brandenburg, Grimme | Re-ranking 18 |
| 24 | Metz, Guo, Szalewicz | Re-ranking 18 |
| 25 | Hoja, Ko, Car, DiStasio Jr, Tkatchenko* | Re-ranking 18 |

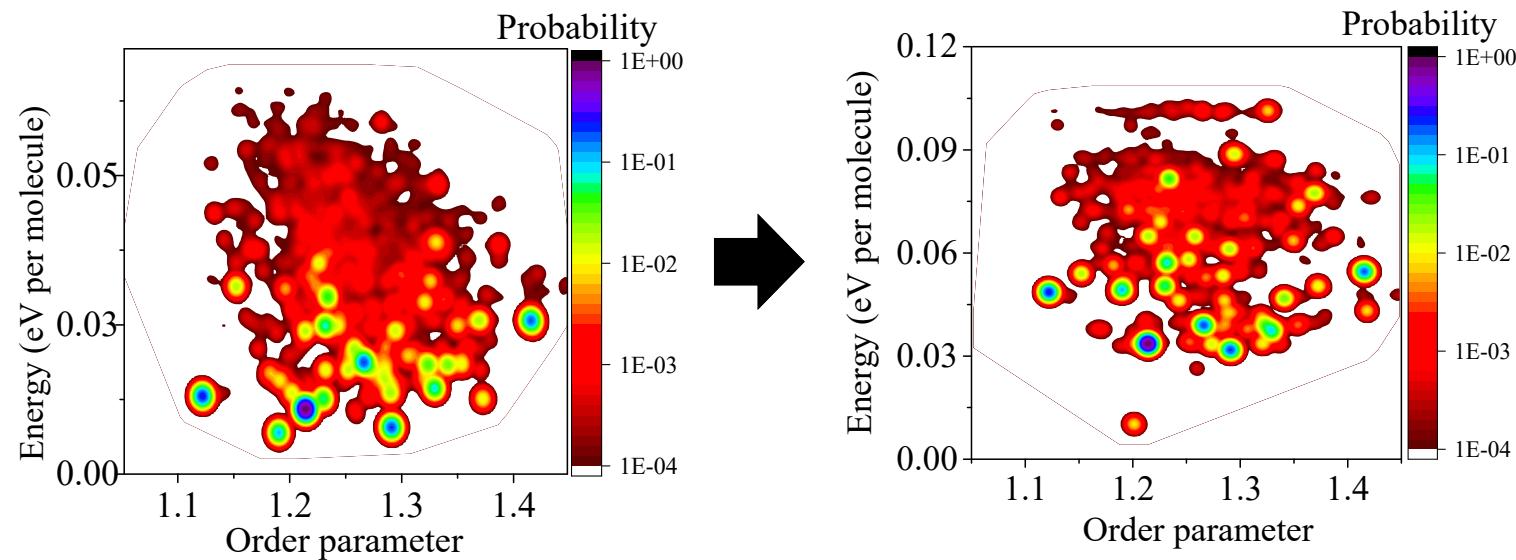
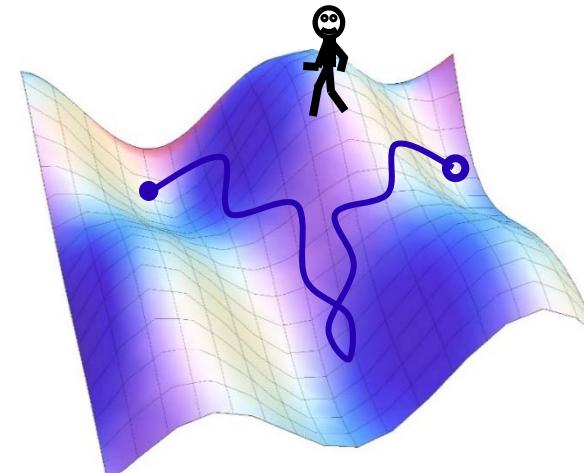
◆ Questions remaining:

- 1. What does the potential energy surface (PES) look like?**

- 2. How does the phase transition affect the experimental observation?**

◆ Calculation details

- ◆ Stochastic Surface walking method (SSW)
- ◆ Rigid body constrains
- ◆ Double-Ended Surface Walking
 - ◆ Amber force field (GAFF) (Lammps) + DFT (PBE +D3) (VASP)



◆Method: Stochastic Surface walking

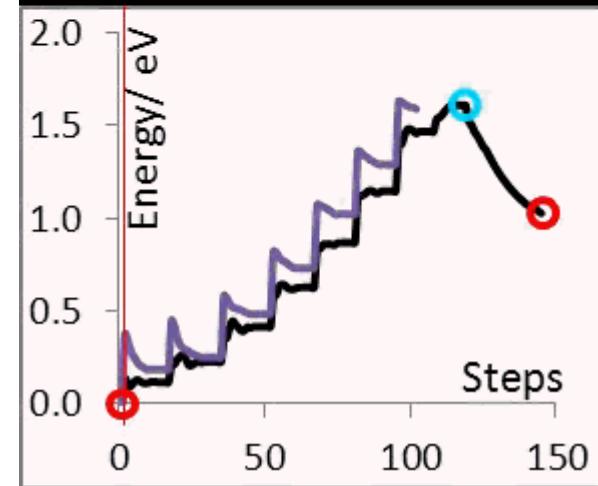
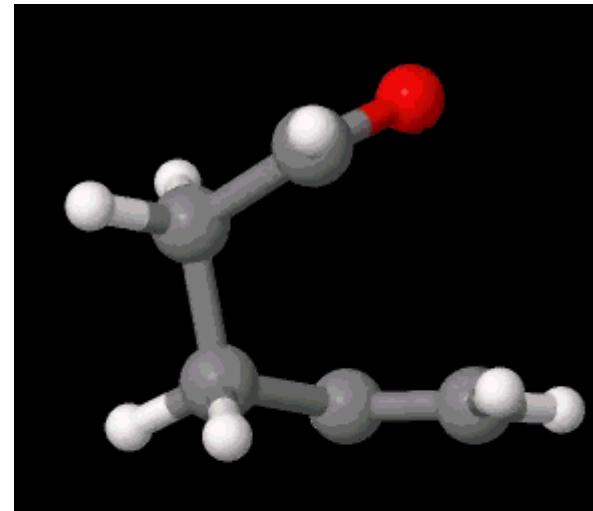
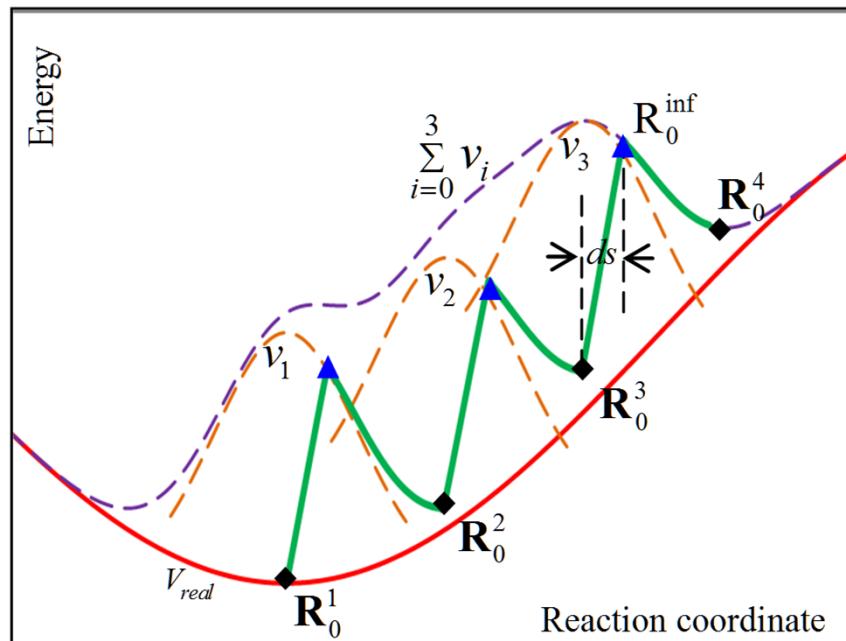
Biased rotation + Biased translation to climb

$$V_{R0} = V_{real} + V_G$$

$$V_G = \sum_i v_i \quad (i=1,2,3\cdots k)$$

$$v_i = w_i \times \exp \left[-\frac{(s_t^i - s_0^i)^2}{2 \times ds^2} \right] \quad s_t^i = \mathbf{R}_0^t \cdot \mathbf{N}_i$$

$$s_0^i = \mathbf{R}_0^i \cdot \mathbf{N}_i$$

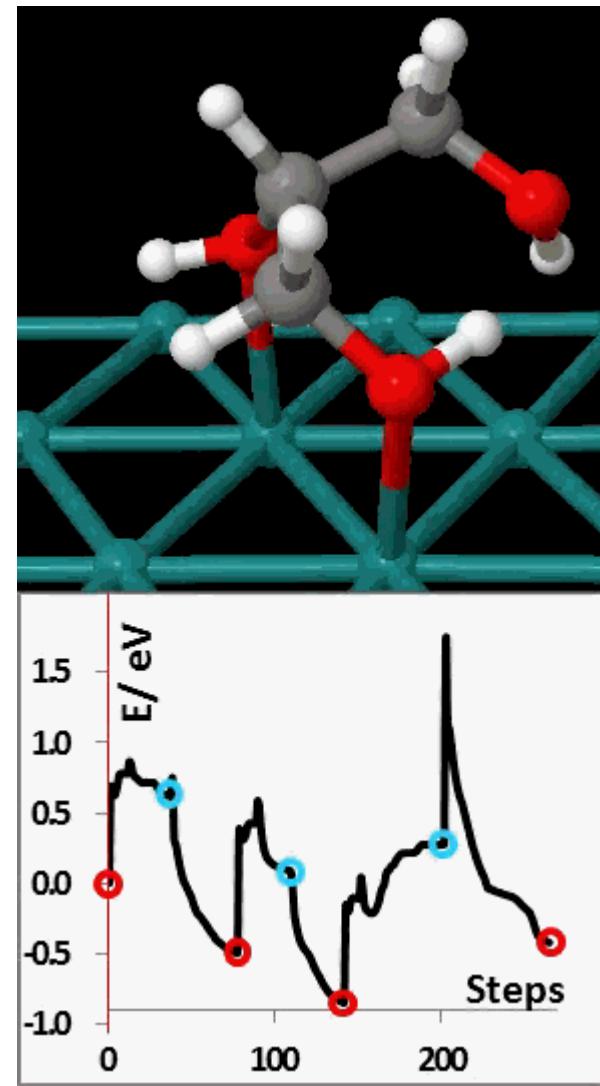
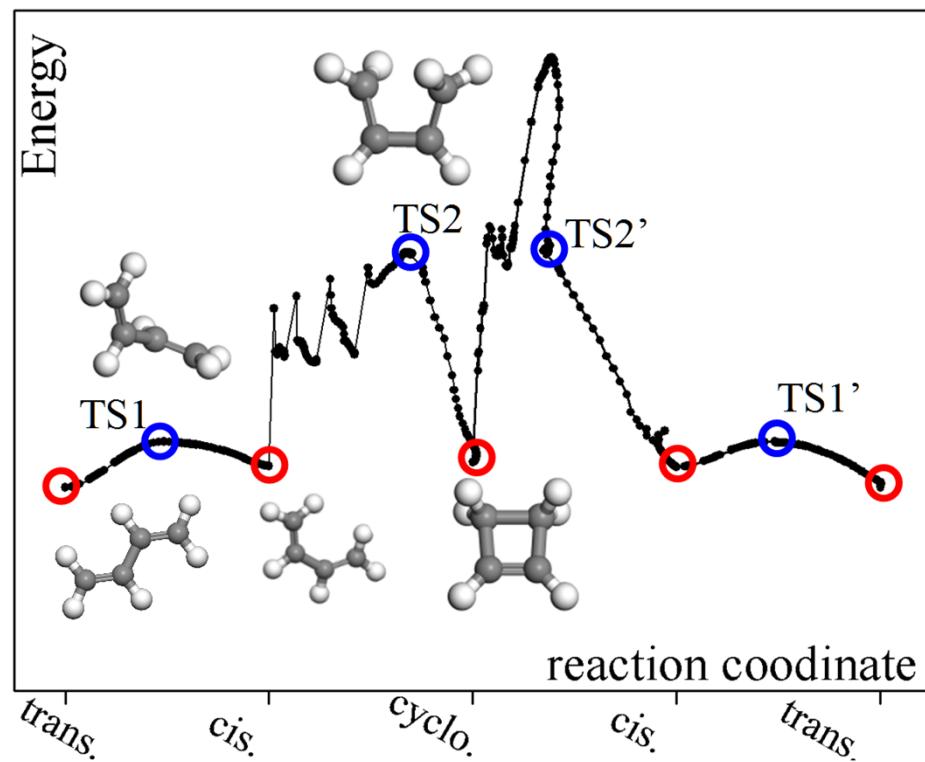


C Shang and Z-P Liu *JCTC* 2010

C Shang and Z-P Liu *JCTC* 2012

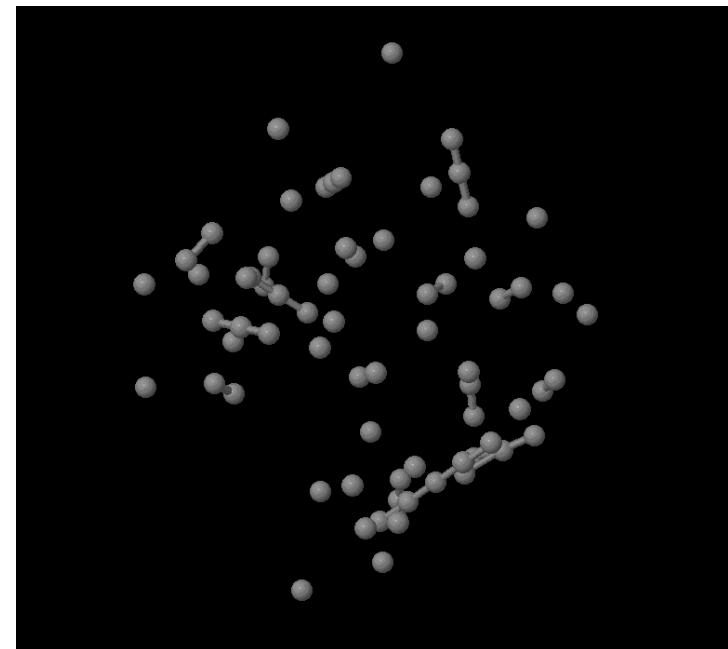
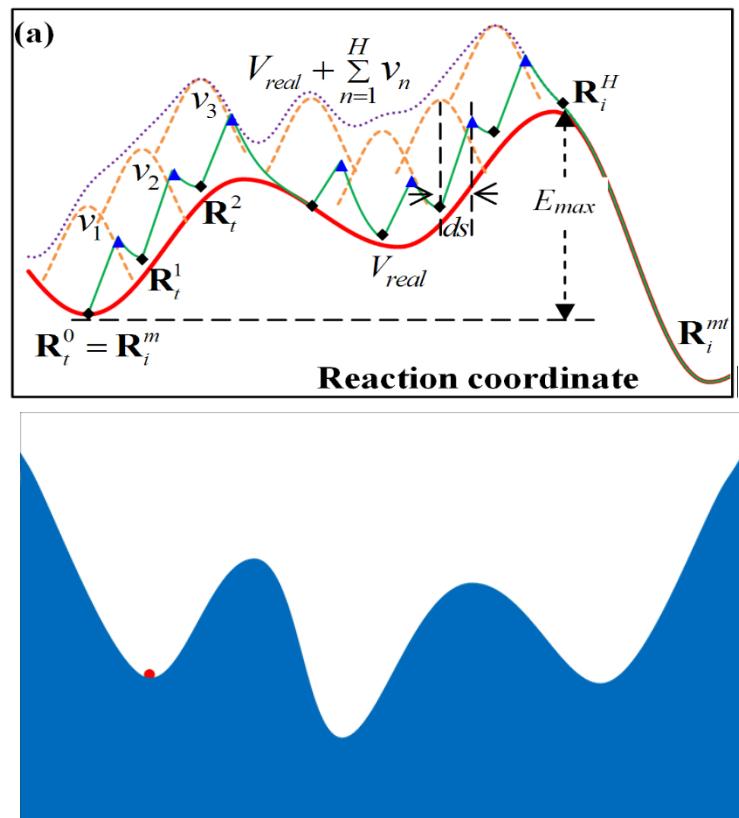
◆Method: Stochastic Surface walking

Continuous TS searching process



◆Method: Stochastic Surface walking

1. Never stop to locate TSs
2. Fix the size and the number of bias potential
3. Generate mode randomly (move class)
4. Metropolis Monte Carlo

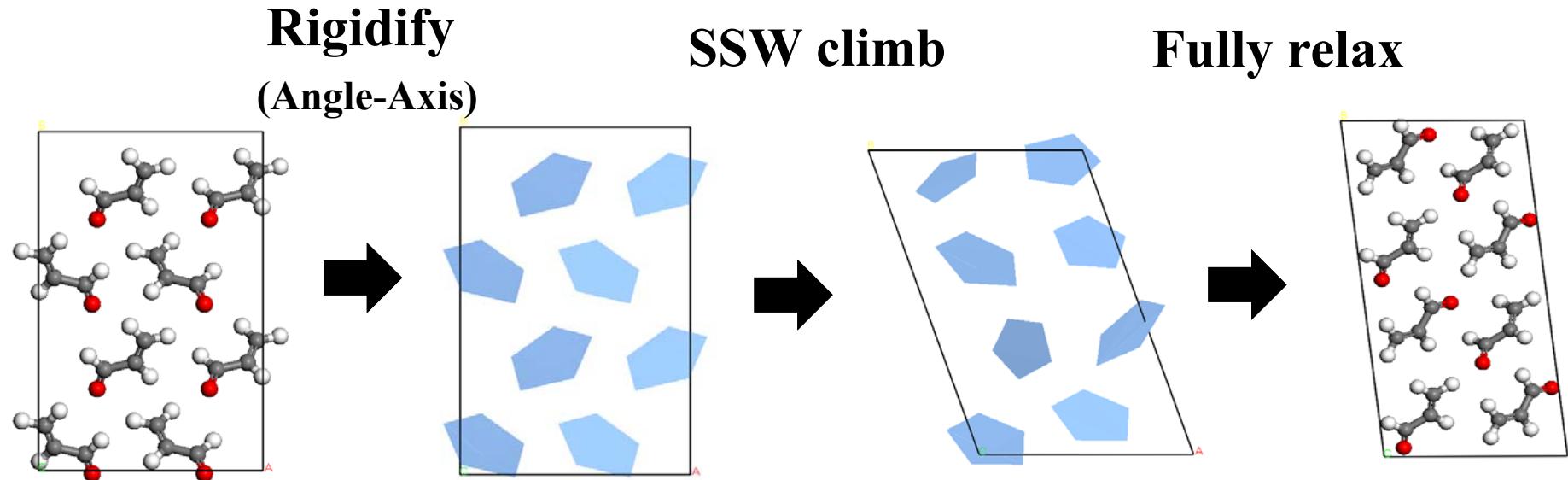


C Shang and Z-P Liu *JCTC* 2013

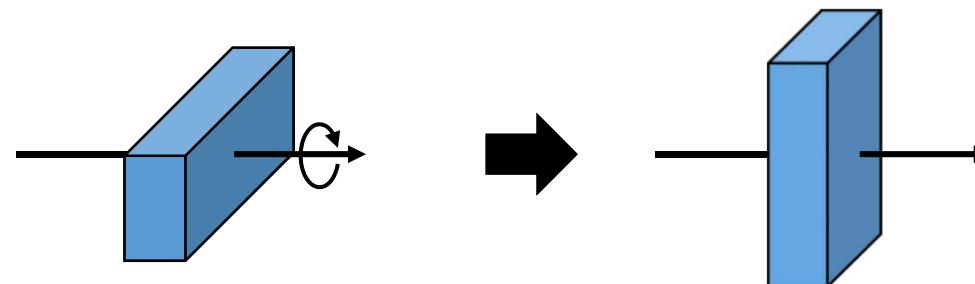
X-J Zhang, C Shang and Z-P Liu *JCTC* 2013

C Shang, X-J Zhang and Z-P Liu *PCCP* 2014

◆ Coarse-grained SSW

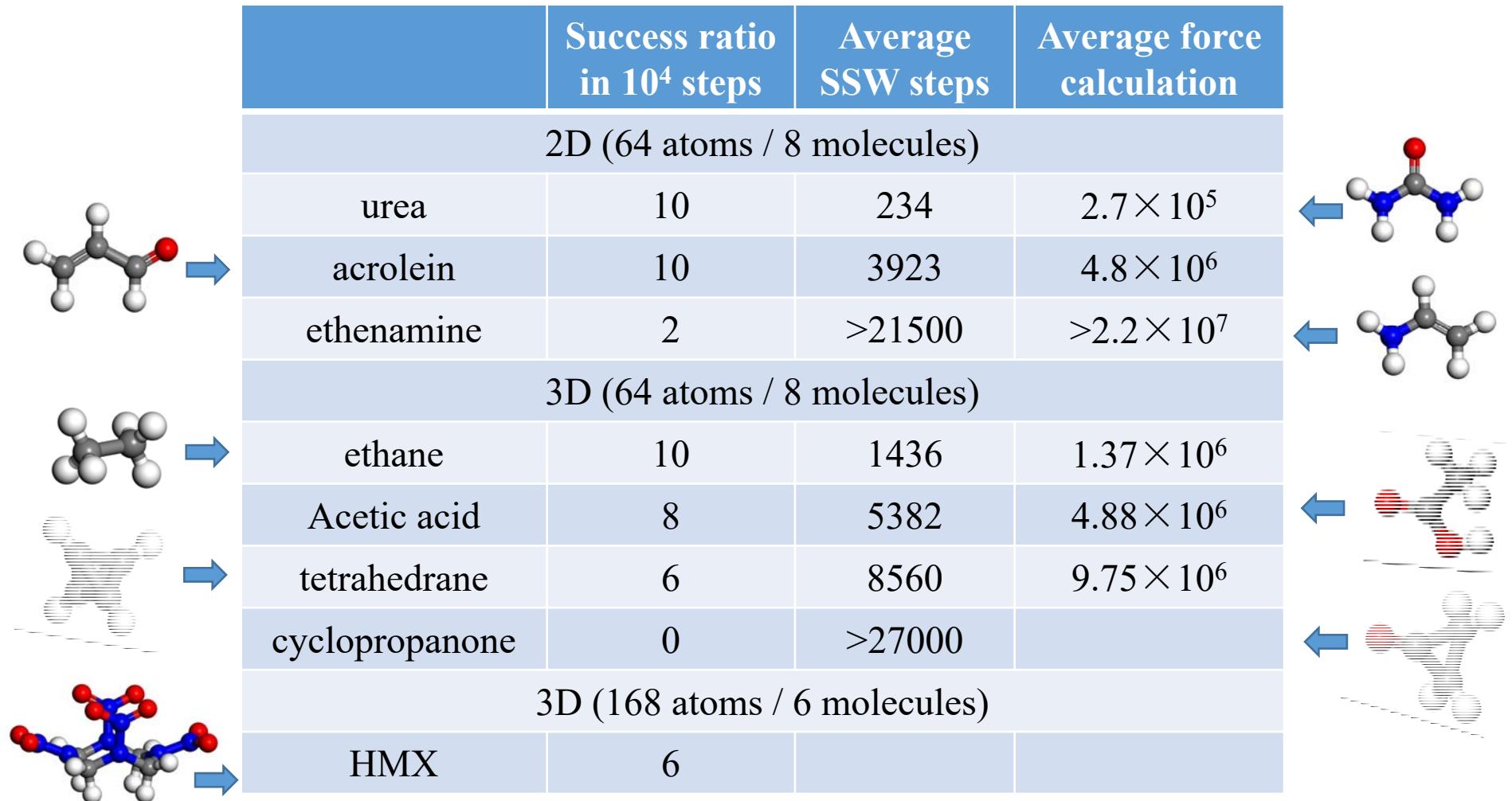


Angle-Axis: $\mathbf{R}_I = \mathbf{I} + (1 - \cos \theta_I) \tilde{\mathbf{p}}_I \tilde{\mathbf{p}}_I + \sin \theta_I \tilde{\mathbf{p}}_I$



◆ Efficiency of global minimum locating

| | Success ratio in 10^4 steps | Average SSW steps | Average force calculation |
|------------------------------|----------------------------------|----------------------|------------------------------|
| 2D (64 atoms / 8 molecules) | | | |
| urea | 10 | 234 | 2.7×10^5 |
| acrolein | 10 | 3923 | 4.8×10^6 |
| ethenamine | 2 | >21500 | $>2.2 \times 10^7$ |
| 3D (64 atoms / 8 molecules) | | | |
| ethane | 10 | 1436 | 1.37×10^6 |
| Acetic acid | 8 | 5382 | 4.88×10^6 |
| tetrahedrane | 6 | 8560 | 9.75×10^6 |
| cyclopropanone | 0 | >27000 | |
| 3D (168 atoms / 6 molecules) | | | |
| HMX | 6 | | |

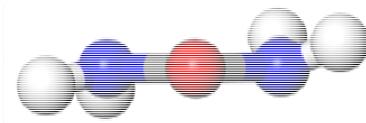
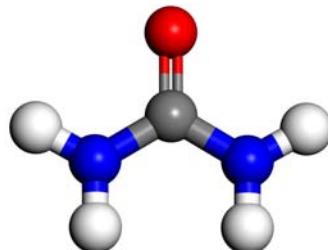


The figure displays molecular structures and 3D surface plots for various molecules. On the left, molecular models are shown with blue arrows pointing right, indicating the direction of optimization. To the right of the table, corresponding 3D surface plots are shown for each molecule, with red dots indicating the global minimum. The molecules listed are urea, acrolein, ethenamine, ethane, Acetic acid, tetrahedrane, cyclopropanone, and HMX.

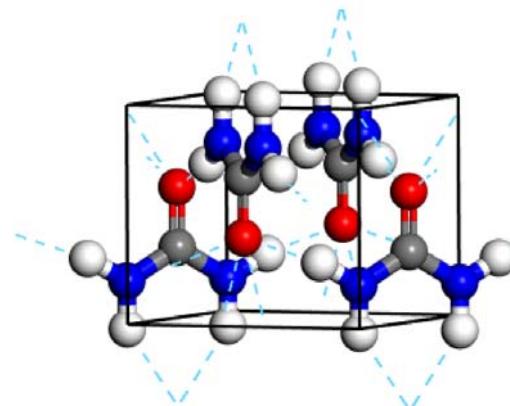
Difficulty: (1) 3D >2D (2) non-polar > polar (hydrogen-bonded)

| | Success ratio in 10^4 steps | Average SSW steps | Average force calculation |
|----------|-------------------------------|-------------------|---------------------------|
| urea | 10 | 234 | 2.7×10^5 |
| acrolein | 10 | 3923 | 4.8×10^6 |

Urea



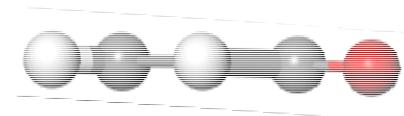
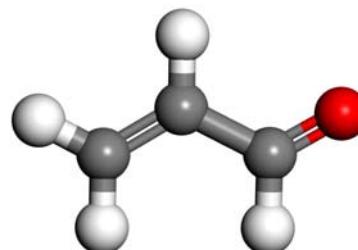
Symmetry: C2



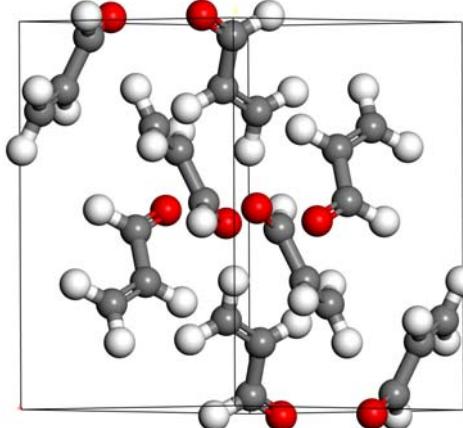
Symmetry:
 $\text{P}\bar{4}2_1\text{m}$ (#113)

Grow from aqueous solution by slow evaporation of the solvent at 43 °C. The structure was determined in early 19th.

Acrolein



Symmetry: Cs



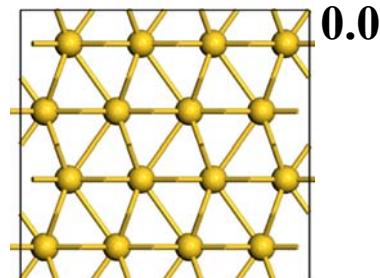
Symmetry:
 Pbca (#61)

Grow at 178 K in situ by laser-assisted zone refinement (Boese & Nussbaumer, 1994). The crystal structure was solved in 2007 by Forster et al.

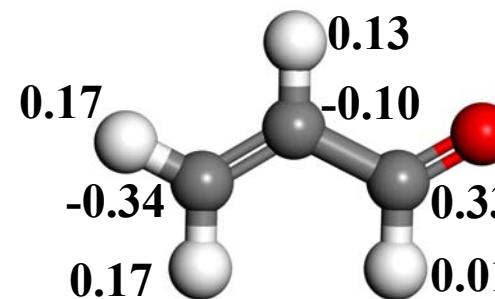
◆ Results

Close packing versus Orientation

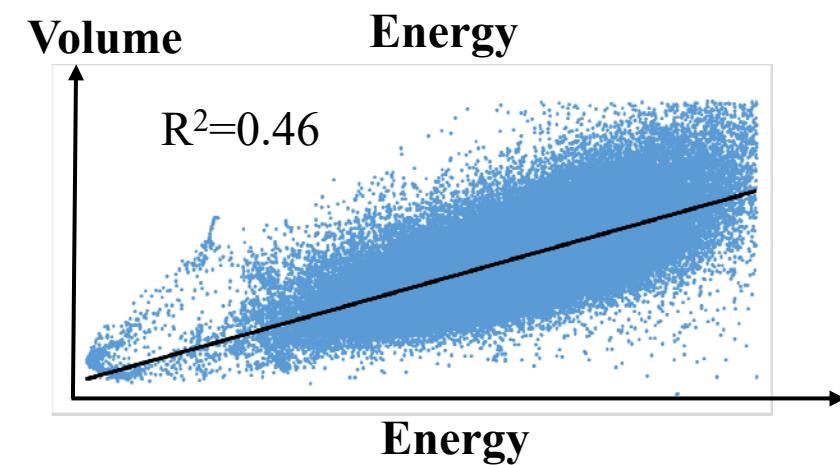
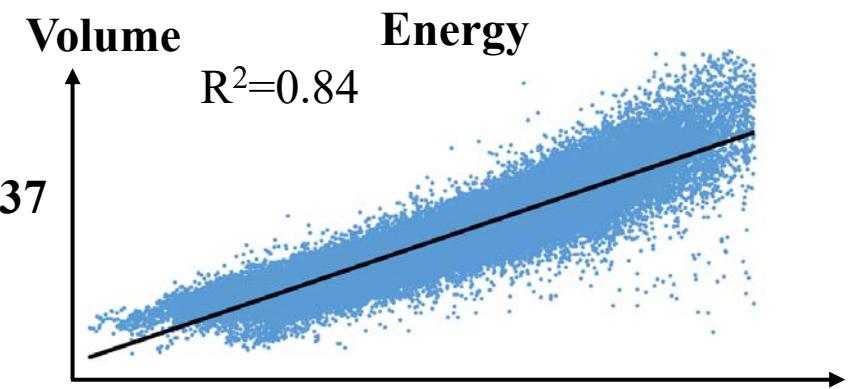
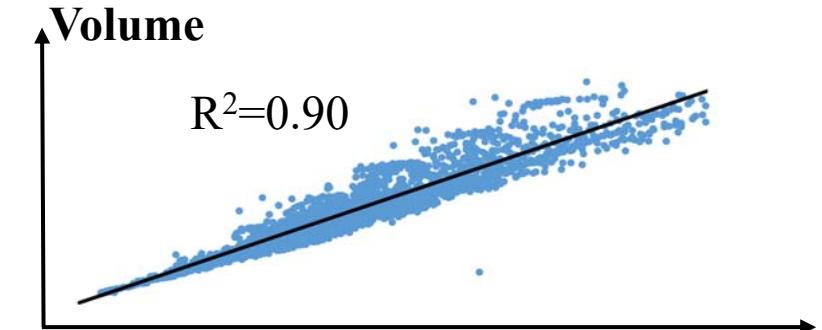
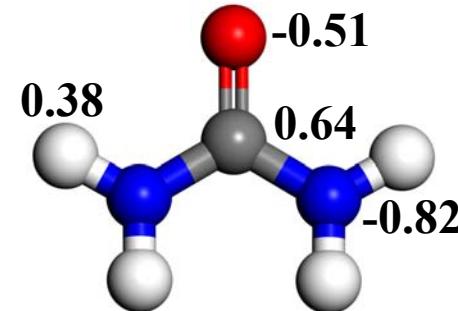
Lennard-Jones



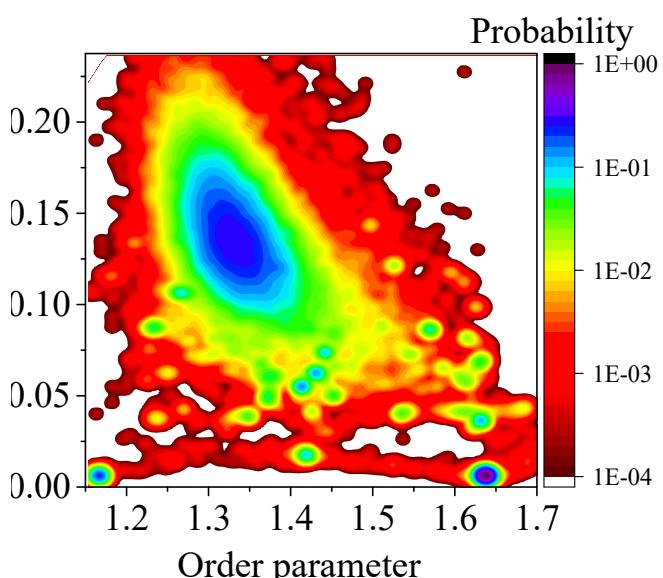
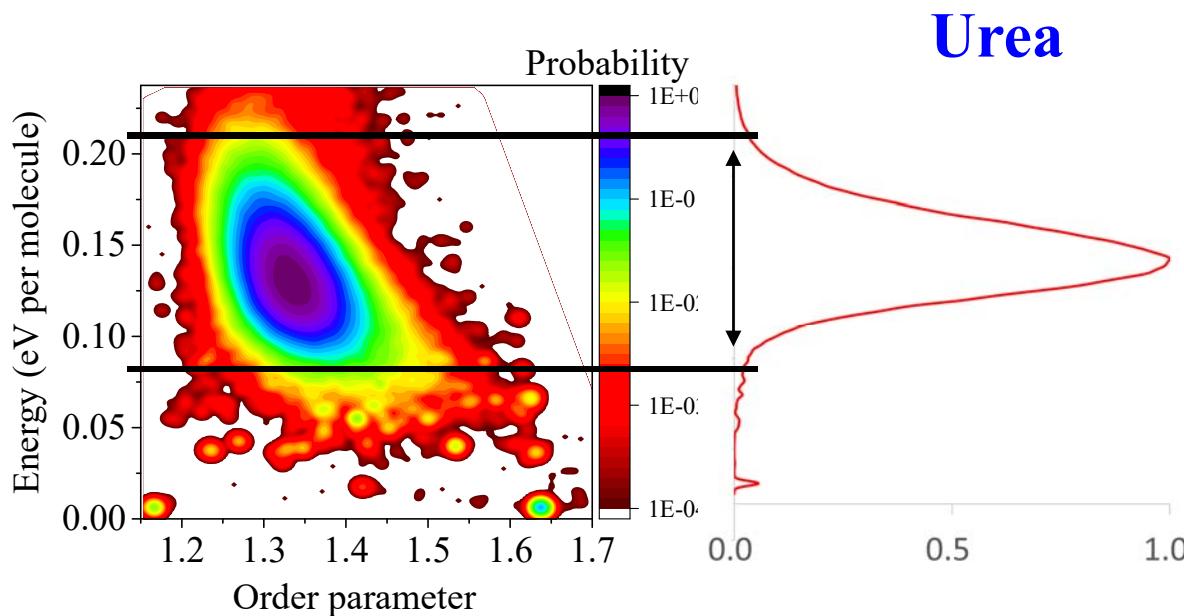
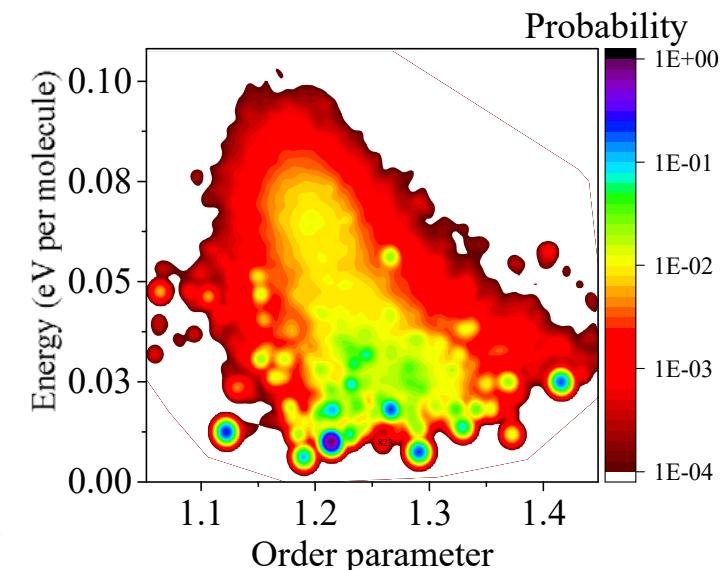
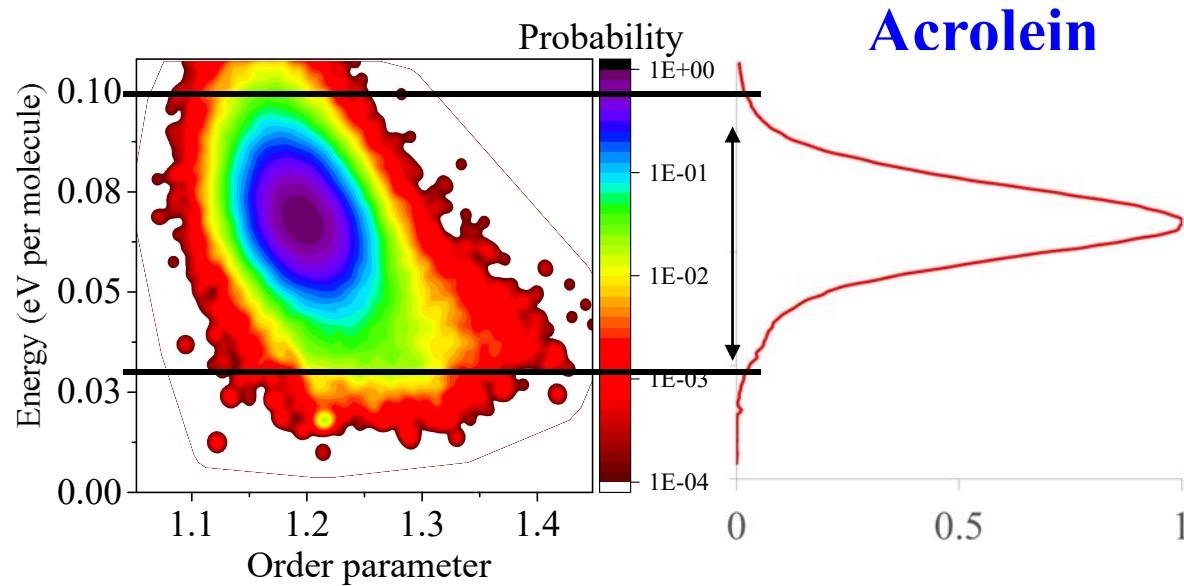
Acrolein
(Non-polar)



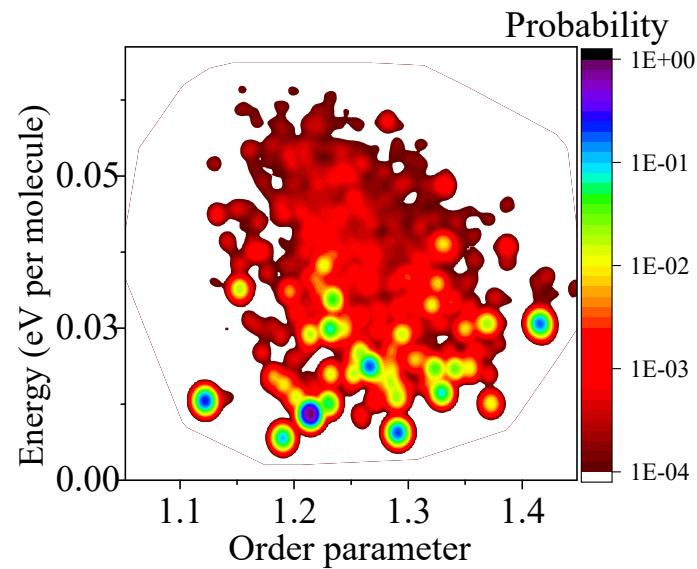
Urea
(Hydrogen-bonded)



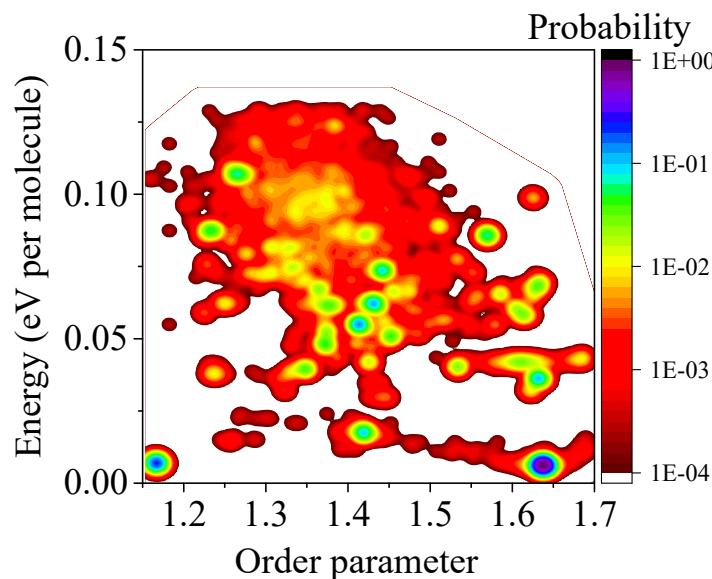
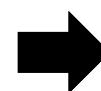
◆ Potential energy surface of acrolein and urea



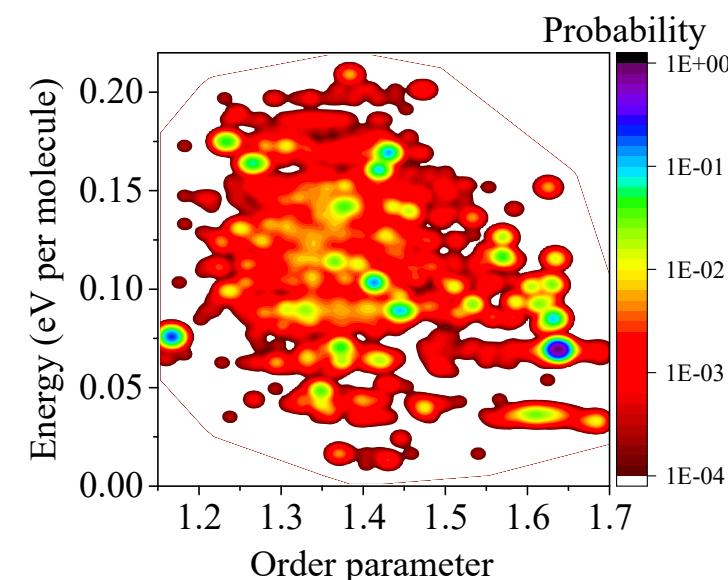
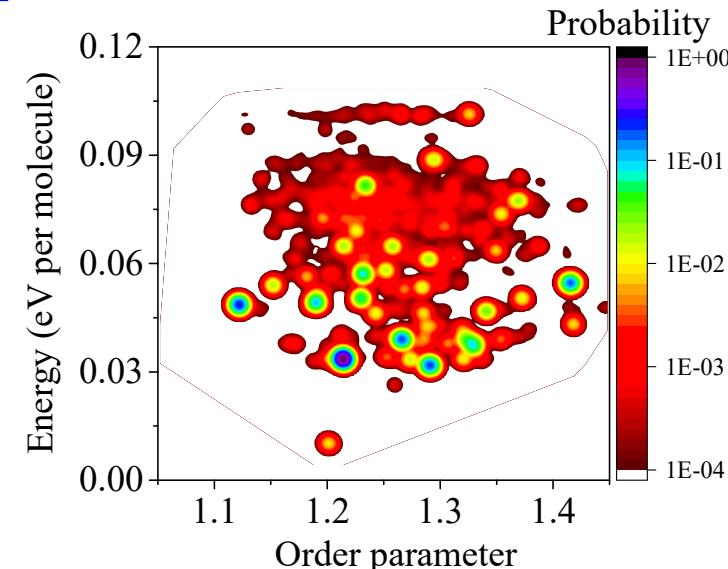
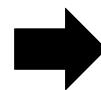
◆ DFT refinement



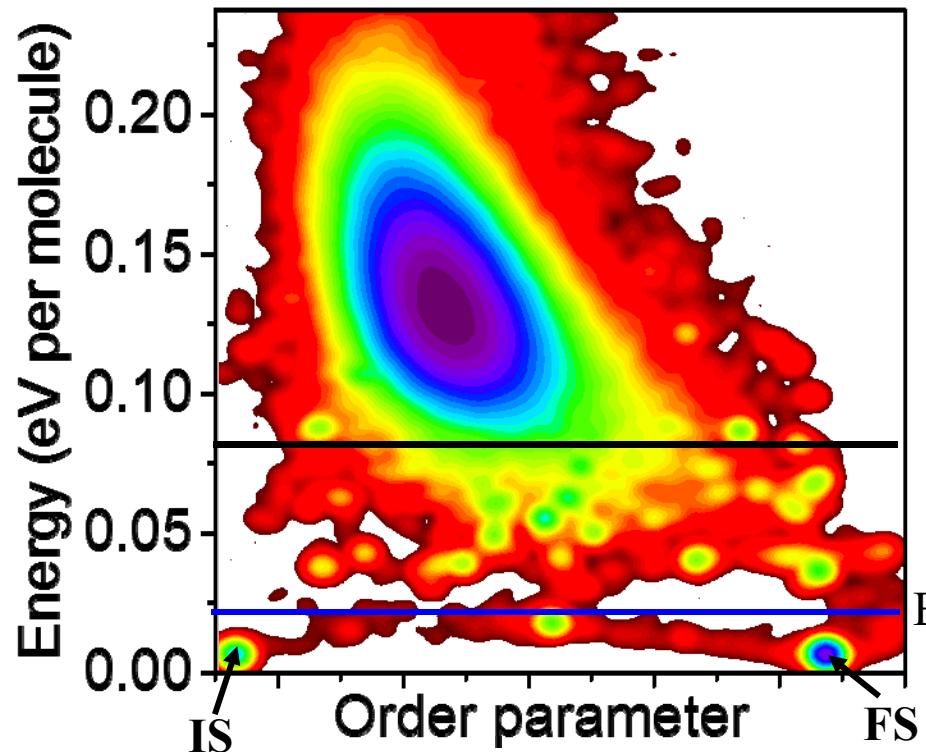
Acrolein



Urea

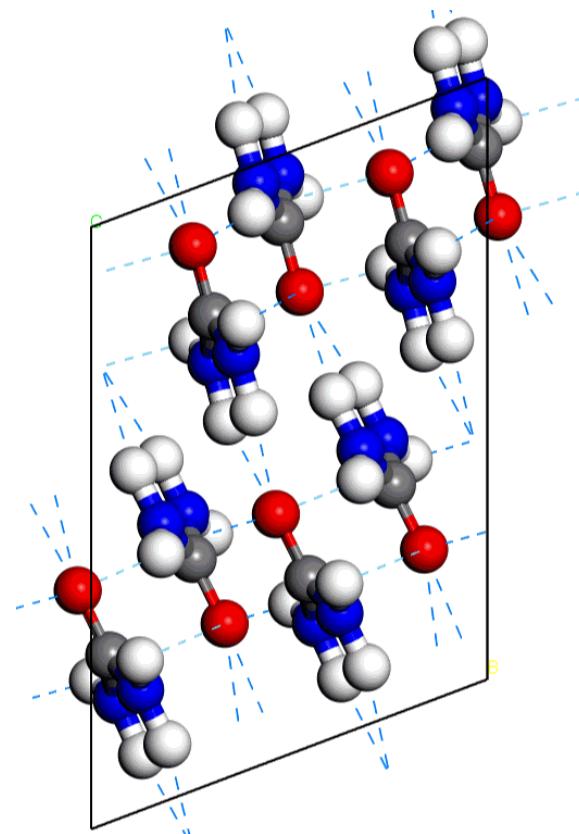
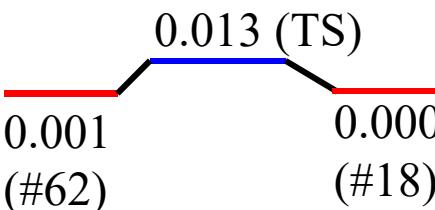


◆ Phase transition of urea

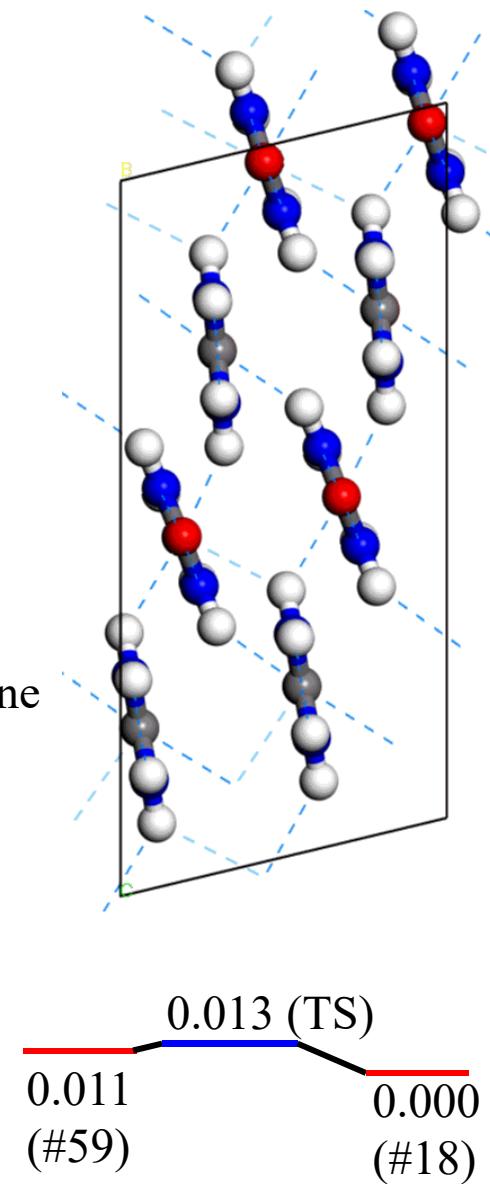
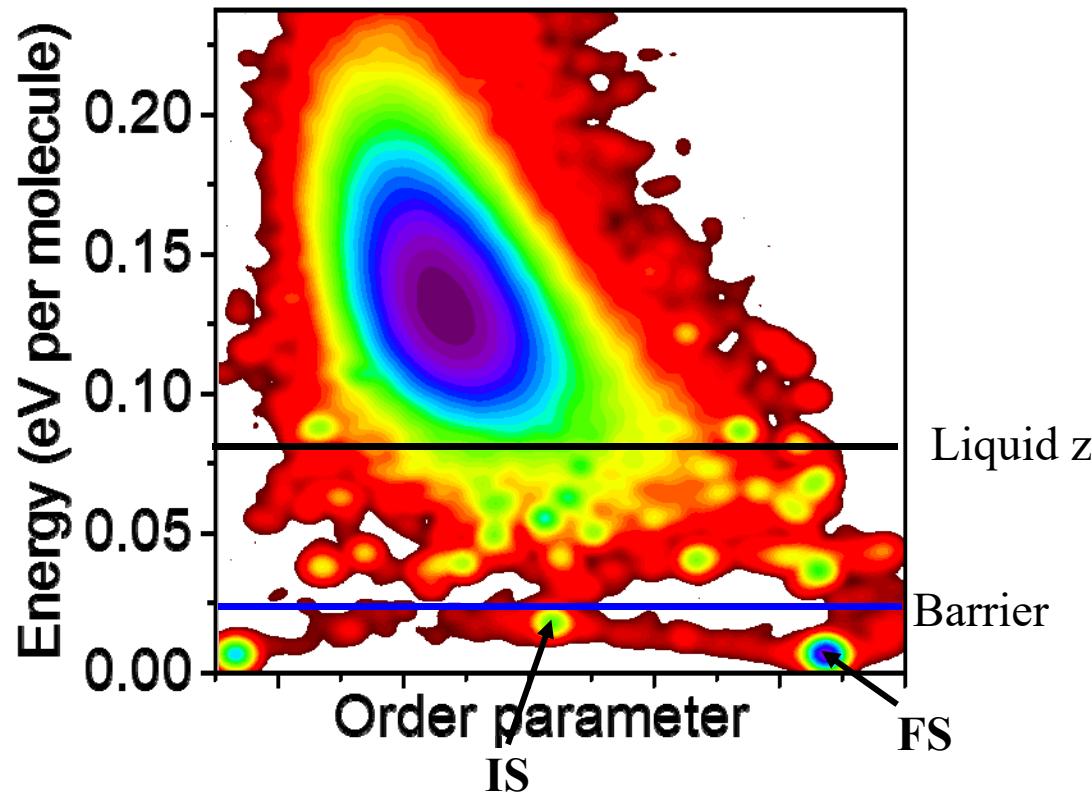


Liquid zone

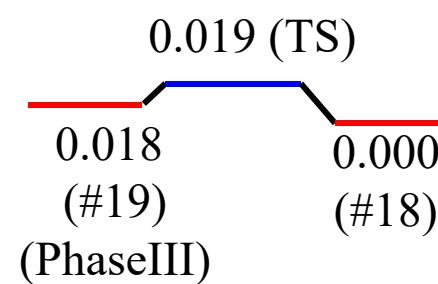
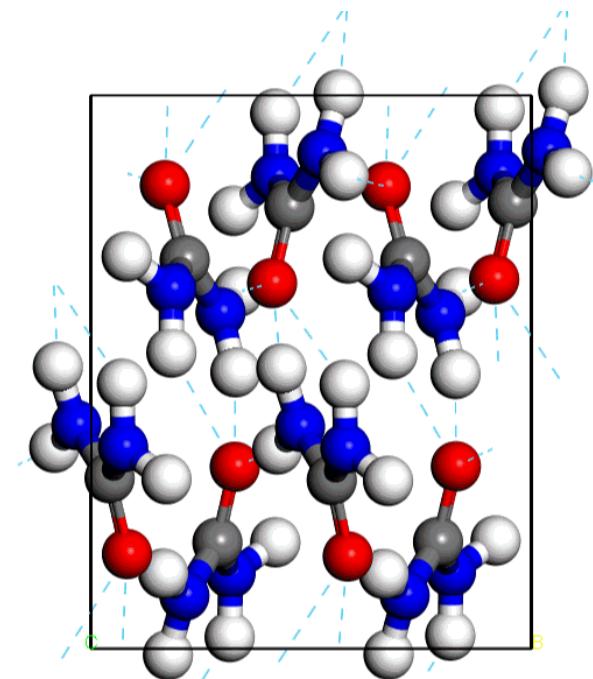
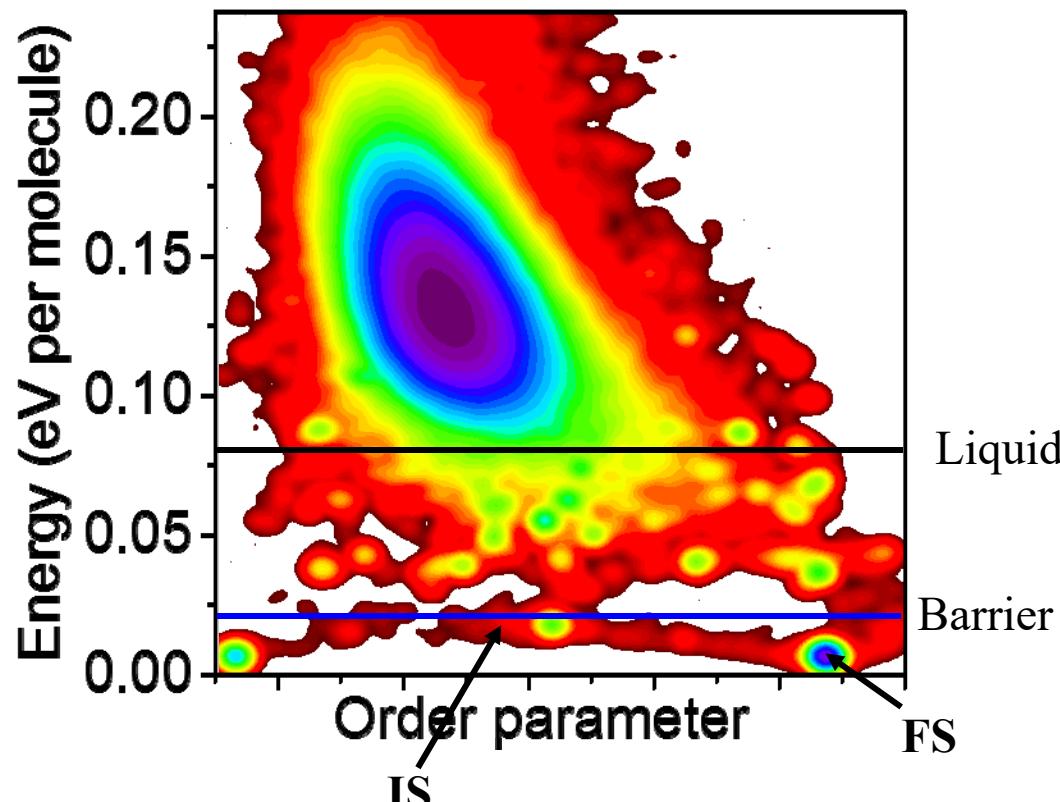
Barrier



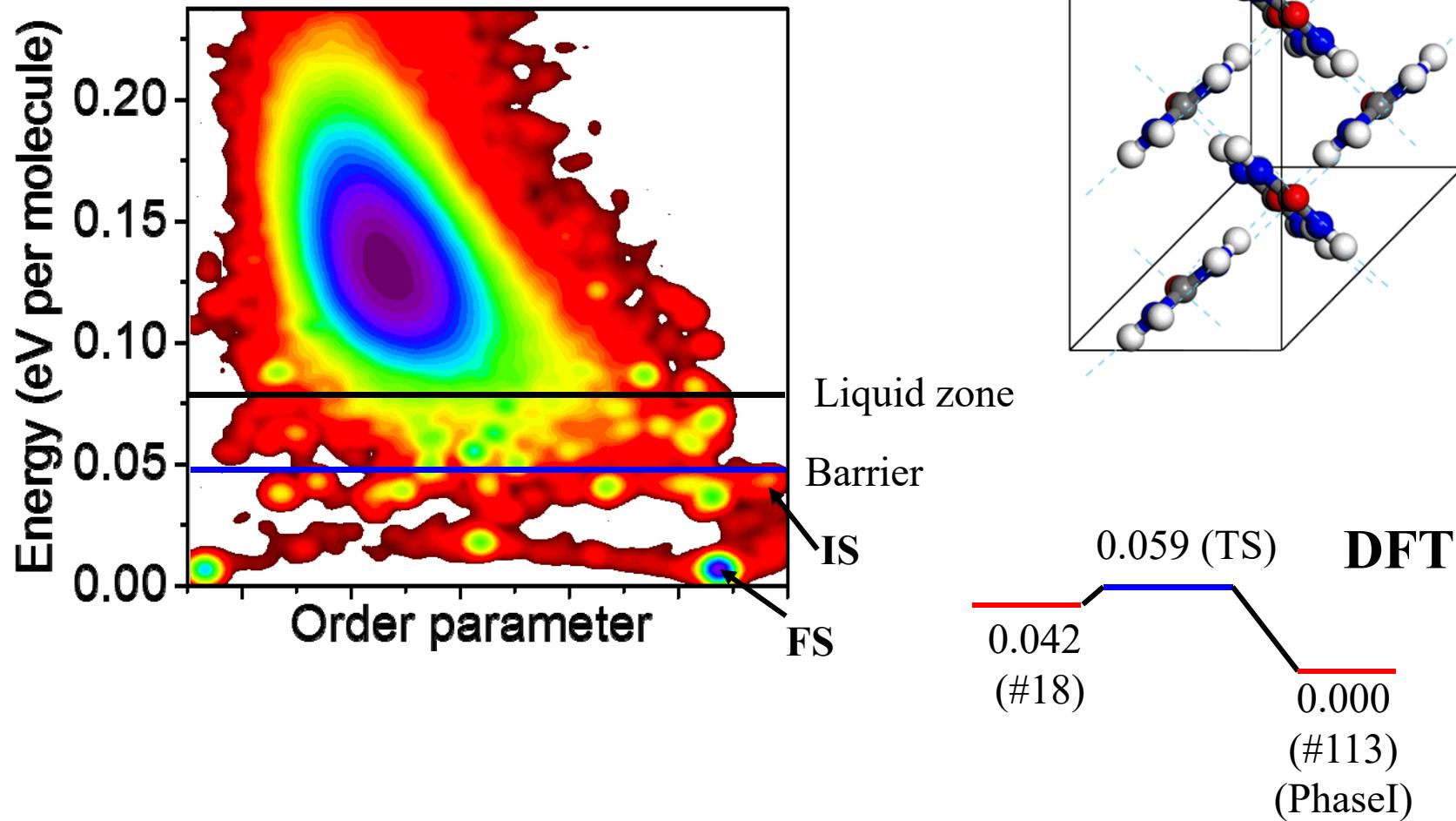
◆ Phase transition of urea



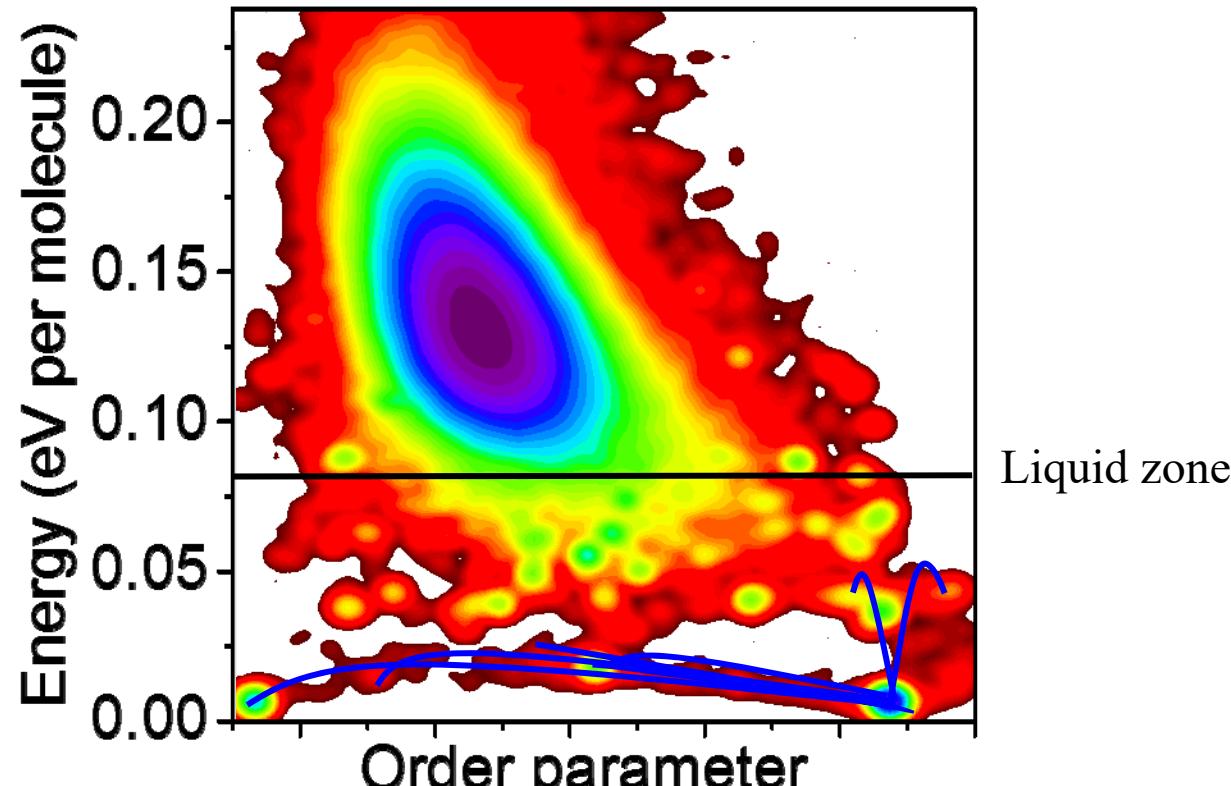
◆ Phase transition of urea



◆ Phase transition of urea

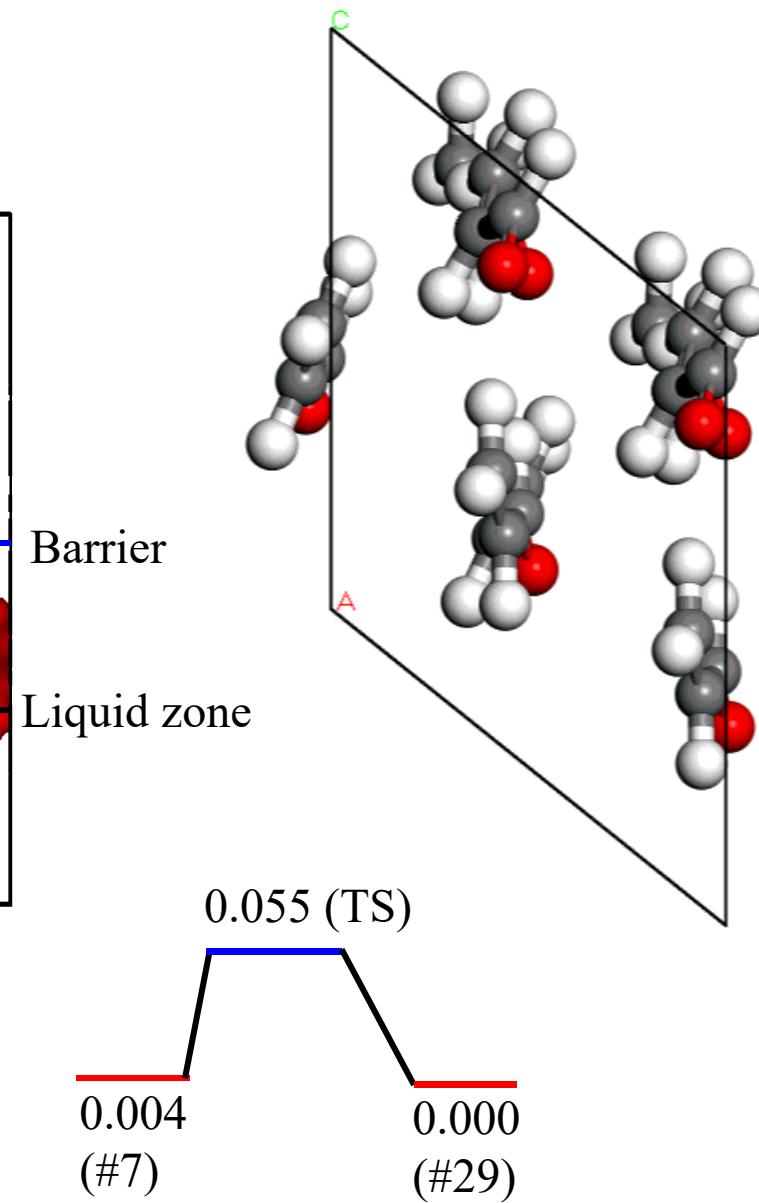
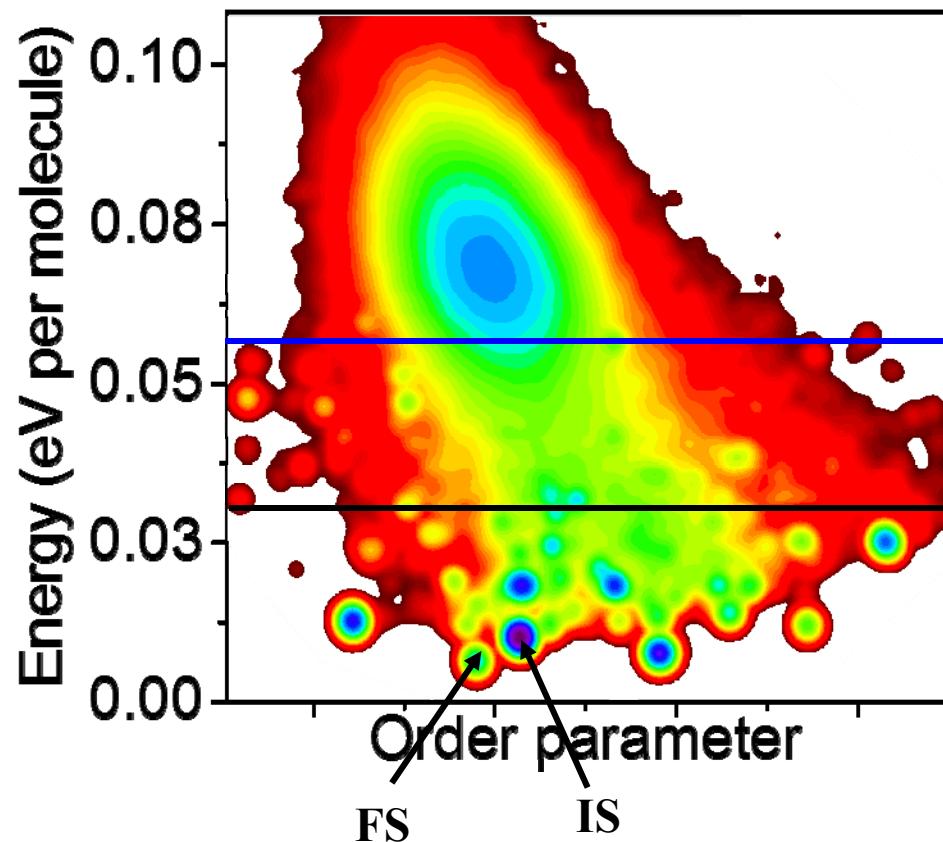


◆ Phase transition of urea

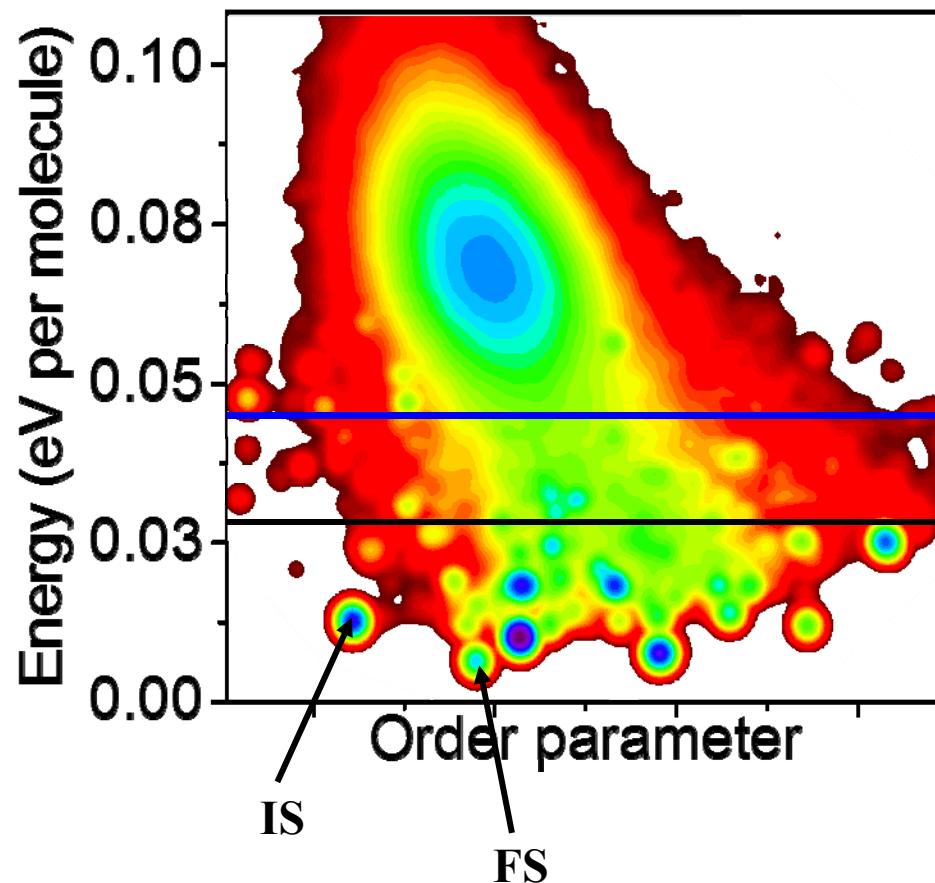


◆ H-bond network is kept during phase transition

◆ Phase transition of acrolein

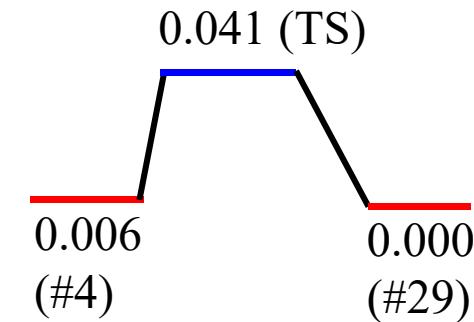
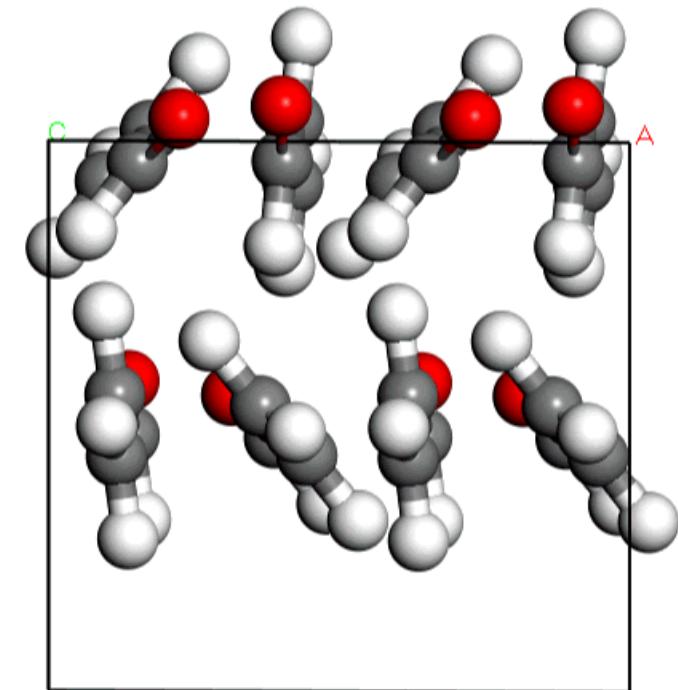


◆ Phase transition of acrolein

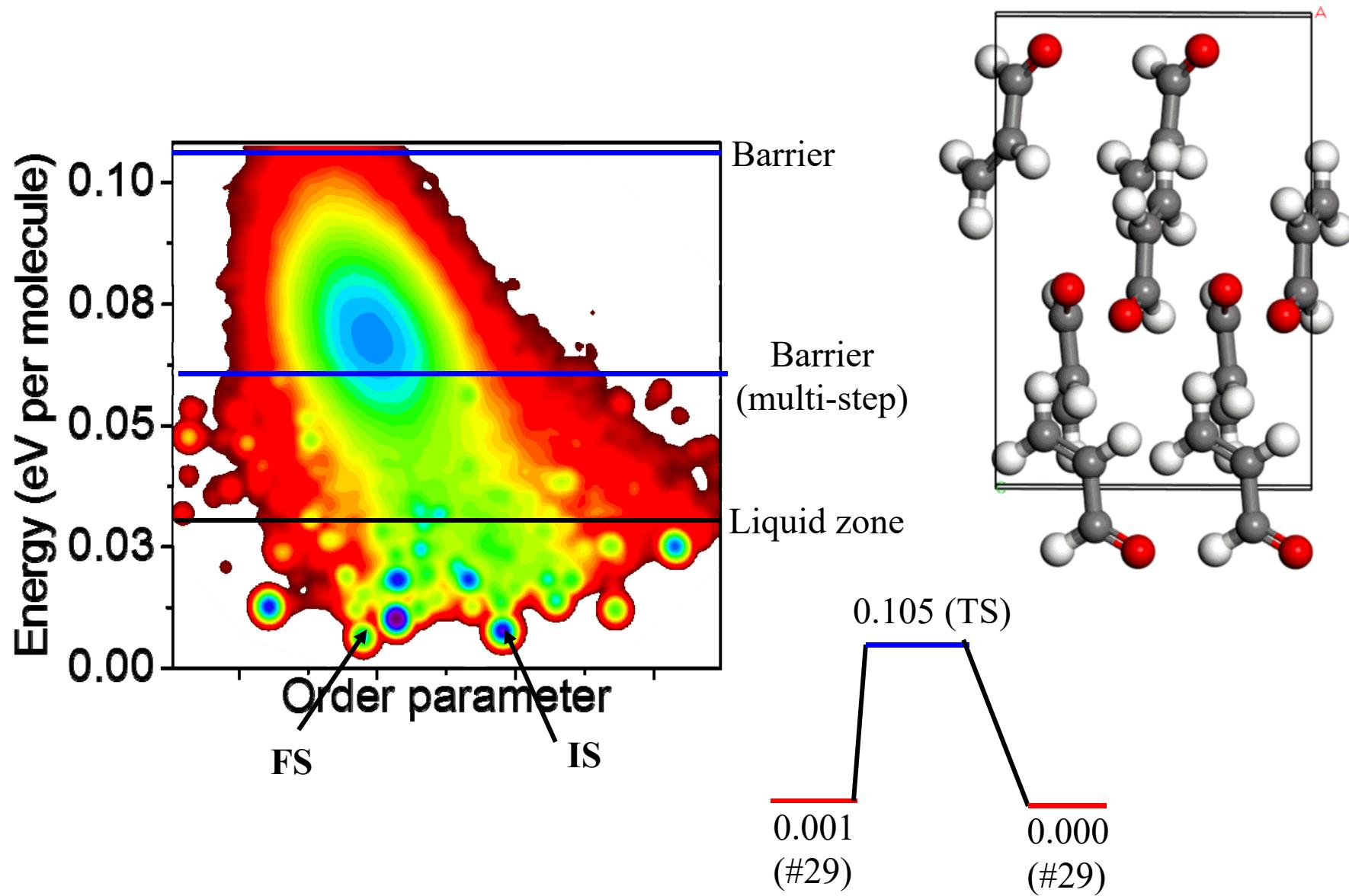


Barrier

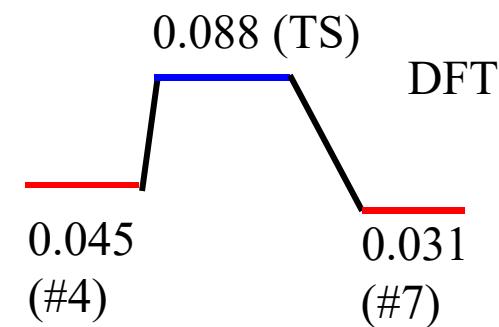
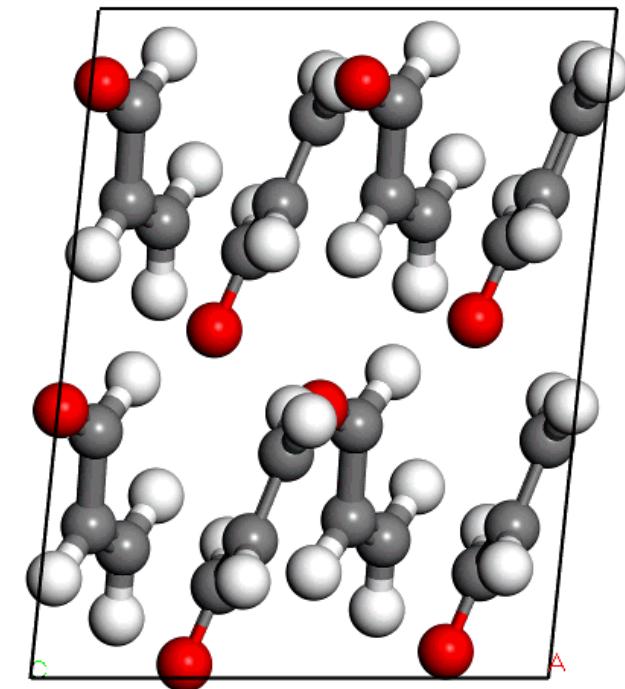
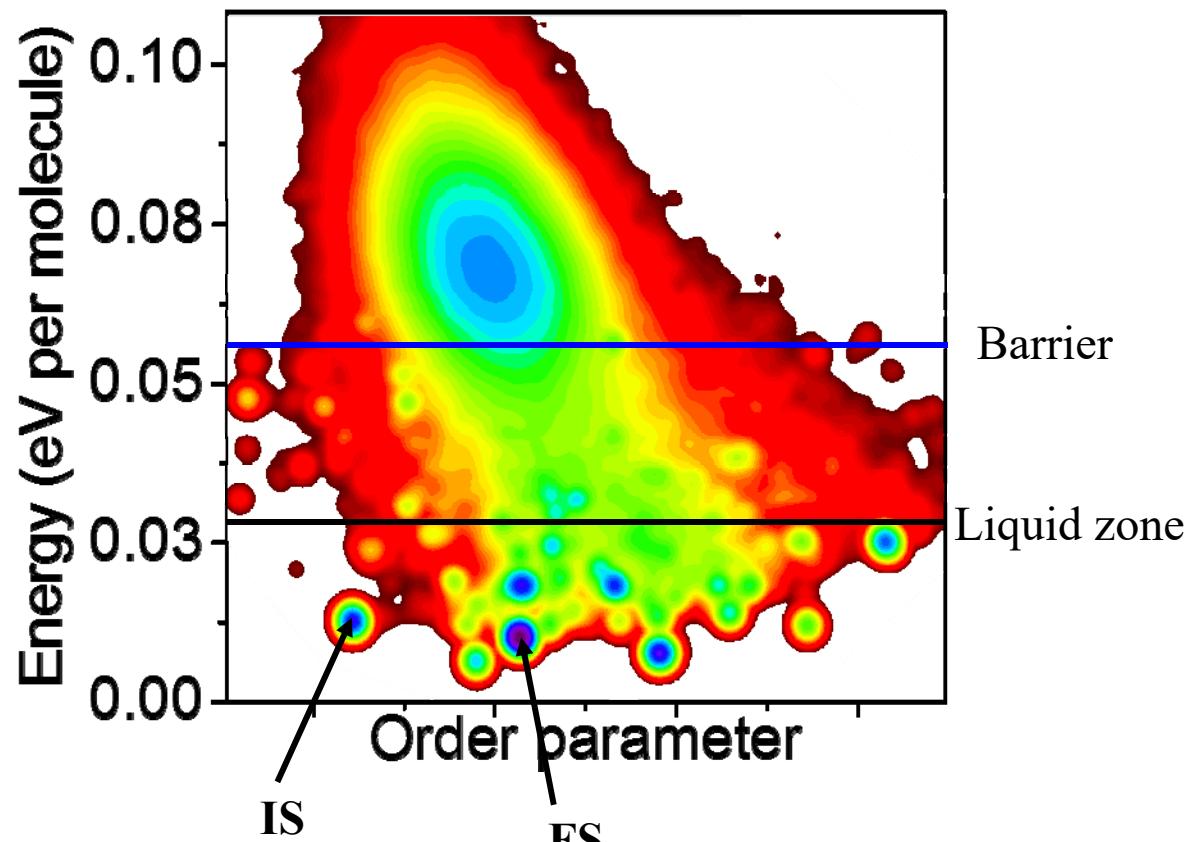
Liquid zone



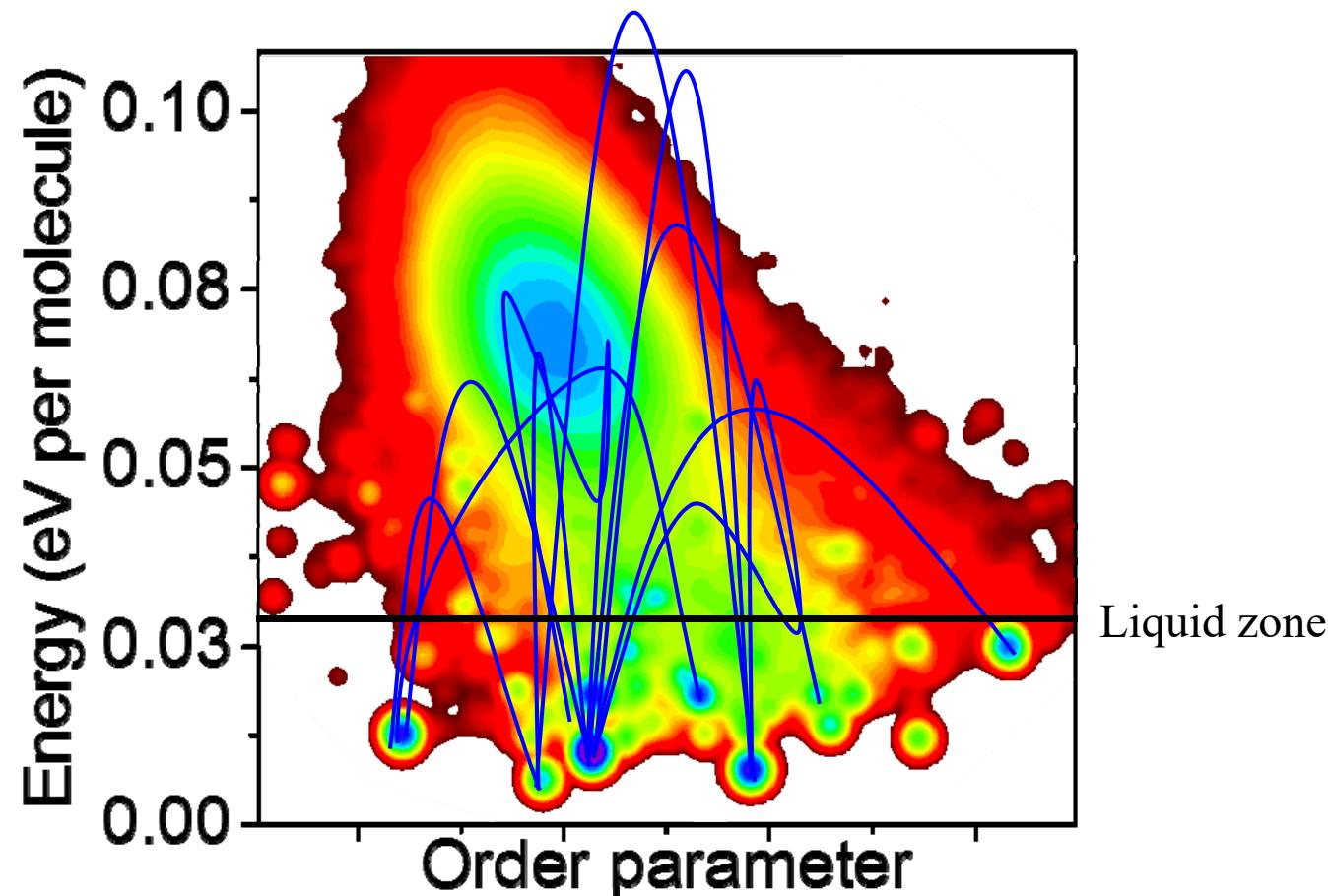
◆ Phase transition of acrolein



◆ Phase transition of acrolein



◆ Phase transition of acrolein



- ◆ No preferred orientation in solid forms.
- ◆ High barrier is resulted from molecules flipping during phase transition

◆ Summary:



- ◆ Identified the liquid-like zone and the distance between the GM and the lower boundary of the liquid-like zone.

- ◆ For non-polar molecules, the barrier of possible phase transition is high, making the transition from any stable phase to the GM difficult.

◆ Acknowledgement



National Natural Science
Foundation of China
国家自然科学基金