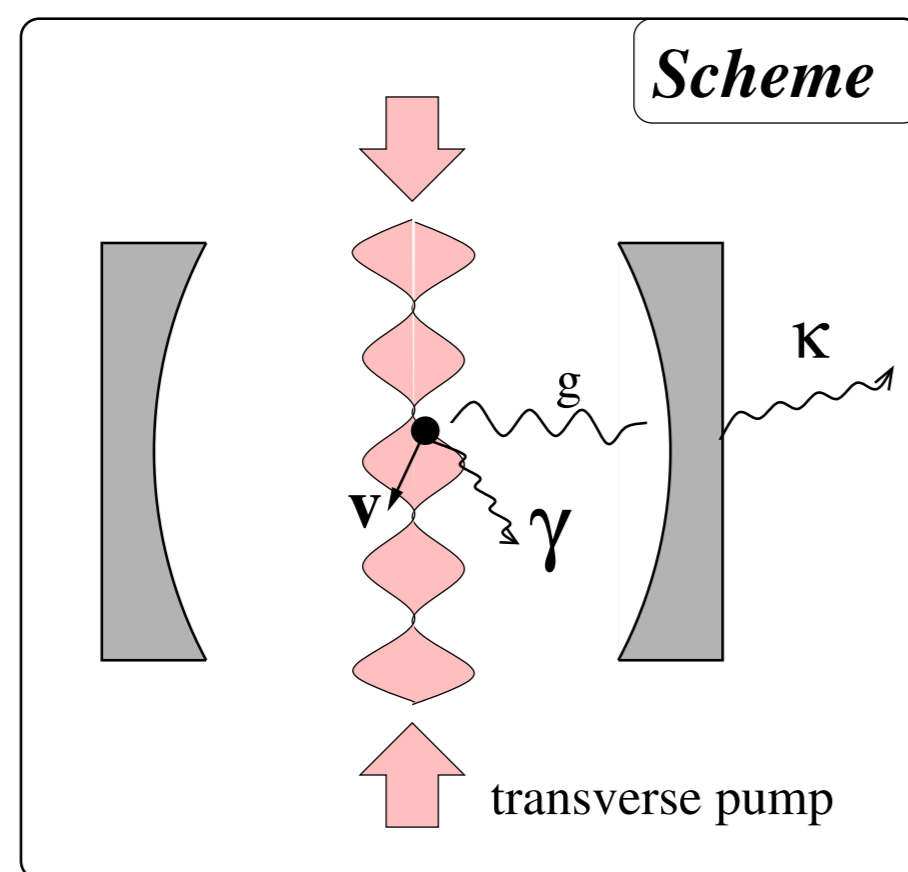


# Interference effects in the cavity-assisted laser cooling of single atoms and atomic ensembles

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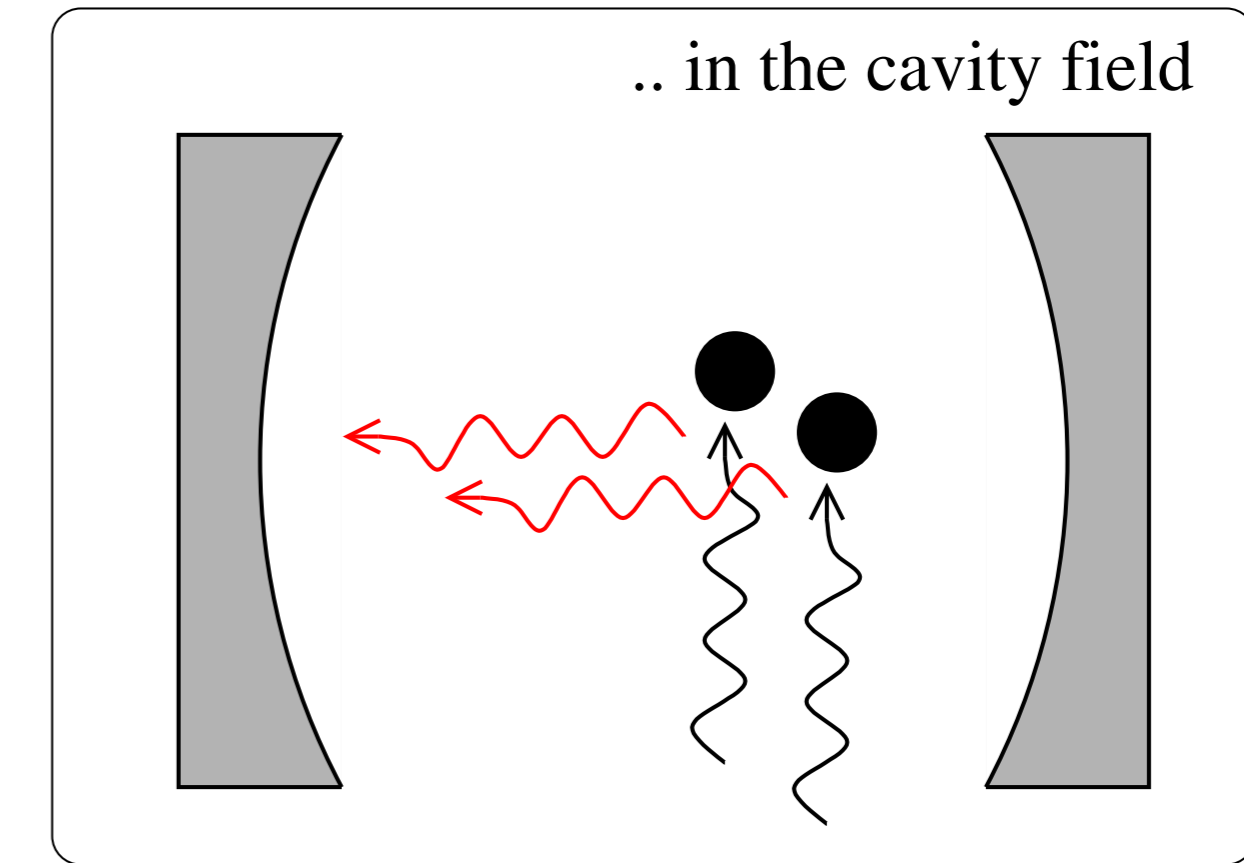
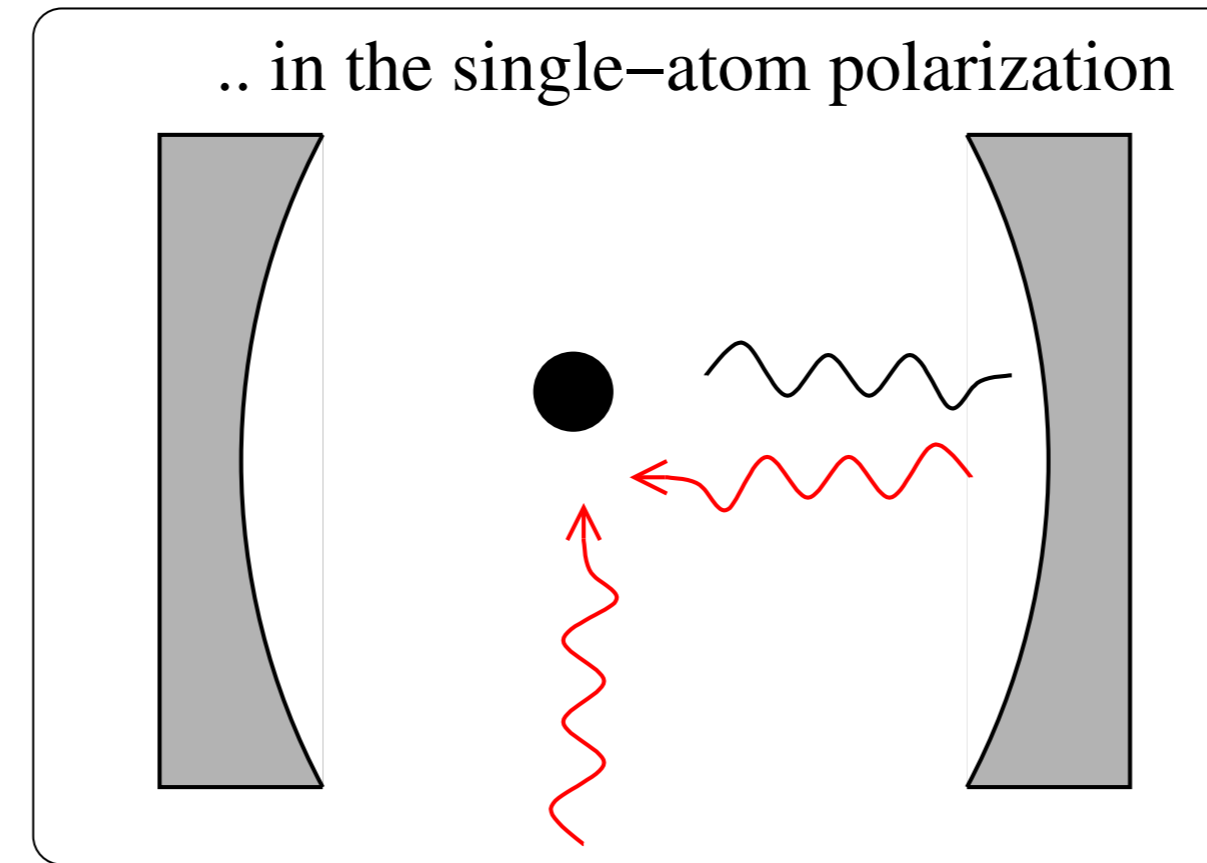
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## 1 Laser-driven atoms in a cavity

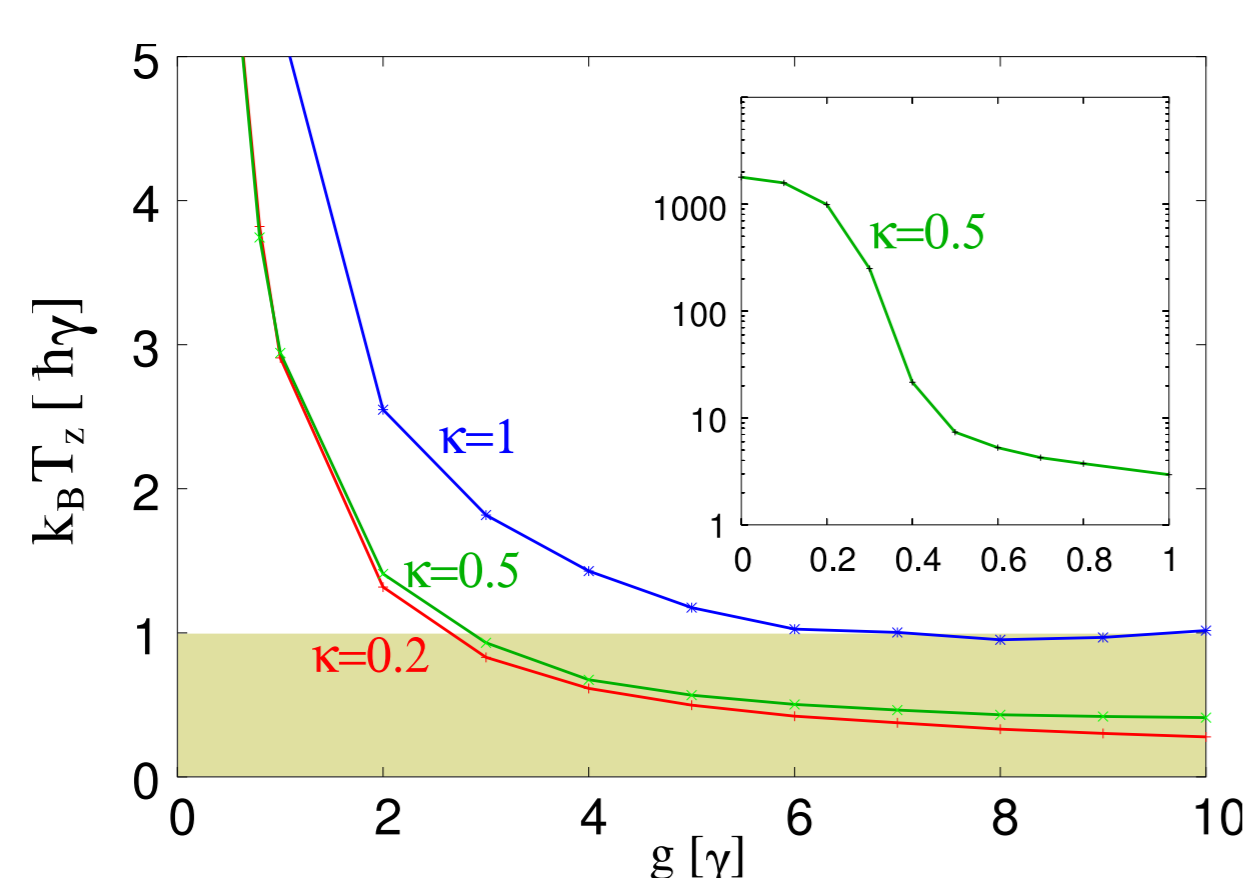


- Strong coupling:  
 $g \sim \gamma$
- High-Q cavity:  
 $\kappa = 0.5\gamma$
- Far detuned pump:  
 $\Delta_A = -350\gamma$
- Near-resonant mode:  
 $\Delta_C = -0.6\gamma$

## 2 Interference effects



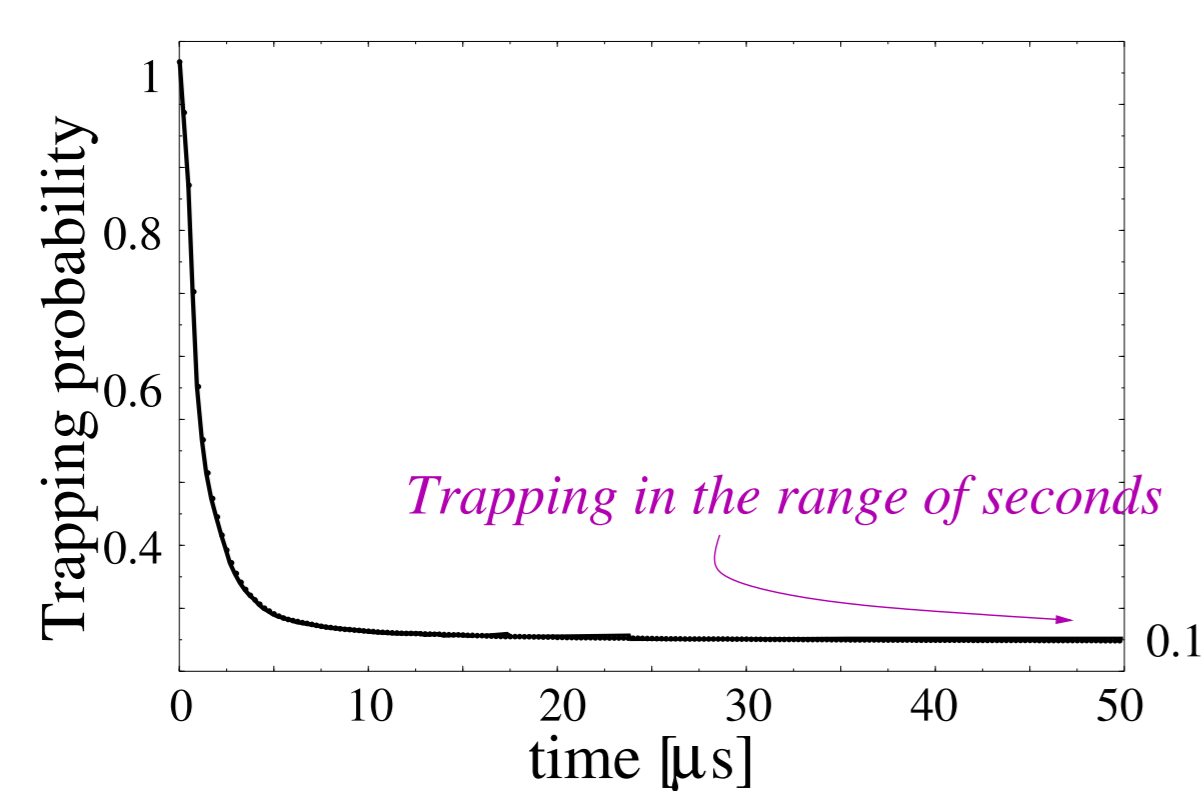
## 3 Temperature strongly depends on coupling $g$



$g = 0 \rightarrow \gamma$ :  $\Delta T_z \sim 3$  orders of magnitude

sub-Doppler regime  $\rightarrow$  very long trapping times

## 4 Trapping probability



Trapping probability decays as a sum of two exponentials (atoms are initially at Doppler-temperature).

## 5 Anomalous Doppler effect

Velocity-dependent interference in the atomic polarization.

$$\langle \sigma \rangle = \frac{\eta t}{i\Delta_A - \gamma + \frac{g^2}{i\Delta_C - \kappa} - ikv_z \left(1 - \frac{g^2}{(i\Delta_C - \kappa)^2}\right)}$$

$$= \frac{\eta t + g \langle a^{(0)} \rangle}{i(\Delta_A - kv_z) + \gamma} + \frac{v_z g \langle a^{(1)} \rangle}{i\Delta_A + \gamma}$$

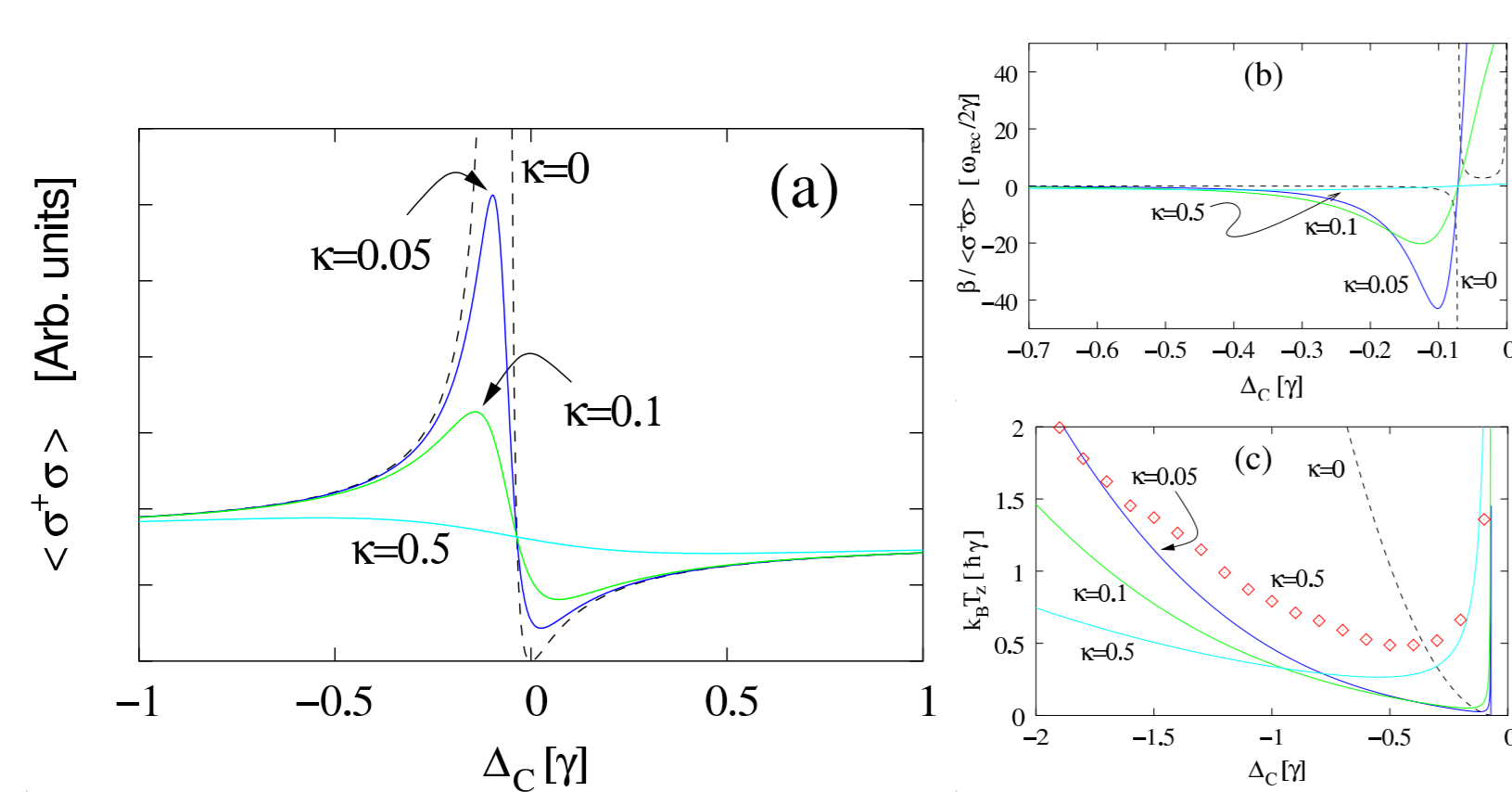
$= \text{adiabatic} + \text{nonadiabatic}$

$$(g/\kappa)^2 = \begin{cases} 100 & \text{(MPQ)} \\ 20 & \text{(Caltech)} \end{cases}$$

Ultra-sensitivity to atomic motion  $\rightarrow$  large friction at low velocities

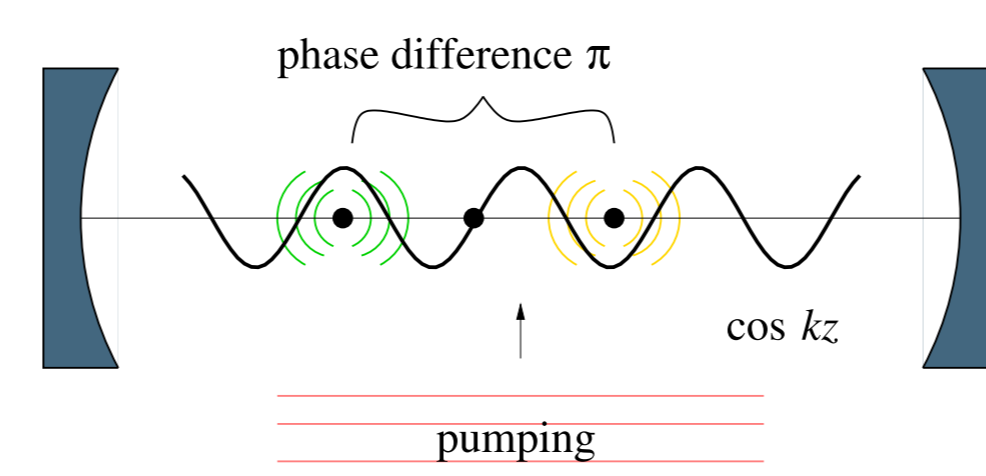
## 6 Polariton cooling

Resonance at  $\Delta_A \Delta_C \approx g^2$  & width  $\approx \kappa + (\gamma - \kappa)g^2/\Delta_A^2$

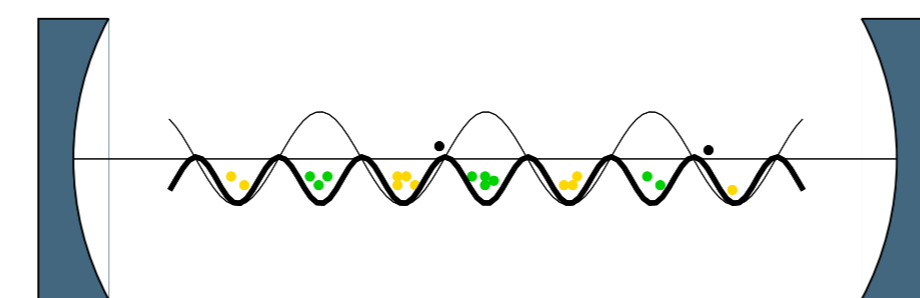


Reference: P. Domokos, A. Vukics, H. Ritsch, Phys. Rev. Lett. 92, 103601 (2004).

## 7 Scattering into the cavity mode

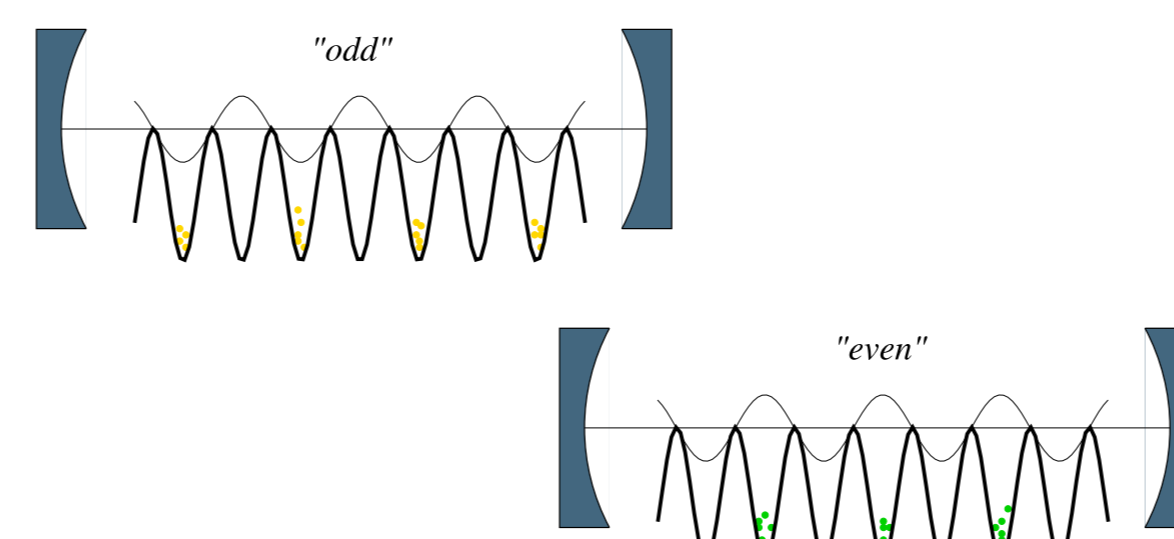


Destructive interference for uniform distribution. Finite number of atoms (fluctuations)  $\Rightarrow$  shallow trapping sites are at the antinodes for red detuning.



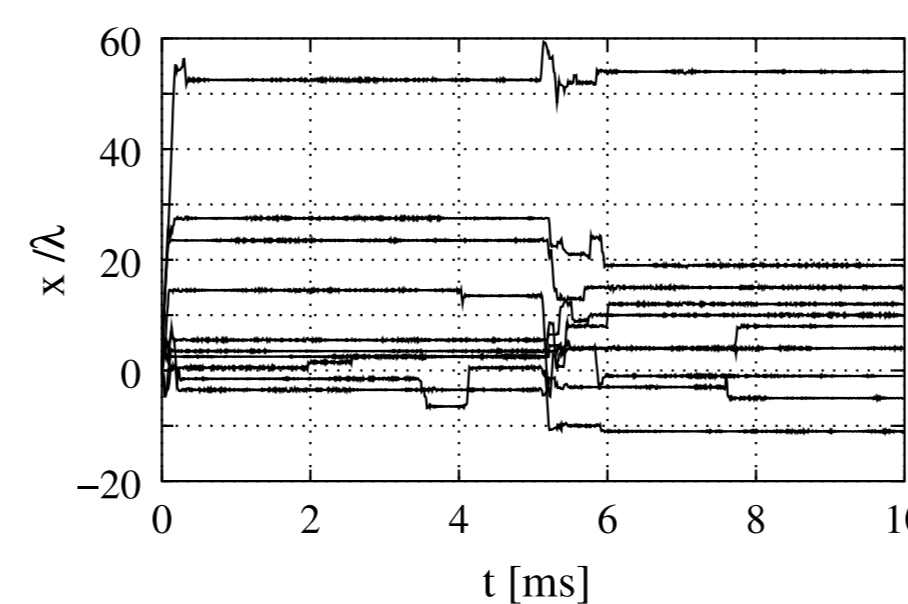
Localisation with a periodicity  $\lambda/2$  occurs?

## 8 Self-organization



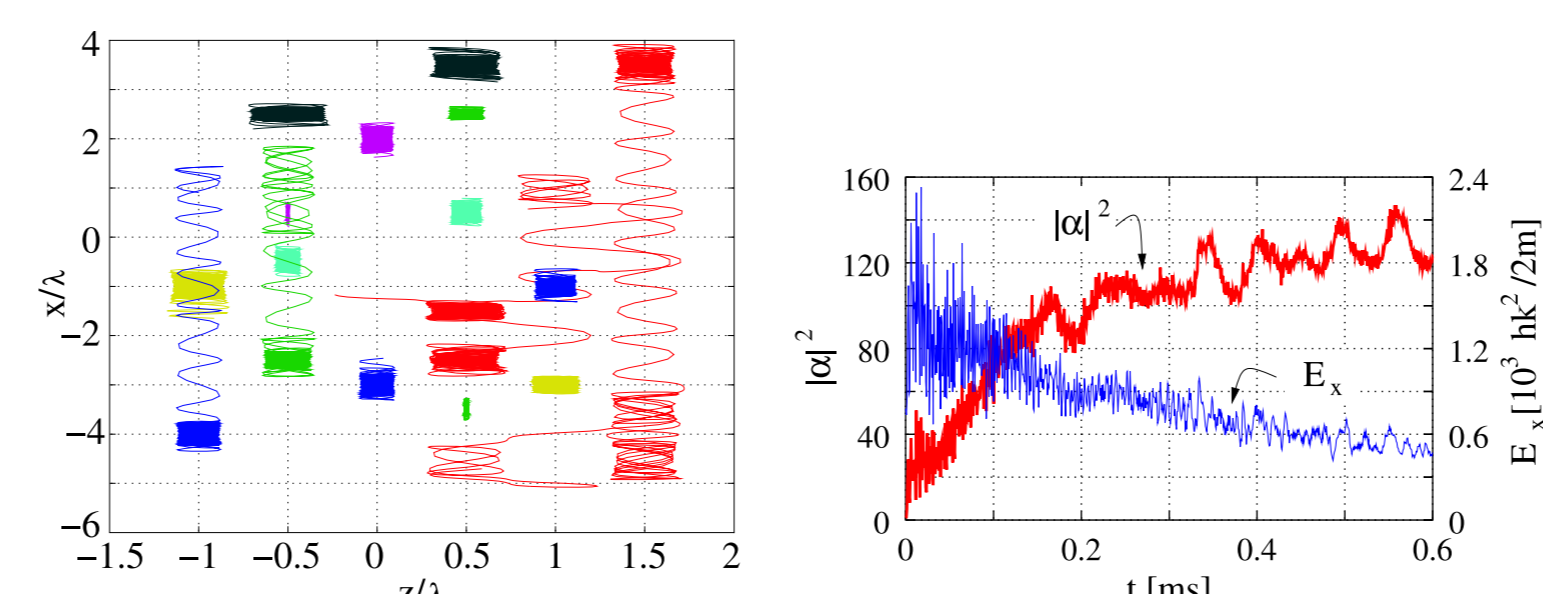
The atoms self-organize into one of the two possible patterns with  $\lambda$  periodicity. They fall into deep potential wells, the energy is dissipated by cavity cooling mechanism.

## 9 One-dimensional motion



$N=10$ ,  $(g, \kappa, \gamma)=(50, 10, 20)/\mu\text{s}$ ,  $\Delta_A = -500\gamma$ ,  $\eta = 1000/\mu\text{s}$  (mean photon number about 7),  $M=85$  (Rb).

## 10 Three-dimensional motion



$N=20$ ,  $(g, \kappa, \gamma)=(30, 10, 20)/\mu\text{s}$ ,  $\Delta_A = -100\gamma$ ,  $\eta = 2500$ .

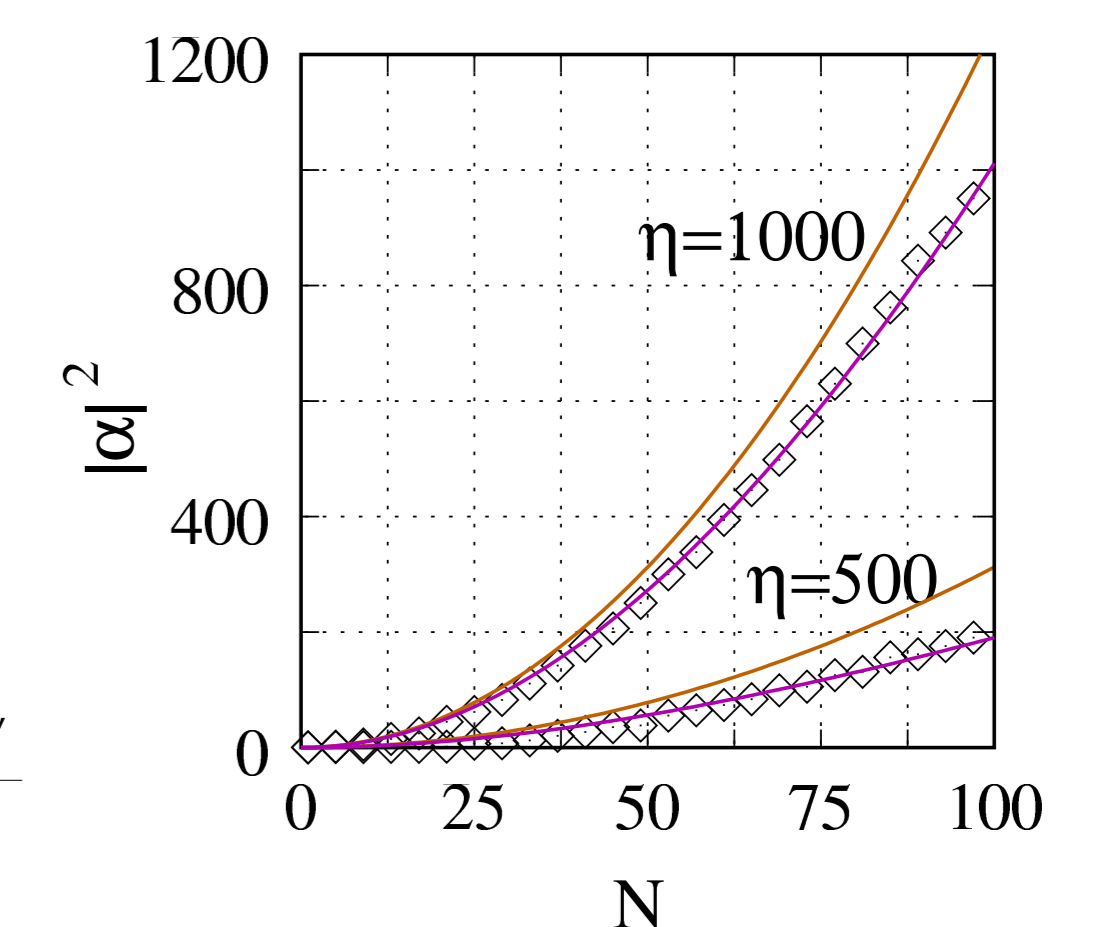
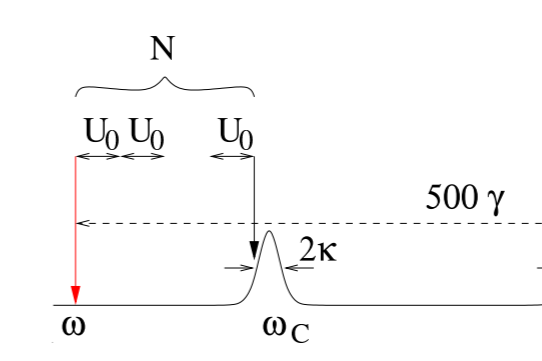
## 11 Superradiance

$$\Delta_C - NU_0 = \kappa$$

$$\kappa = \gamma/2$$

$$U_0 = \gamma/80$$

Saturation  $< 0.06$

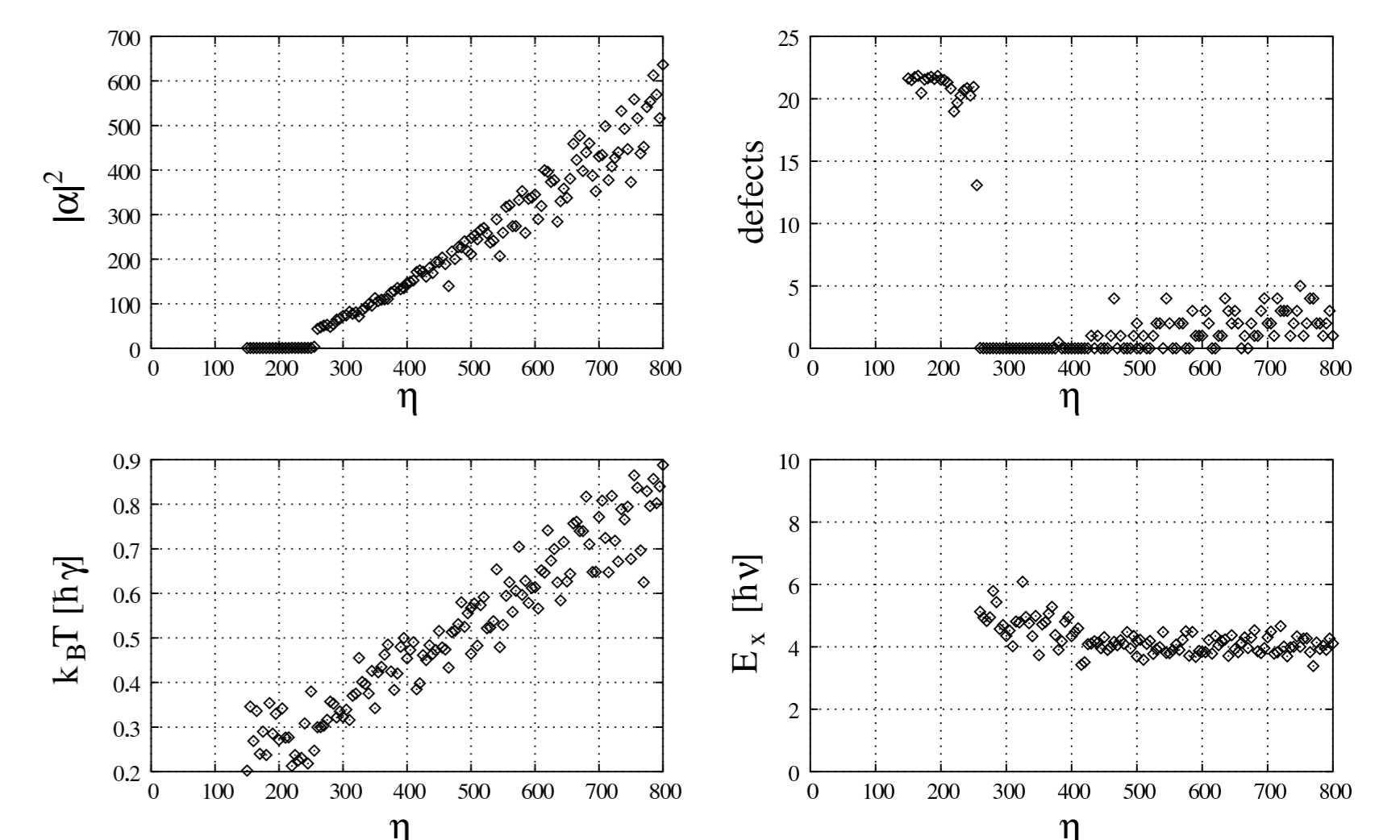


$$|\alpha|^2 = N^2 \frac{|\eta_{\text{eff}}|^2}{\kappa^2} \frac{(1 - k^2 x^2)}{1 + [1 + (U_0 N / \kappa) k^2 x^2]^2}$$

$$x^2 = 0$$

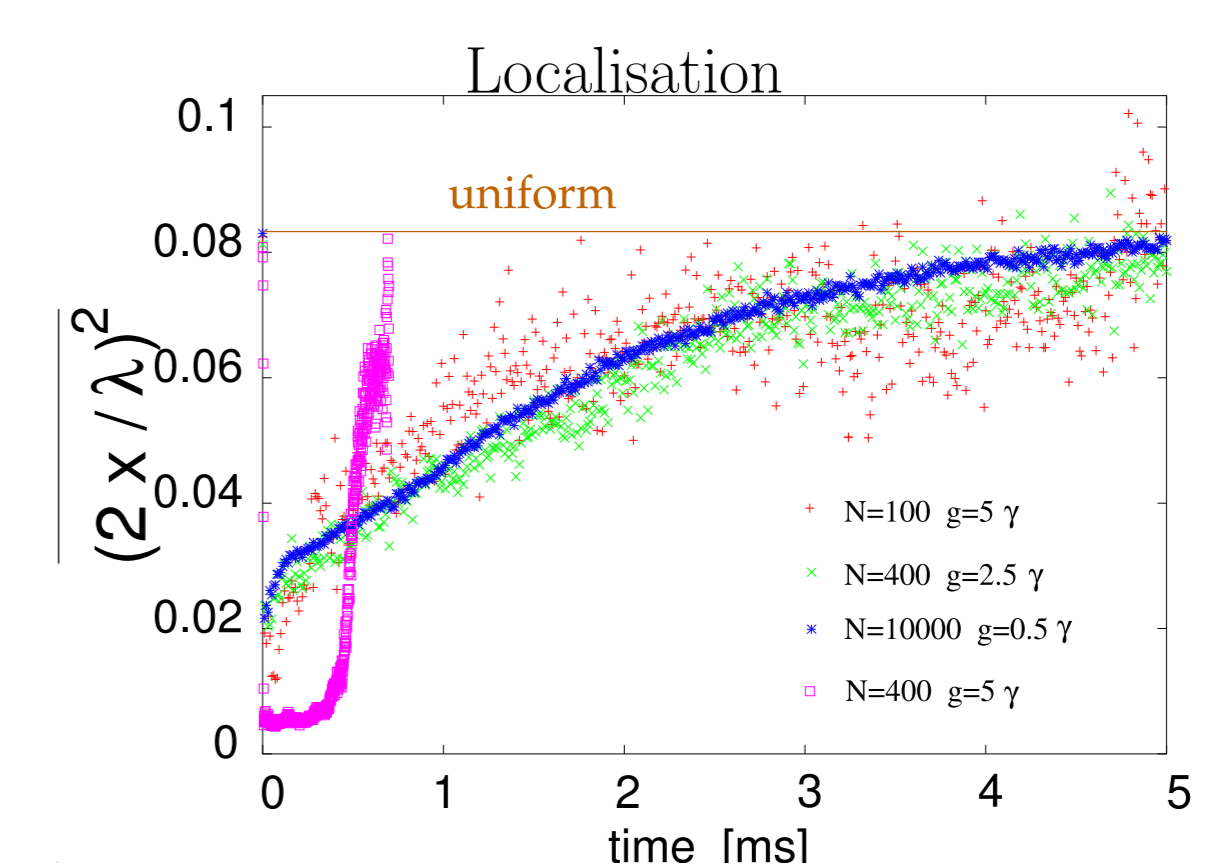
$$k^2 x^2 = 0.14 \quad (\eta = 500), \quad k^2 x^2 = 0.06 \quad (\eta = 1000)$$

## 12 Threshold and temperatures



$N=50$ ,  $(g, \kappa, \gamma)=(100, 10, 20)/\mu\text{s}$ , saturation  $< 0.1$

## 13 Scaling for large ensemble



Pattern formation is independent of  $Ng^2$ .

Reference: P. Domokos and H. Ritsch, Phys. Rev. Lett. 89, 253003 (2002).

## 14 Quantum Monte Carlo wavefunction simulations of cavity cooling

