

# Photonic devices for quantum information processing:

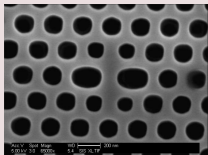
coupling to dots, structure design and fabrication

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Optoelectronics Group, Cavendish Lab



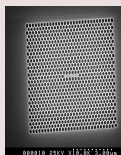
## Vuckovic's group



## Noda's group



## Mine



# Outline

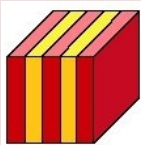
- 1 The ingredients
  - Photonic crystals
  - Quantum dots
- 2 The theoretical cake
  - Solid-state cavity QED!
  - The add-drop filter
- 3 Designing the recipe
  - Working principle
  - Simulations
- 4 Issues on the fabrication of the cake
  - Microfabrication
- 5 Conclusion and further cakes

# Photonic crystals

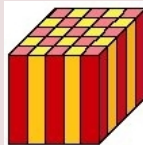
## Definition

Structure with periodic modulation of dielectric constant in space

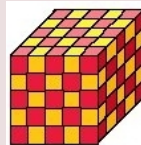
1D



2D



3D



# Photonic crystals

## Definition

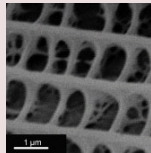
Structure with periodic modulation of dielectric constant in space

1D



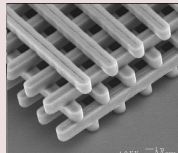
GaAs/AlAs stack

2D



Butterfly wing

3D



Si based

# Photonic crystals

## Definition

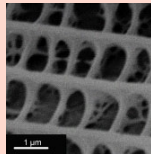
Structure with periodic modulation of dielectric constant in space

1D



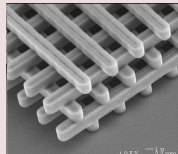
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2D



Butterfly wing

3D



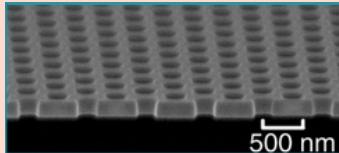
Si based

# Photonic crystals

## Definition

Structure with periodic modulation of dielectric constant in space

### 2D slabs



Free-standing membrane of air holes  
in semiconductor

# Photonic crystals

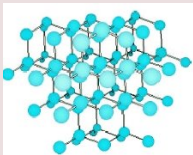
## Periodic medium and unit cell



# Photonic crystals

## Periodic medium and unit cell

### Electronic crystal

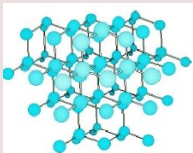


Atoms in diamond structure

# Photonic crystals

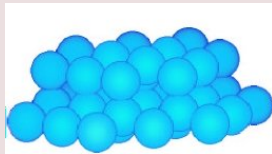
## Periodic medium and unit cell

### Electronic crystal



Atoms in diamond structure

### Photonic crystal



Dielectric spheres in  
diamond lattice

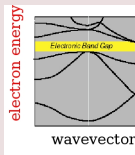
# Photonic crystals

## Bloch waves and bandgap formation

# Photonic crystals

## Bloch waves and bandgap formation

### Electronic crystal

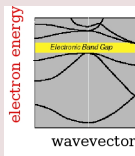


Atoms in diamond structure

# Photonic crystals

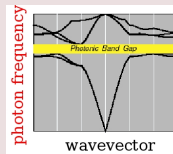
## Bloch waves and bandgap formation

### Electronic crystal



Atoms in diamond structure

### Photonic crystal



Dielectric spheres in  
diamond lattice

# Photonic crystals

## Definition

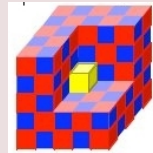
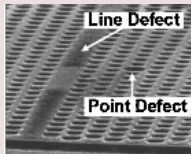
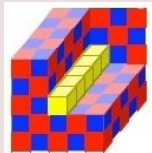
Structure with periodic modulation of dielectric constant in space

## It follows that...

- Photonic crystals present discrete translational symmetry
- Forbidden propagation of photons within certain energy ranges, in determined crystal directions
- Light transmission properties dictated by geometry, periodicity, and dielectric constants of media composing the crystal (*and not by some atomic-scale property!*)

# (Intentional) defects in photonic crystals

## Local breaking of translational symmetry ("photonic doping")

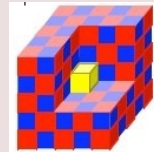
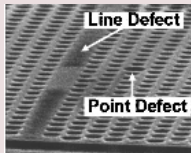
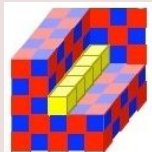


## Effect

Introduction of peaks in the density of states of the crystal falling within the bandgap

# (Intentional) defects in photonic crystals

## Local breaking of translational symmetry ("photonic doping")



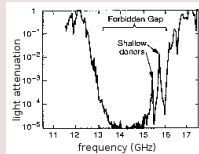
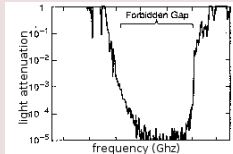
## Effect

Localized/evanescent field modes with complex wave vector become (physical) solutions of Maxwell's equations, decaying exponentially from the defect



# (Intentional) defects in photonic crystals

If defect = suppressed air holes ("donor defect") then

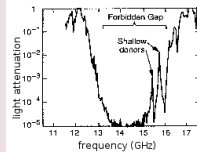
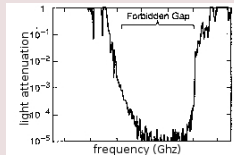


Unperturbed crystal → With defect

Tayloring defects → localization and trapping of evanescent modes

# Defect cavities in photonic crystals

If defect = suppressed air holes  
("donor defect") then



Unperturbed crystal  $\rightarrow$  With defect

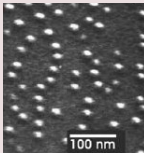
Tayloring defects  $\rightarrow$  localization and trapping of evanescent modes

# Quantum dots

## Definition

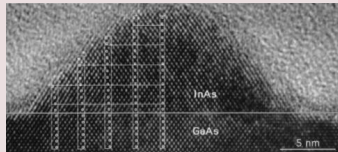
Semiconductor nanostructures confining carriers in 3D

### Self-assembled InAs dots



Density  
 $\sim 10^{10} \text{ dots/cm}^2$

### Nucleation by strain (lattice mismatch)



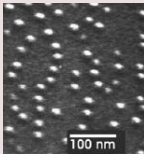
Grown by MBE on GaAs  
substrate

# Quantum dots

## Definition

Semiconductor nanostructures confining carriers in 3D

### Self-assembled InAs dots



Density  
 $\sim 10^{10} \text{ dots/cm}^2$

Bandgap InAs < GaAs  
↓  
carriers confined  
↓  
only discrete energy levels can  
be occupied

# Quantum dots

## Definition

Semiconductor nanostructures confining carriers in 3D

## It follows that...

- Carriers present a discrete spectrum: "artificial atoms"
- Photoemission range:  $\sim 900 - 1100\text{nm}$  (isotropic)
- Dipole moment:  $d \sim 10 - 100\times >$  atomic dipole moment  
→ enhanced coupling to light

# Quantum dots

## Definition

Semiconductor nanostructures confining carriers in 3D

## Bear in mind...

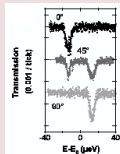
- Ideal QD  $\sim$  perfectly circular disk  $\rightarrow$  only one neutral exciton line
- Real QD  $\rightarrow$  neutral exciton split in orthogonal polarisation peaks via *spin-spin electron-hole exchange interaction*

# Quantum dots

## Definition

Semiconductor nanostructures confining carriers in 3D

Neutral exciton split



## Why put together PhC and QDs?

**Solid-state cavity QED!**



# Model

## Parameters and assumptions

- Defect acting as a cavity:

$$\omega_{cav}$$

$$\gamma_{cav} \sim 100\mu eV \longrightarrow \tau_{cav} \equiv \frac{1}{\gamma_{cav}} \sim 1ps$$

$$\text{quality factor } Q \equiv \frac{\omega_{cav}}{\gamma_{cav}}$$

mode volume  $V$

- QD as point-like emitter, placed at the antinode of a PhC defect cavity in-plane electric field mode  $E$ :

$$\omega_{QD}$$

$$\gamma_{QD} \sim 5\mu eV \longrightarrow \tau_{QD} \equiv \frac{1}{\gamma_{QD}} \sim 1ns$$

dipole moment  $d$

- Enhanced interaction light-matter

# Model

## Hamiltonian

- Exciton-photon coupling parameter  $2g$  (*Rabi splitting*):

$$2g = \frac{2|\langle d \cdot E \rangle|}{\hbar}$$

- Eigenfrequencies in resonance ( $\omega_{QD} = \omega_{cav} \equiv \omega_{res}$ ):

$$\Omega_{\pm} = \omega_{res} - \frac{i}{4}(\gamma_{QD} + \gamma_{cav}) \pm \sqrt{g^2 - \left(\frac{\gamma_{QD} - \gamma_{cav}}{4}\right)^2}$$

# Two regimes

## Weak coupling



$$2g \ll \left| \frac{\gamma_{QD} - \gamma_{cav}}{2} \right| \quad \rightsquigarrow \quad \Omega_{+} = \omega_{res} - i \frac{\gamma_{cav}}{2}$$

$$\Omega_{-} = \omega_{res} - i \left( \frac{\gamma_{QD}}{2} + \frac{2g^2}{\gamma_{cav}} \right)$$

- Irreversible energy transfer
- Control of the spontaneous emission rate: increase (decrease) for QDs in resonance (out of resonance) with the cavity
- $\frac{Q}{V}$

# Two regimes

## Strong coupling

- 

$$2g > \left| \frac{\gamma_{QD} - \gamma_{cav}}{2} \right|$$

→ spontaneous emission spectrum split by

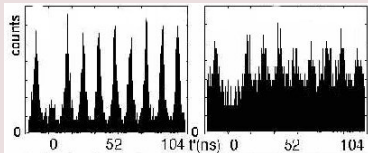
$$2\hbar\sqrt{g^2 - \left(\frac{\gamma_{QD} - \gamma_{cav}}{4}\right)^2}$$

→ average linewidth  $\frac{(\gamma_{QD} + \gamma_{cav})}{2}$

- Coherent energy transfer
- $\frac{Q}{\sqrt{V}}$

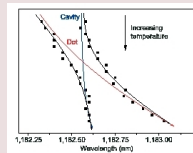
# Two regimes

## Weak coupling



Single photon source

## Strong coupling



Anti-crossing

# Applications

Generally speaking...

Linear optics Qcomp, Qrepeater, Qmemory, QDlaser...

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Linear optics Qcomp, Qrepeater, Qmemory, QDlaser...

## In particular...

- Photon storage in a single exciton
- State storage in a single photon (what about state transfer?)
- Interface among different kinds of qubits

# Applications

## Generally speaking...

Linear optics Qcomp, Qrepeater, Qmemory, QDlaser...

## In particular...

- Photon storage in a single exciton
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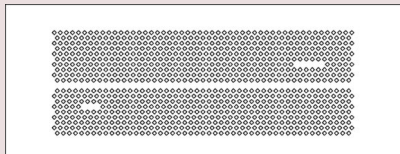
static qubit (QD)  $\longleftrightarrow$  flying qubit (photon)  $\longleftrightarrow$  static qubit (QD)



# The add-drop filter

static qubit (QD)  $\longleftrightarrow$  flying qubit (photon)  $\longleftrightarrow$  static qubit (QD)

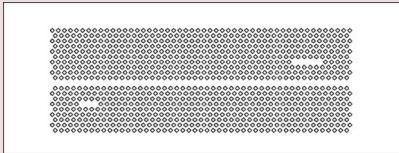
## Proposed structure



Defect cavities (L3, L5) with  
embedded dots connected through a  
defect waveguide

# Working principle

## Proposed structure



Defect cavities (L3, L5) with embedded dots connected through a defect waveguide

Excite a QD randomly placed at the input cavity to the point it emits an in-plane photon (*centered or not around the cavity resonance!*)

↓  
photon transfer via waveguide

↓  
at its proximity, the output cavity traps the photon

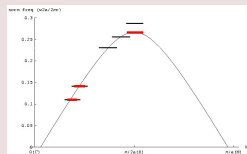
↓  
one out-of-plane photon is emitted to free space (and analysed)

# Coupled mode theory (forget about the QDs for a while!)

Interaction waveguide/cavity  
via electromagnetic field

- Defect cavity can act as transmitter in-plane  $\rightarrow$  vertical direction (*even with mismatch waveguide mode/cavity resonance!*)
- Waveguide: discrete translational symmetry + important dispersion effects (*Not regular treatment!*)  
 $\rightarrow$  toy model

Toy model dispersion relation for (arbitrary) photonic waveguide

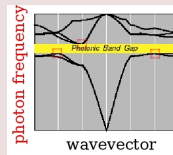


# Coupled mode theory (forget about the QDs for a while!)

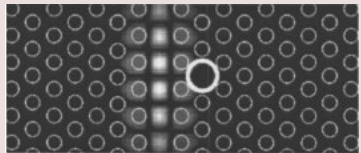
## Non linear dispersion regime

- Edges of the band: group velocity  $\equiv \frac{\partial \omega}{\partial \mathbf{k}} \rightarrow 0$   
 $\rightarrow$  standing waves that spread into the lattice
- $\omega_{res}$  close to waveguide band edge mode  $\rightarrow$  light scattered with  $\omega_{edge}$

## Band level-off at the edges



## Simulated in-plane $E$ for waveguide band edge mode

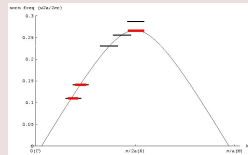


# Coupled mode theory (forget about the QDs for a while!)

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## Toy model dispersion relation for (arbitrary) photonic waveguide

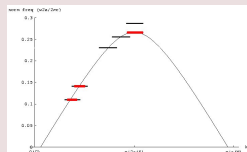


# Coupled mode theory (forget about the QDs for a while!)

## Linear dispersion regime

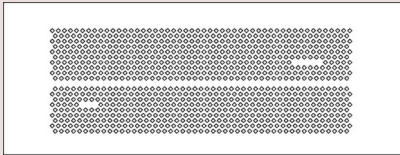
- Cavity resonance  $\omega_{res}$  in the linear dispersion of the waveguide  $\rightarrow$  light scattered with  $\omega_{res}$  (by resonant tunneling)

## Toy model dispersion relation for (arbitrary) photonic waveguide



# Working principle in detail (QDs are back)

## Proposed structure

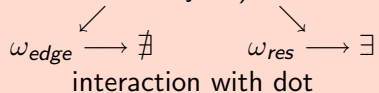


Defect cavities (L3, L5) with embedded dots connected through a defect waveguide

## Suppose that...

- Output cavity  $\omega_{res}$  sits at non linear dispersion region of waveguide, but  $\omega_{res} < \omega_{edge}$

(Suppose) QD in input cavity emits an in-plane  $\omega_{edge}$  photon  
 ↓  
 photon transfer via waveguide  
 ↓  
 at its proximity, the output cavity traps the photon  
 ↓  
 one out-of-plane photon is emitted to free space (and analysed)



# Photonic lattice and slab

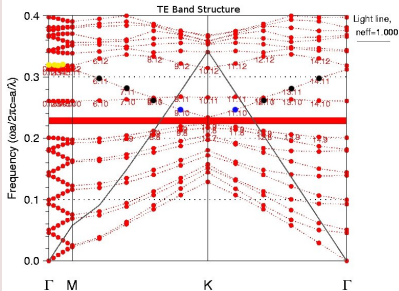
## Desired properties

- Study confinement of in-plane  $E \rightarrow$  broad bandgap for in-plane  $E$  ( $TE$  modes)  $\rightarrow$  hexagonal lattice with lattice constant  $0.240\mu m$
- Compromise between quantities increasing with radius of air holes: bandgap  $\times$  mode tendency to leak to free space  $\rightarrow$  radius  $0.084\mu m$
- Dots photoemission range:  $\sim 900 - 1100nm \rightarrow$  photonic bandgap falling within it  $\rightarrow$  ( $2D$  plane wave expansion calculated) bandgap  $[0.710, 1.012]\mu m$
- Height of slab  $\rightarrow$  constrained by available sample  $\rightarrow$  thickness  $0.200\mu m$



# Waveguide

2D plane wave expansion calculated defect waveguide band structure

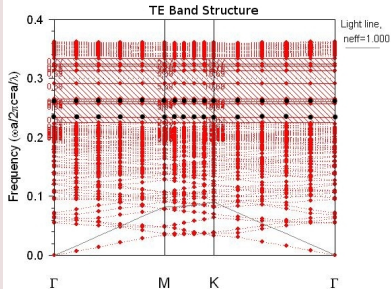


It means that...

- *Not the standard procedure for calculating waveguide supported modes!*
- Marked eigenfrequencies: guided modes
- Estimated coupling edge  $[0.976, 1.026] \mu m$

# (Isolated) defect cavities

2D plane wave expansion simulated band structure for crystal with L3 defect cavity

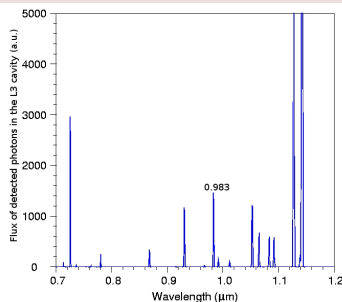


It means that...

- Simulated fundamental resonant wavelengths:  
 L3  $\rightarrow$   $1.026\mu m$   
 L5  $\rightarrow$   $1.030\mu m$
- Monomode cavity for range of order  $\sim 0.060\mu m$   
 $\rightarrow$  good optical selectivity of trapped modes

# (Isolated) defect cavities

3D FDTD simulated resonant spectrum for crystal with L3 defect cavity

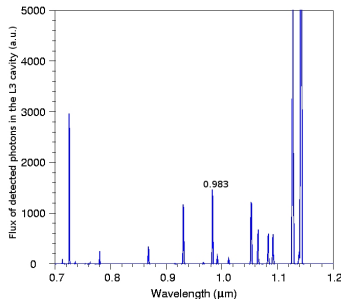


It means that...

- Spectrum computed at the center of the slab
- Simulated fundamental resonant wavelengths:  
 $L3 \rightarrow 0.983\mu m$   
 $L5 \rightarrow 1.010\mu m$
- Simulated fundamental resonant wavelengths  
 $2D > 3D$

# (Isolated) defect cavities

3D FDTD simulated resonant spectrum for crystal with L3 defect cavity



It means that...

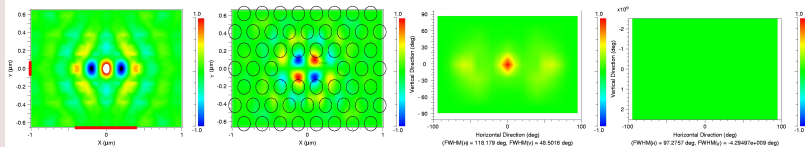
- Quality factors for the fundamental modes:

L3  $\longrightarrow$  820

L5  $\longrightarrow$  410

## (Isolated) Defect cavities

## 3D FDTD simulated fundamental mode profiles for L3 cavity

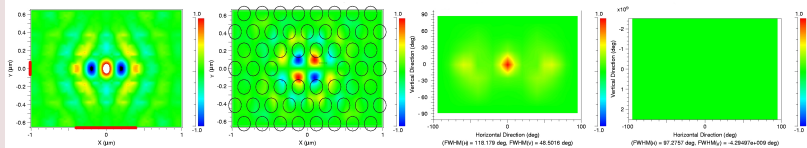
 $E_y$  near-field $E_x$  near-field $E_y$  far-field $E_x$  far-field

It means that...

- Near-field  $\leftarrow FT \rightarrow$  far-field
- By  $FT$  separately  $E_x$  and  $E_y \rightarrow$  polarization and radiation angle information of scattered light

## (Isolated) Defect cavities

## 3D FDTD simulated fundamental mode profiles for L3 cavity

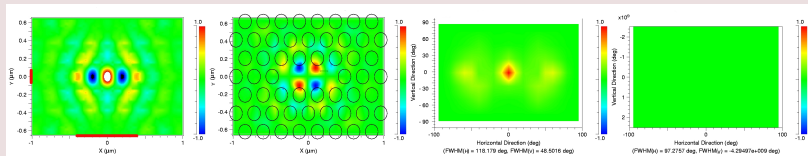
 $E_y$  near-field $E_x$  near-field $E_y$  far-field $E_x$  far-field

It means that...

- Scattered light from the cavity is vertically emitted *and*  $y$  polarised

## (Isolated) Defect cavities

## 3D FDTD simulated fundamental mode profiles for L3 cavity

 $E_y$  near-field $E_x$  near-field $E_y$  far-field $E_x$  far-field

Real QD exciton has a natural linear polarisation basis  $\longrightarrow$   
maybe cavity could address only the  $y$  polarized exciton

## Come together

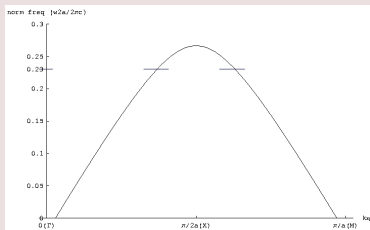
## Simulations methods compared

Defect	2D wl. ( $\mu m$ )	3D wl. ( $\mu m$ )	Discrepancy(%)
hex. latt.	0.719-1.176	0.710-1.012	0.6-7.5
L3	1.026	0.983	2.1
L5	1.030	1.010	1.0
wg.	0.755-0.976	0.985-0.995	13.2-1.0
wg. edge	0.976-1.026	-	-



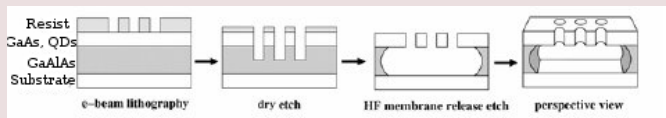
# Come together

## Simulated dispersion relation for modelled photonic waveguide

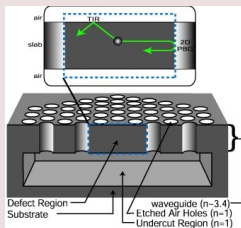


# Microfabrication

## Processing

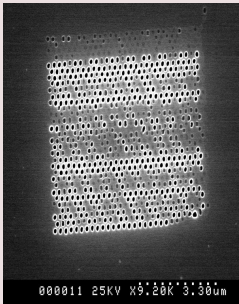


## Importance of slab



# Microfabrication

## Results in the QDs sample

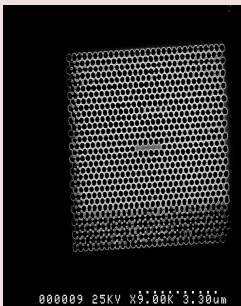


## Limitations of the technique

- Random position of QDs
- Holes not uniformly etched
- Backscattering of electrons during e-beam lithography → changes in hole radii
- Worse optical confinement than if it were a free-standing membrane

# Microfabrication

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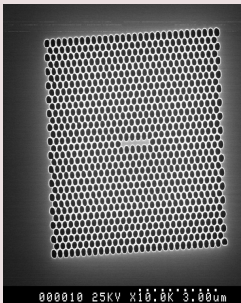


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# Microfabrication

## Results in the QDs sample



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# Conclusion

## In summary

- PhC structures suitable for strong *and* weak couplings to QDs
- Inexpensive and easy (!!!) technique
- Ideal platform for integration → Qnetwork, Qrepeater...
- Scalable

## References

### In order of appearance!

- J. Vuckovic et al.: *APL* **82**, 3696 (2003)
- S. Noda et al.: *Nature* **407**, 608 (2000)
- J. D. Joannopoulos et al.: *Photonic Crystals - molding the flow of light*(Princeton University Press, Princeton, 1995)
- M. Pelton et al.: *Physica E* **17**, 564 (2003)
- Biro et al.: *PRE* **67**, 021907 (2003)
- J. G. Fleming et al.: *Opt. Lett.* **24**, 49 (1999)
- M. Fujita et al.: *Science* **308**, 1296 (2005)

## References

### In order of appearance!

- A. Sugitatsu et al.: *APL* **86**, 171106 (2005)
- E. Yablonovitch et al.: *PRL* **67**, 3880 (1991)
- J. P. Reithmaier et al.: *Nature* **432**, 197 (2004)
- A. Hogele et al.: *PRL* **93**, 217401 (2004)
- D. Englund et al.: *PRL* **95**, 013904 (2005)
- T. Yoshie et al.: *Nature* **432**, 200 (2004)



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