



# Bees and the Traveling Salesman Problem

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Andy Reynolds (Roth. Research, UK)

N

A



B

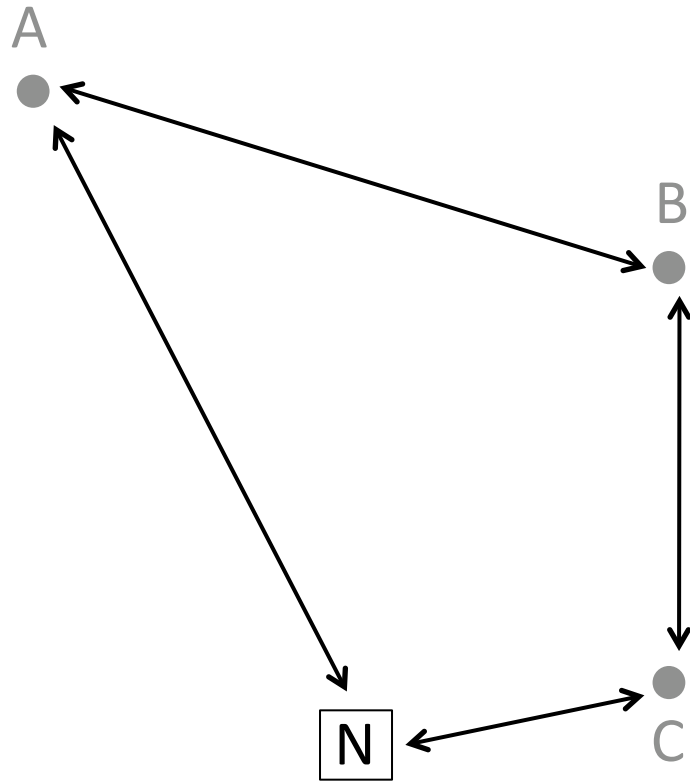


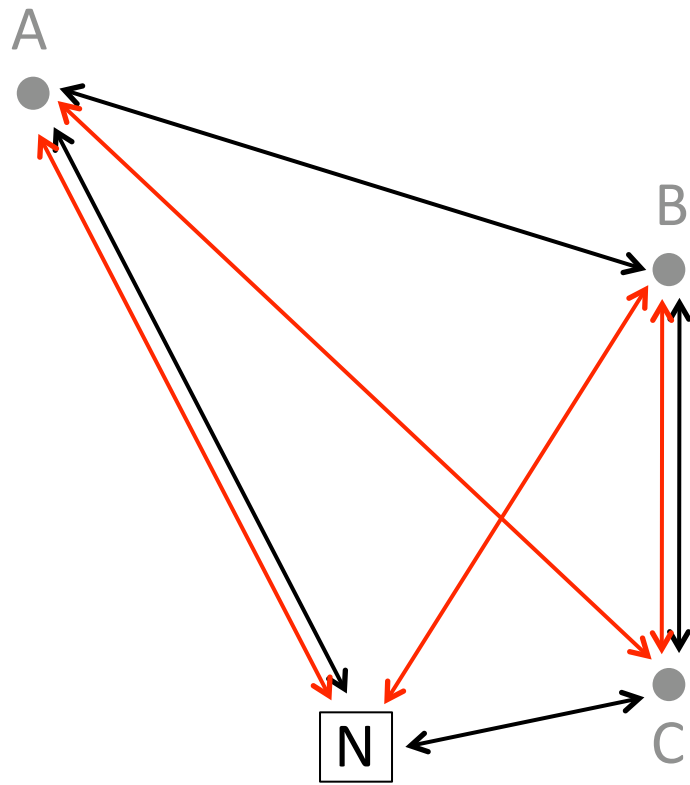
N



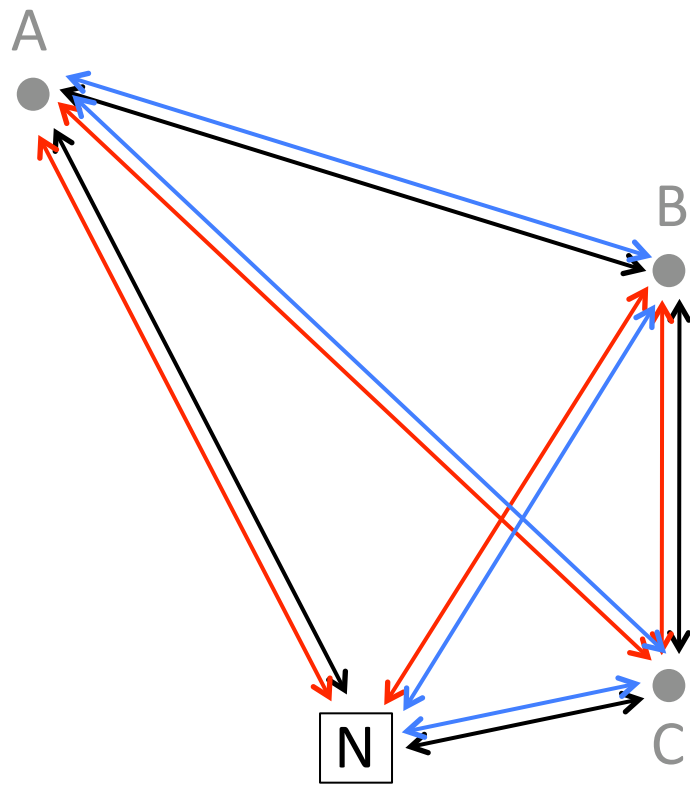
C

ABC  
CBA

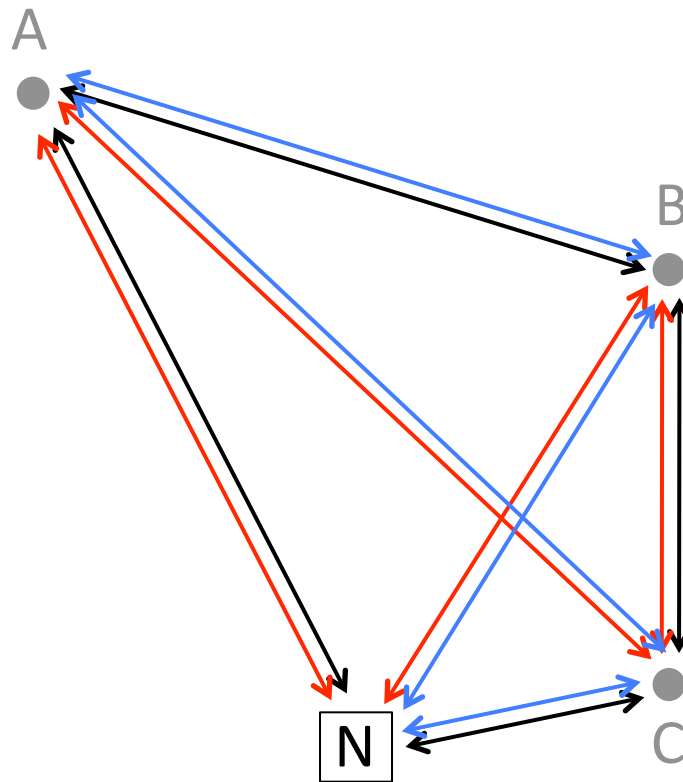




ABC  
CBA  
BCA  
ACB



- ABC
- CBA
- BCA
- ACB
- CAB
- BAC



ABC  
CBA  
BCA  
ACB  
CAB  
BAC

3 locations  
 $3 \times 2 \times 1 = 6$  routes

A



B



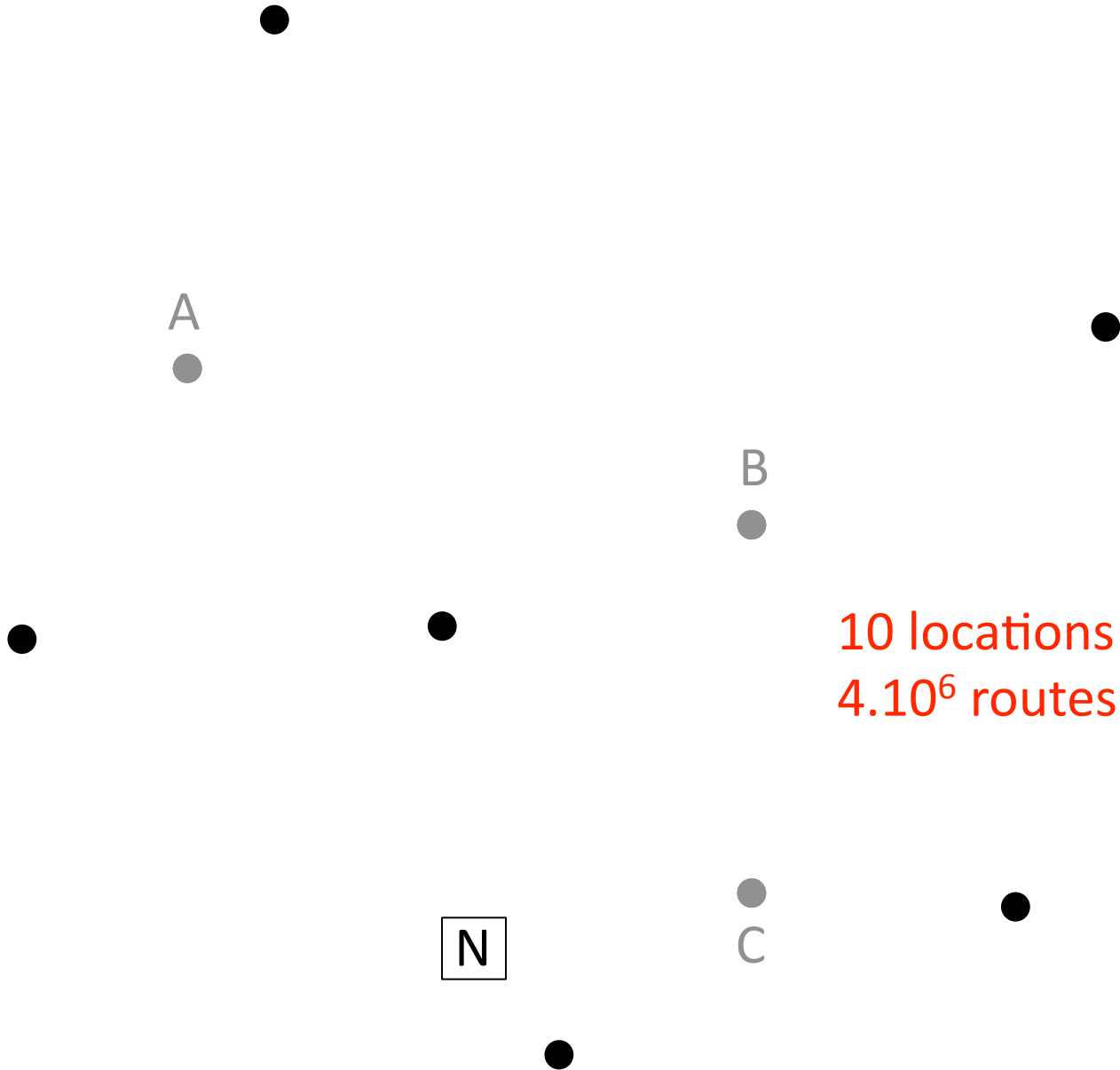
C



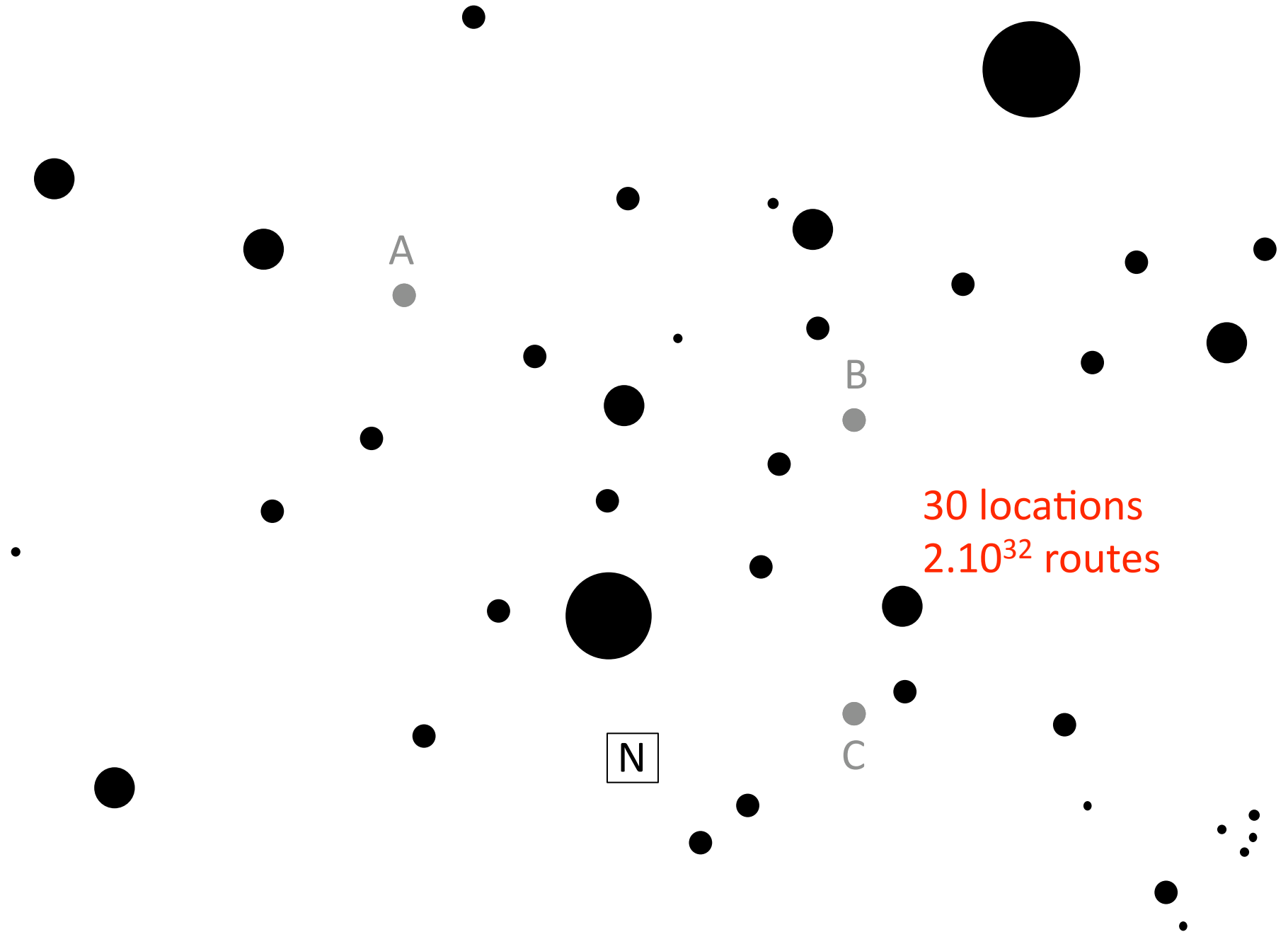
N

5 locations  
120 routes





10 locations  
4.10<sup>6</sup> routes



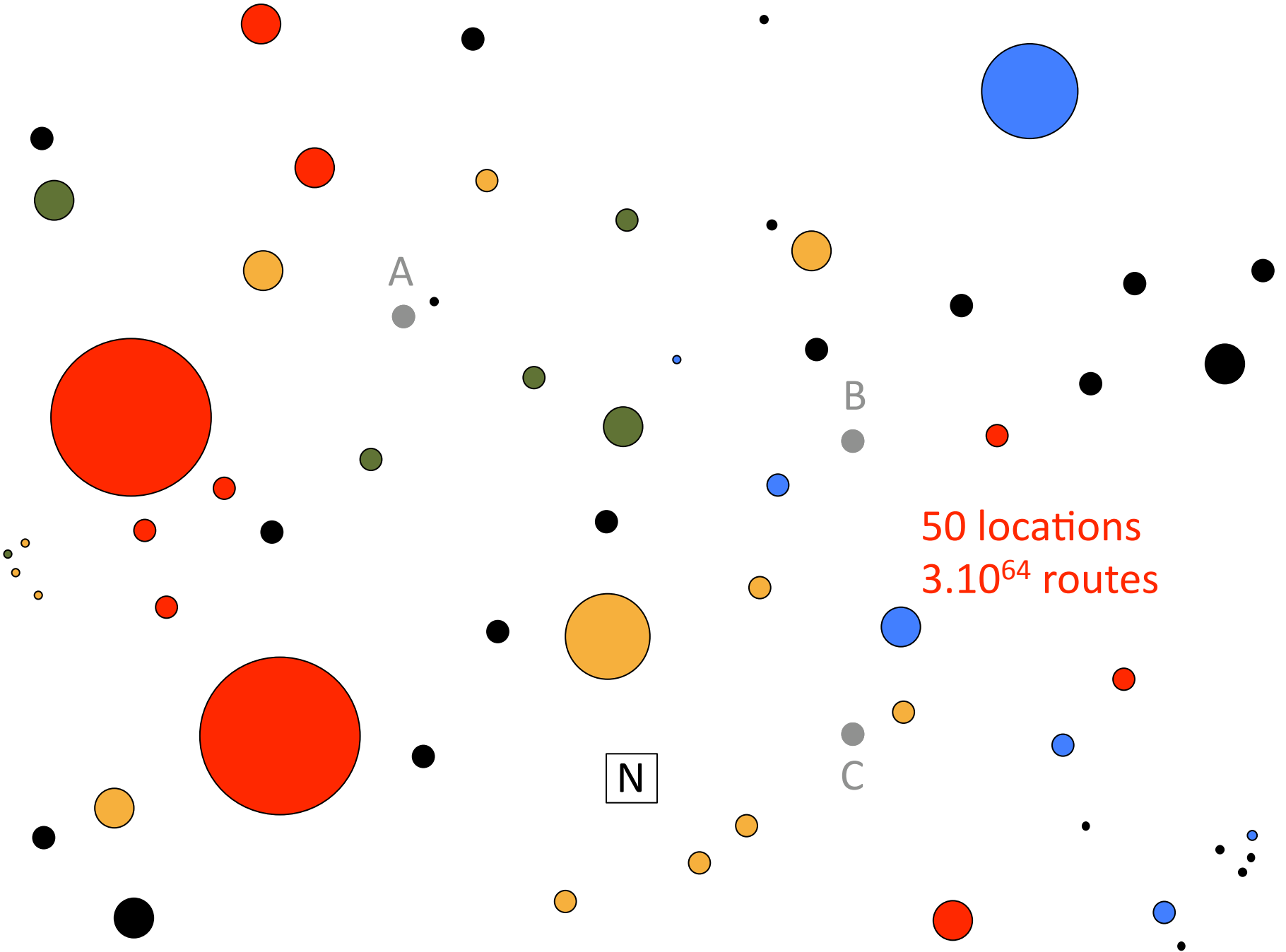
A

B

C

N

30 locations  
 $2 \cdot 10^{32}$  routes

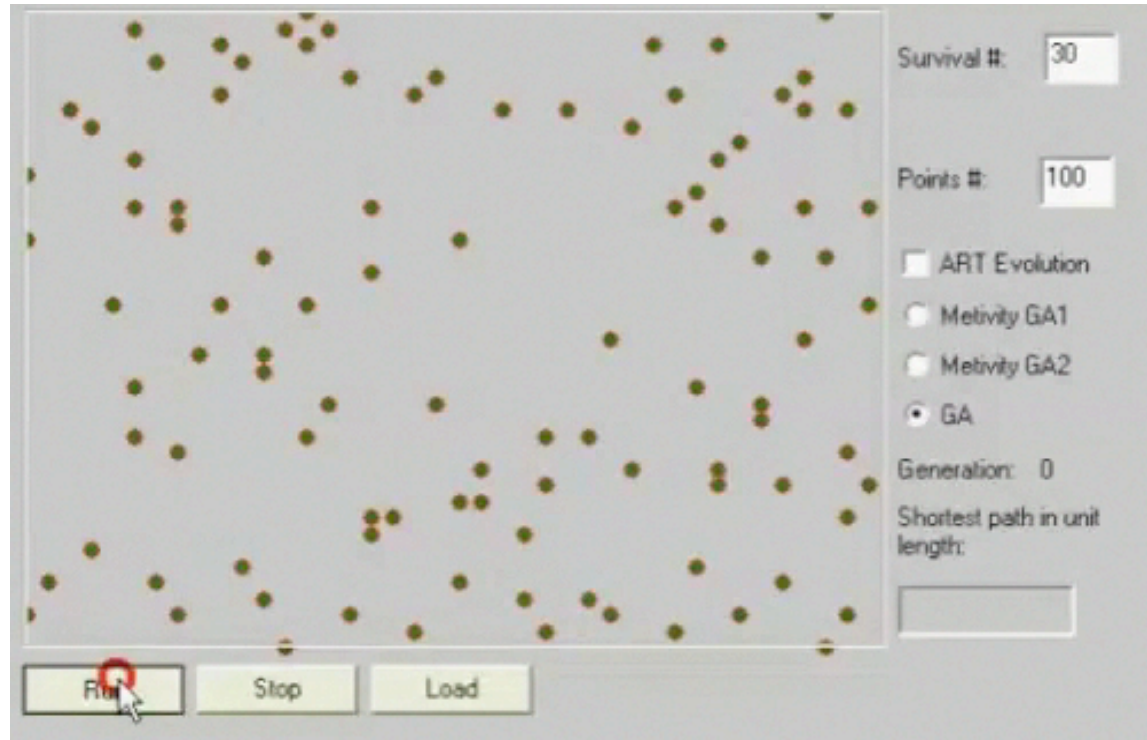


# The Travelling Salesman Problem

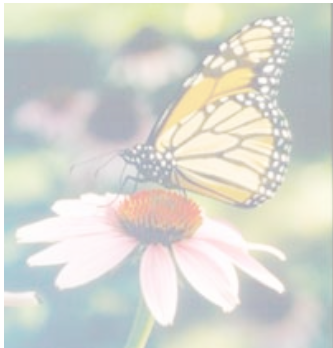
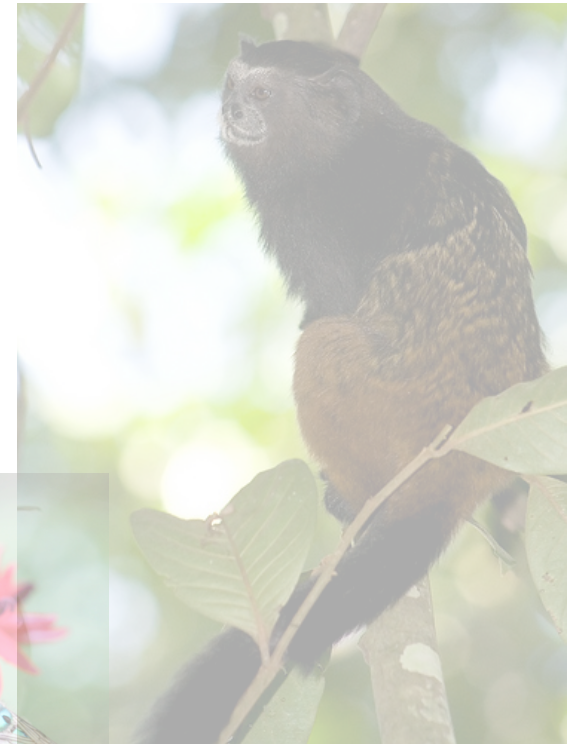
*“Finding the shortest path that passes through a set of locations once and return to the origin”*



RW Hamilton (1805-1855)



# The case of pollinators



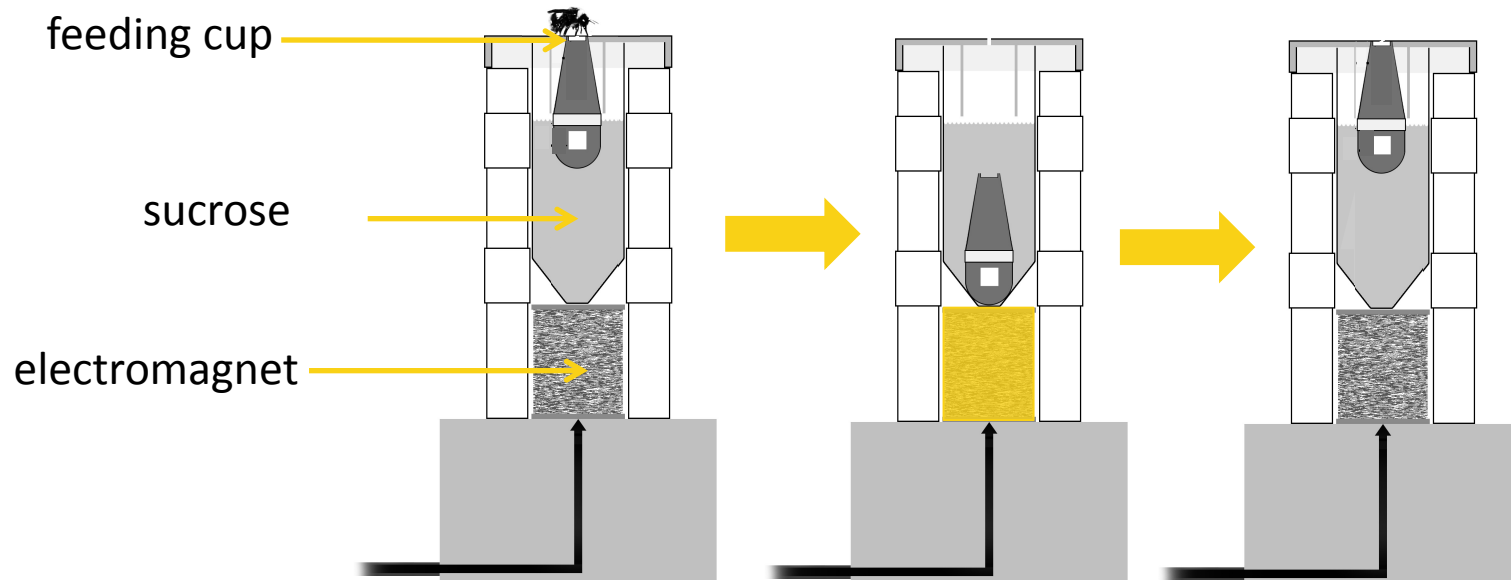
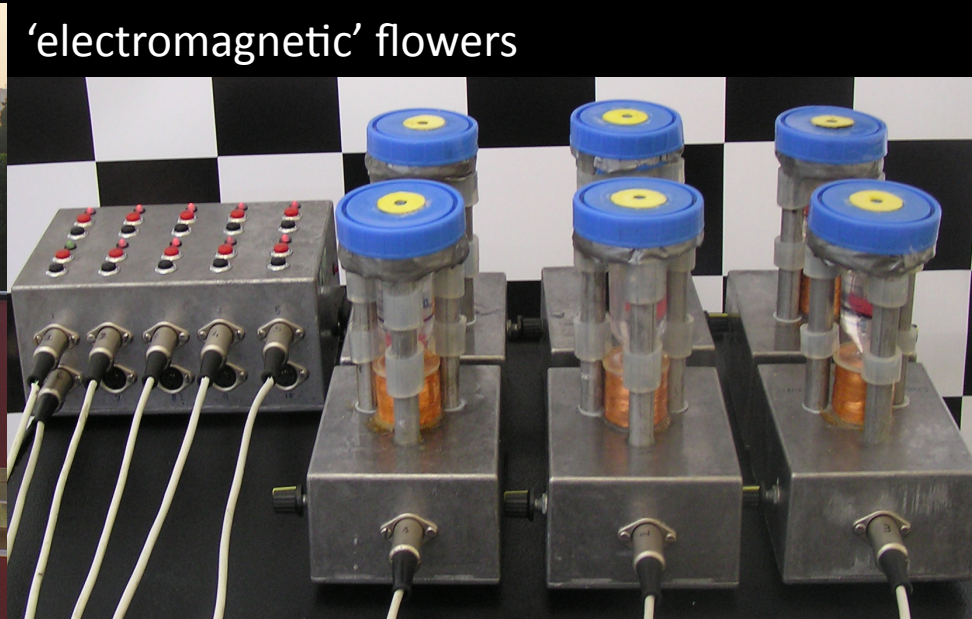
# Outline



1. Forming routes

- one forager

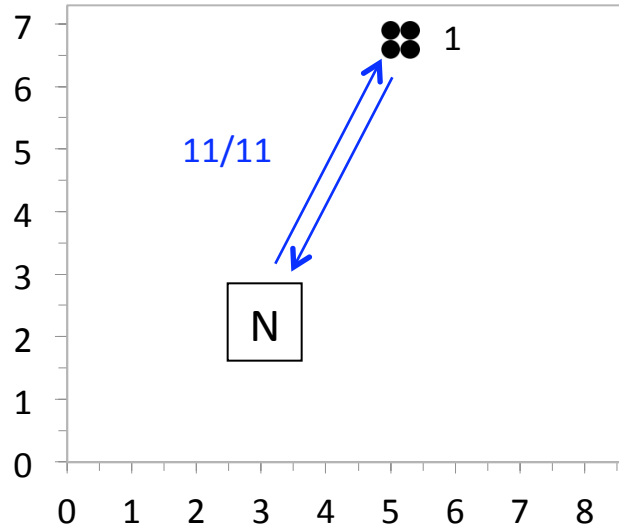
# Foraging in the lab



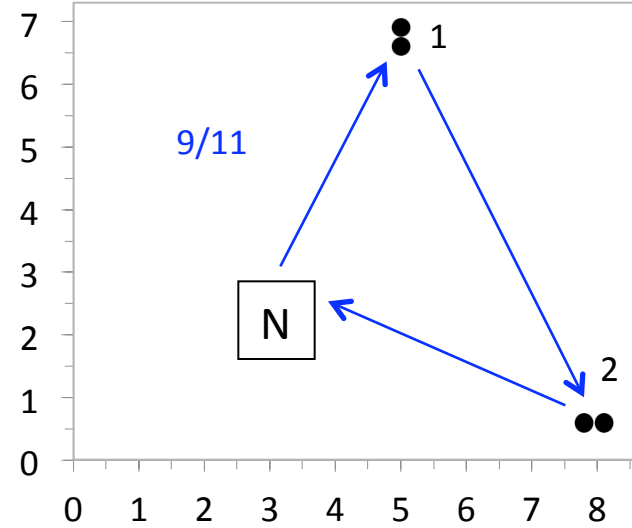
# Flower discovery order

20 bouts/config  
N = 11 bees

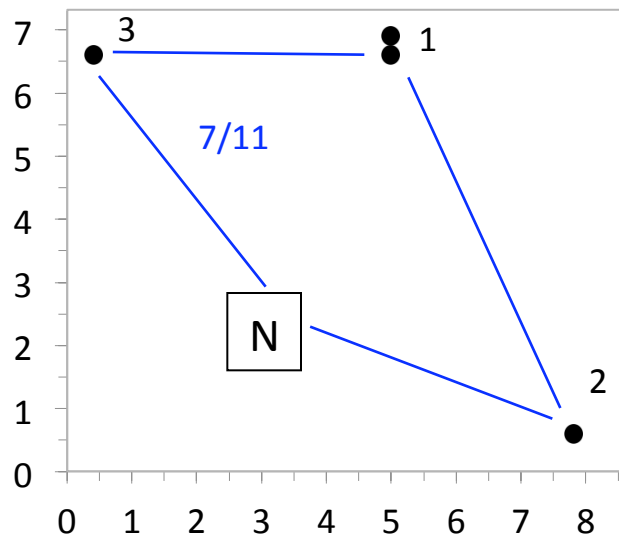
Configuration 1



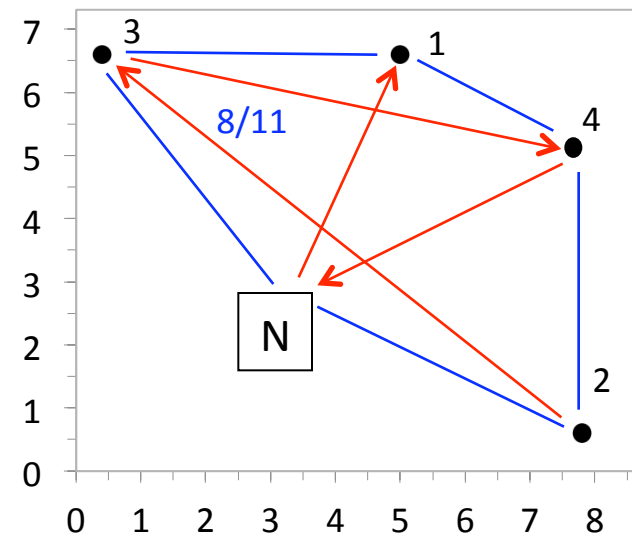
Configuration 2



Configuration 3



Configuration 4

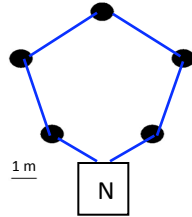


Bees develop flexible and near-optimal 'trapplines' with experience.

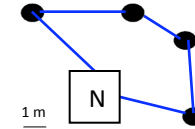


# Overall travel distances

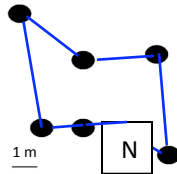
Lihoreau et al. (2011) Funct Ecol



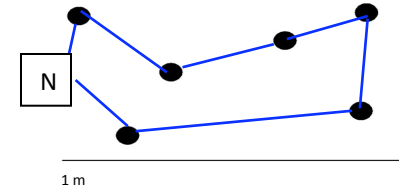
Lihoreau et al. (2010) Am Nat



Lihoreau et al. (2012) Biol Lett

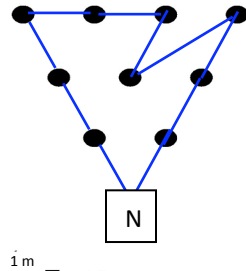


Saleh and Chittka (2007) Oecologia

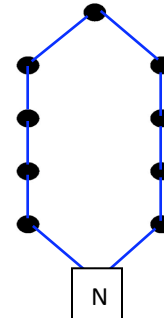


Bees develop flexible and near-optimal 'traplines' with experience.

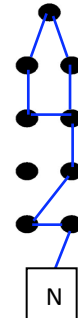
Ohashi et al. (2007) Behav Ecol 2007



Ohashi et al. (2010) BES



Ohashi et al. (2012) Behav Ecol



# Heterogenous rewards

40 bouts/phase

N = 5 bees

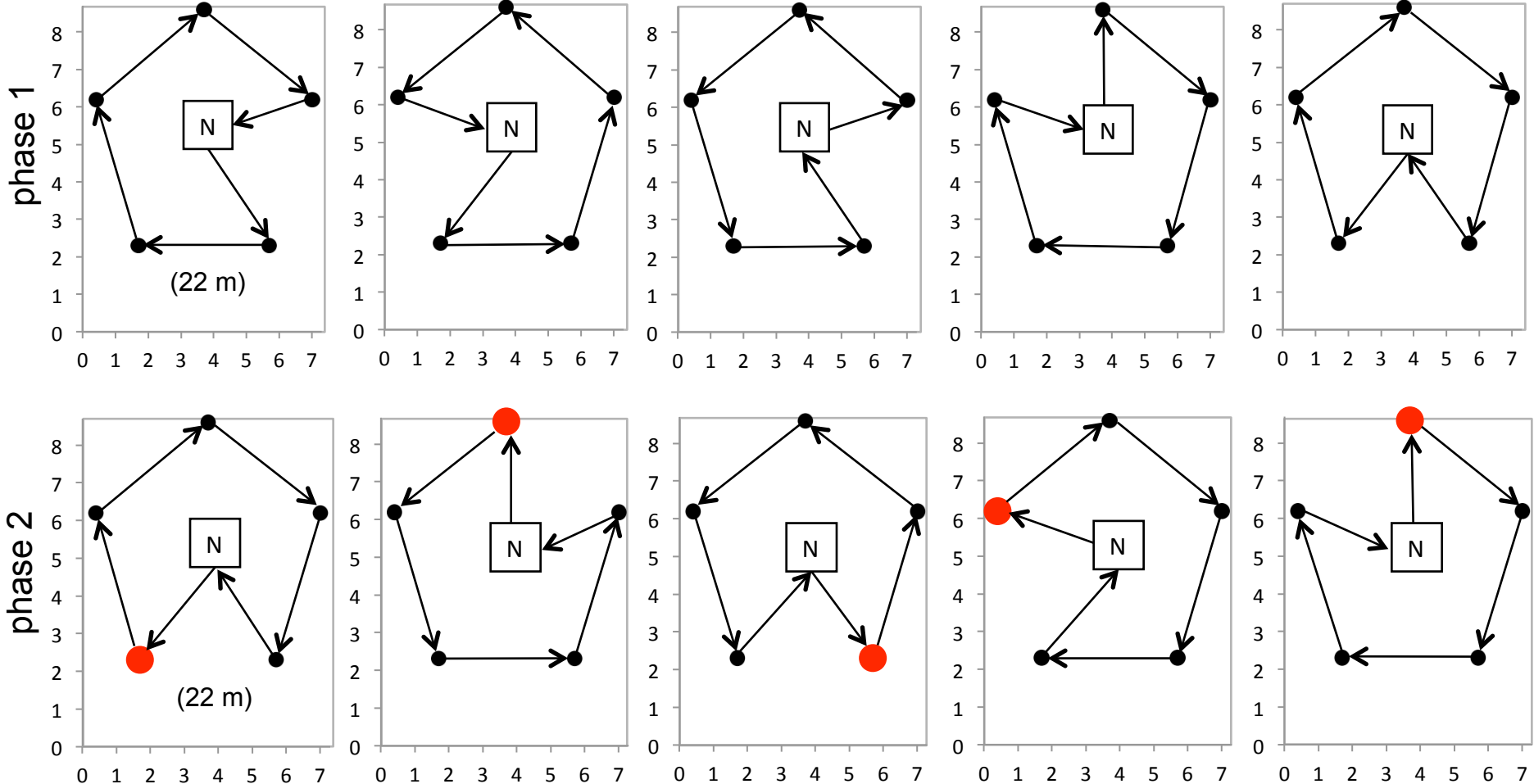
individ. 1

individ. 2

individ. 3

individ. 4

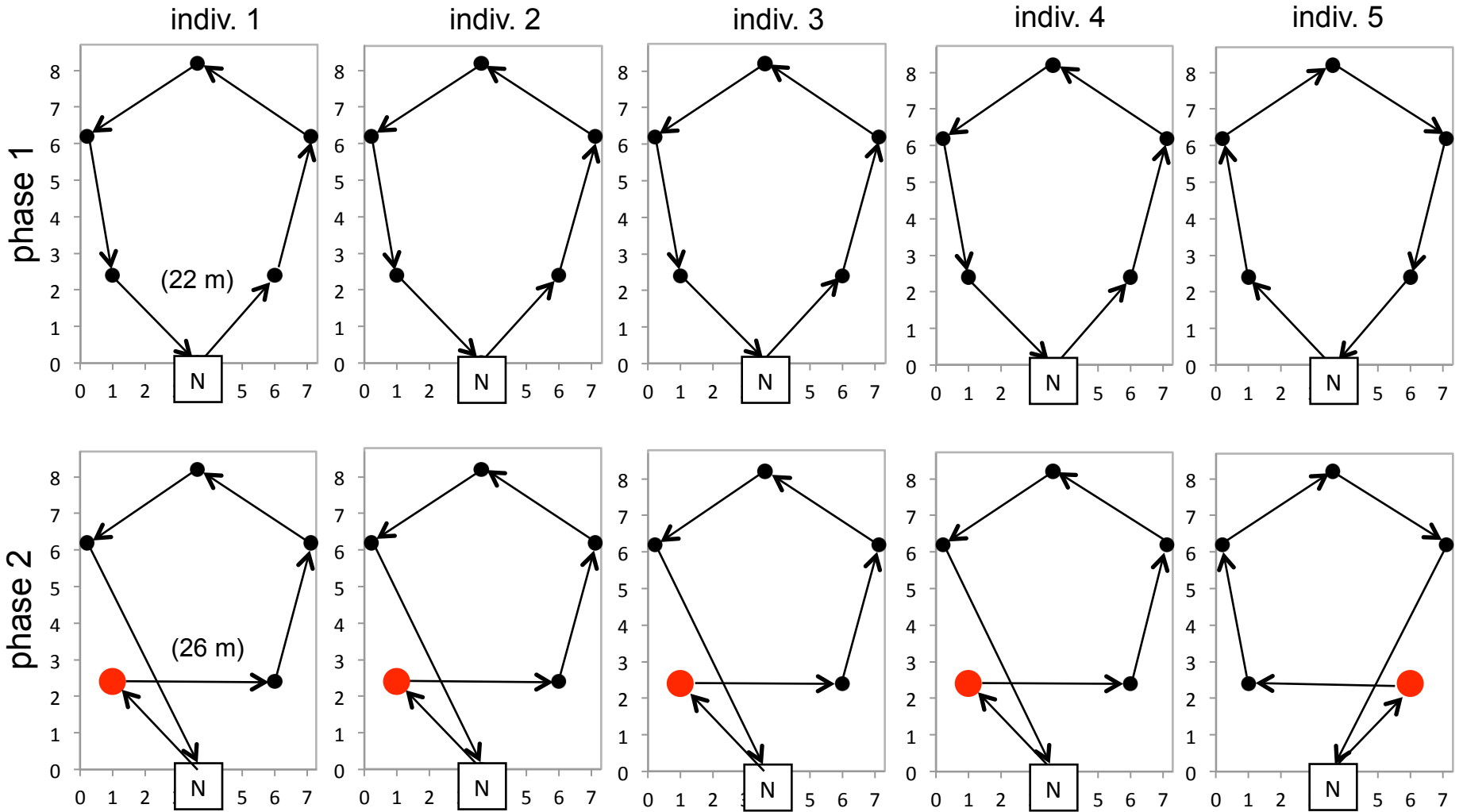
individ. 5



# Heterogenous rewards

40 bouts/phase

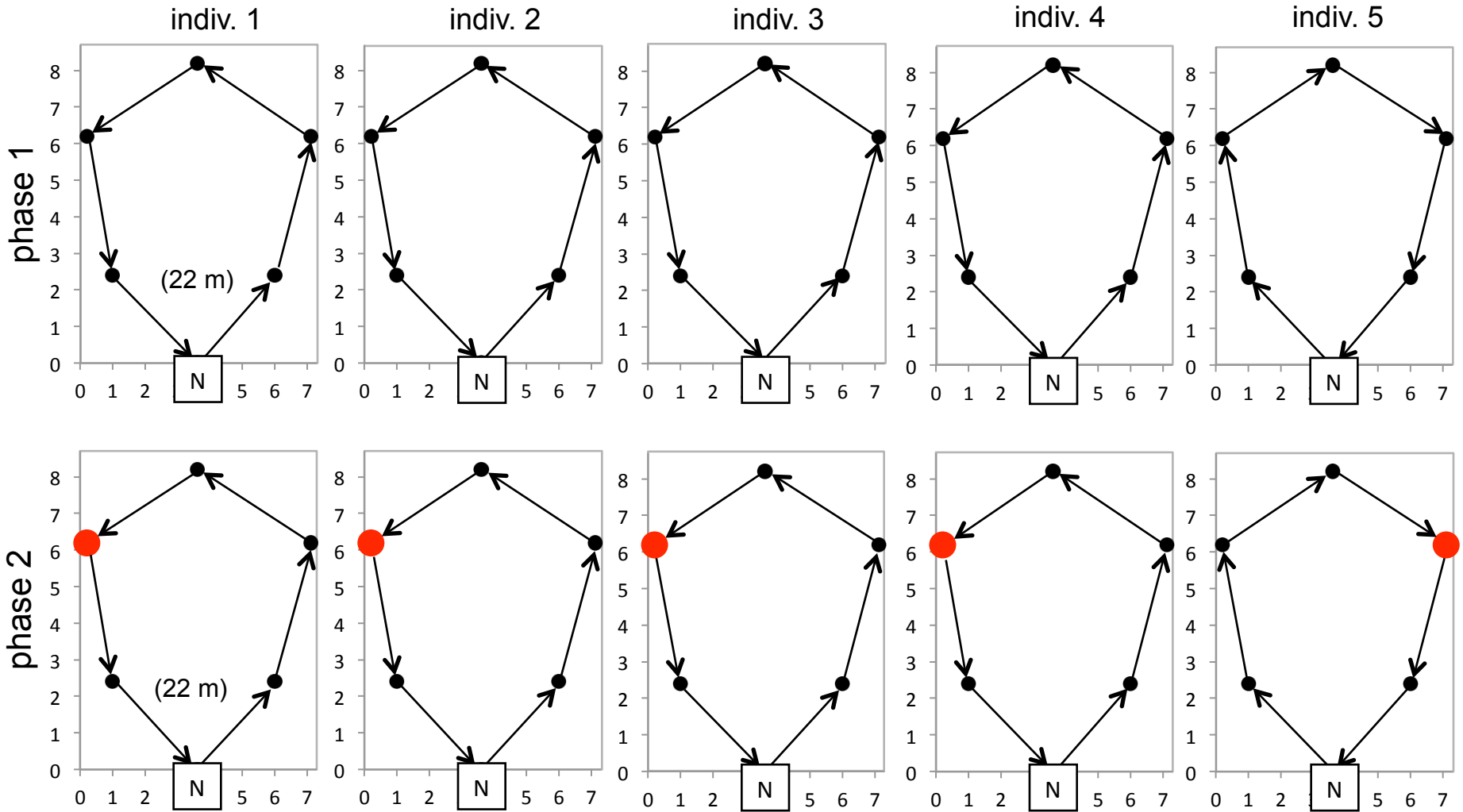
N = 5 bees



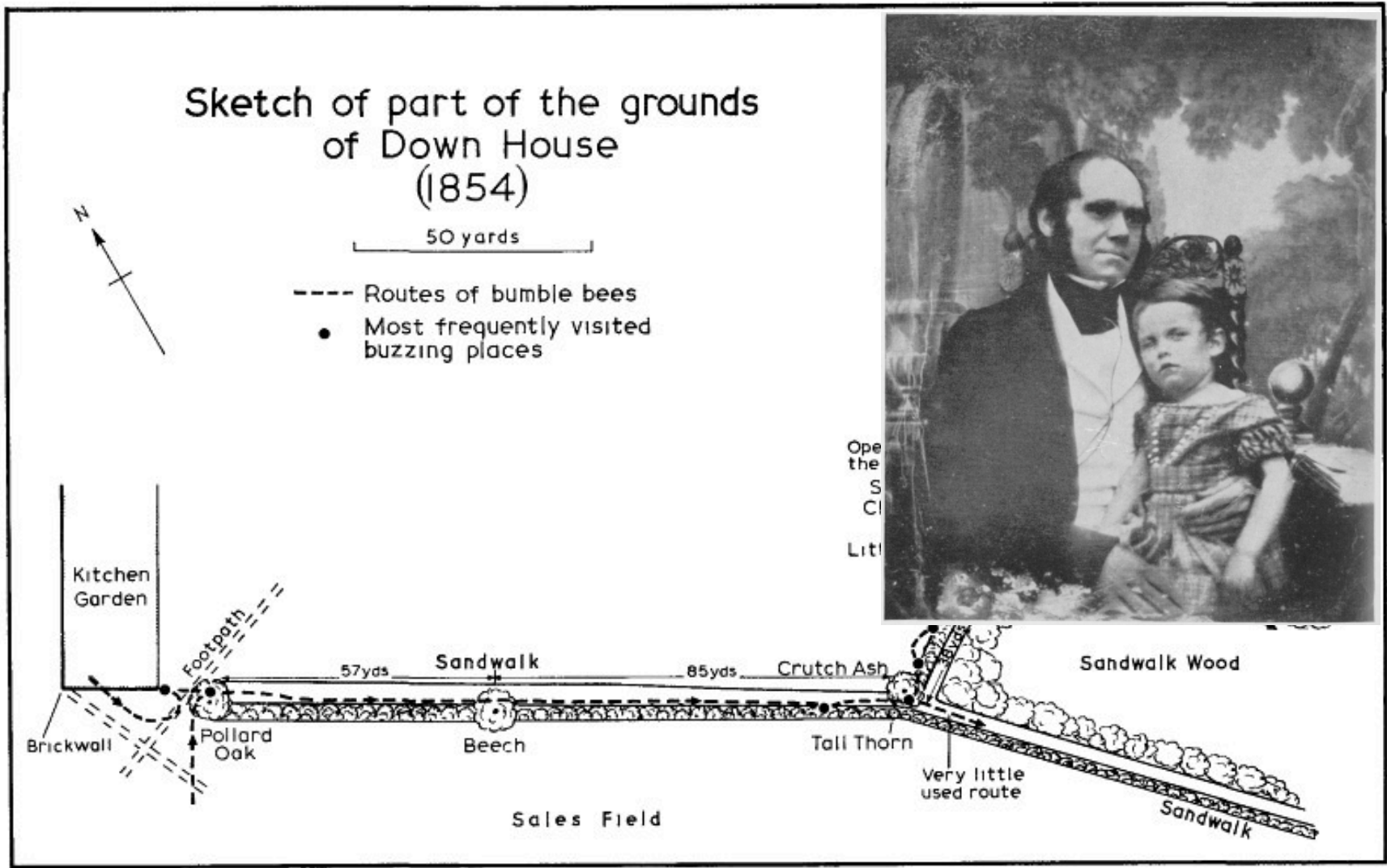
# Heterogenous rewards

40 bouts/phase  
N = 5 bees

Bees trade-off optimisation of travel distances and reward intake rates.



# Large spatial scales



Darwin (1861) Bul Br Mus Nat Hist

# Large spatial scales



Harmonic radar



Bee with a transponder

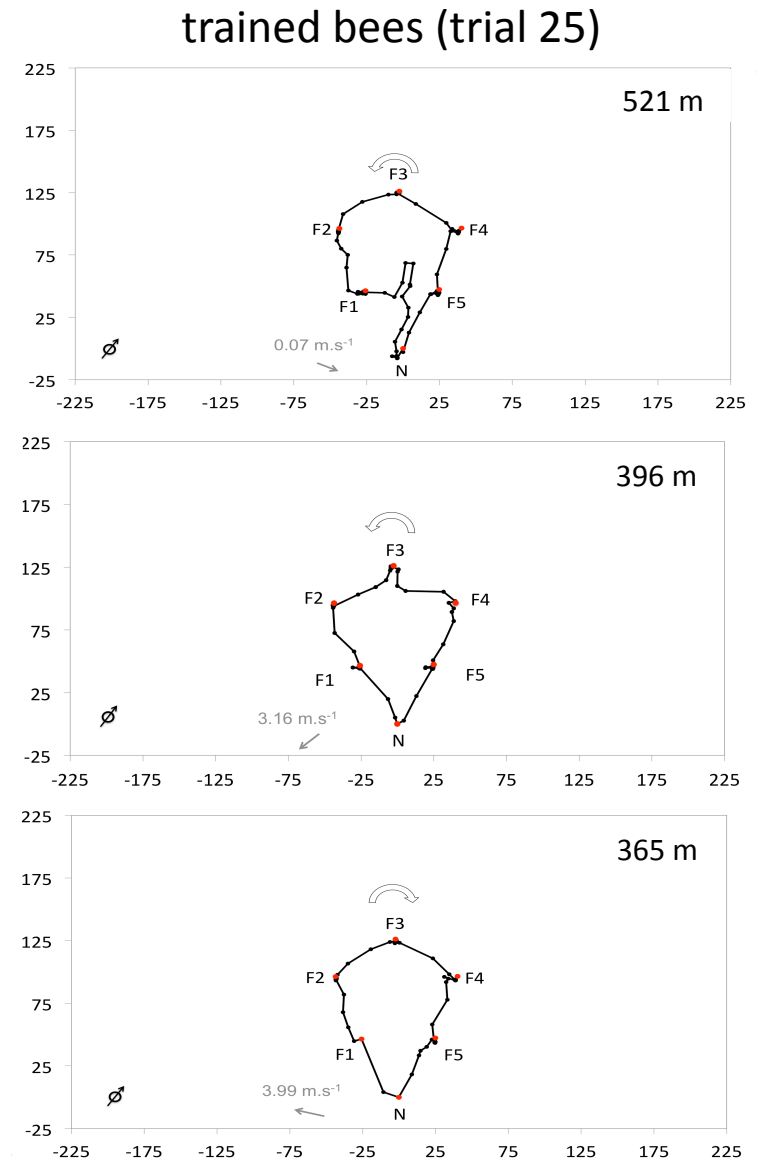
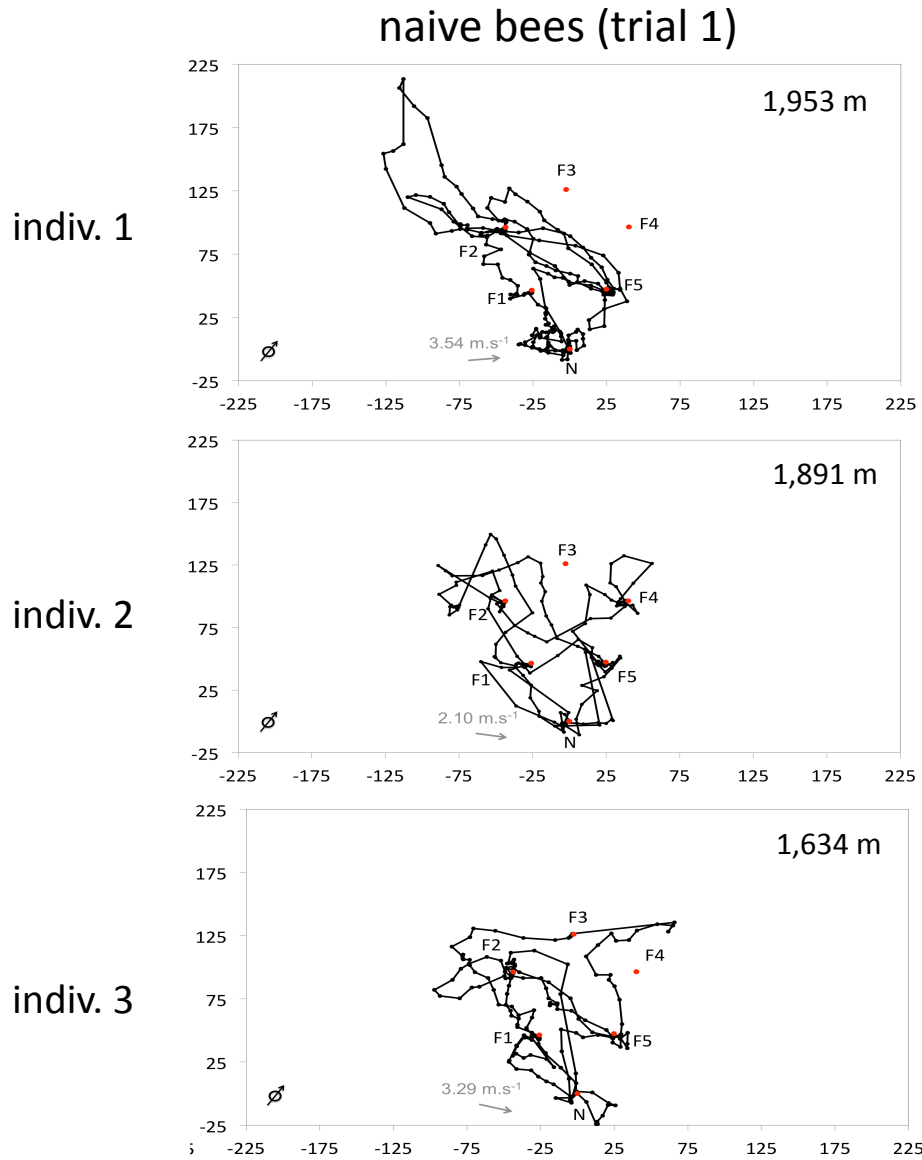


Motion detection 'flowers'

# Large spatial scales



# Large spatial scales

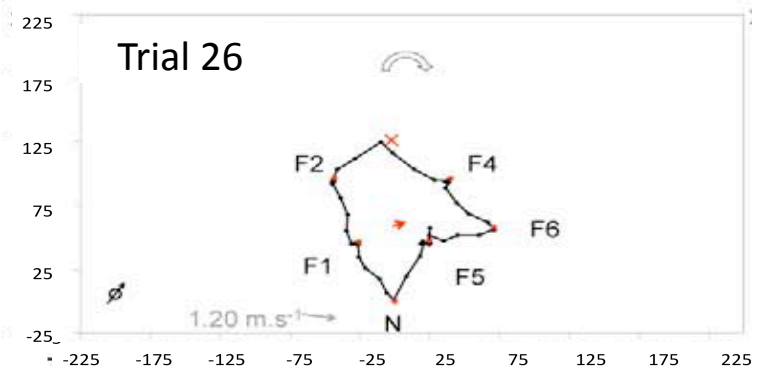
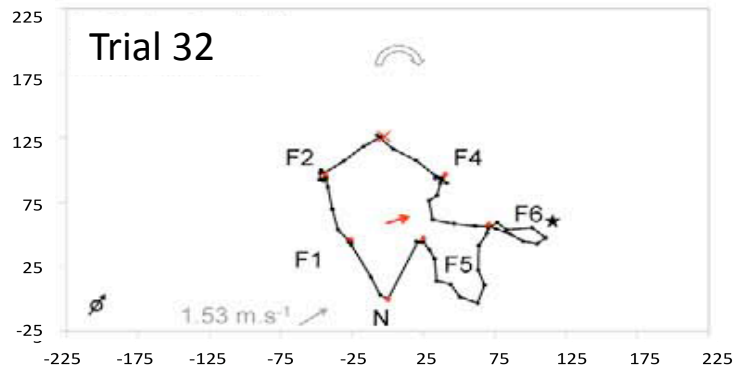
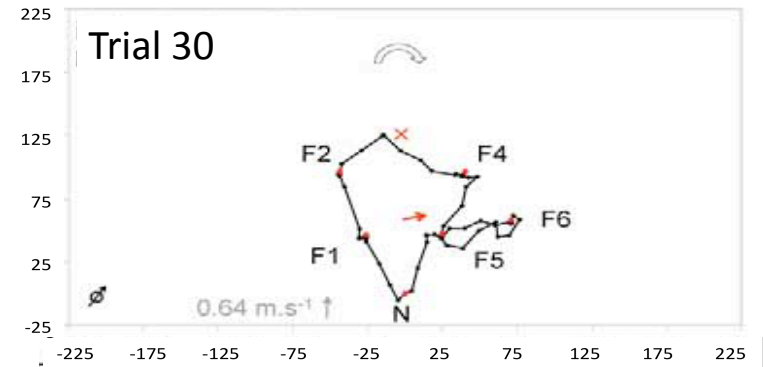
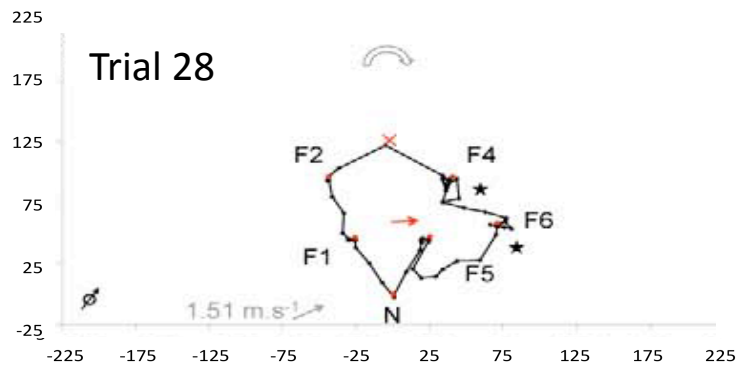
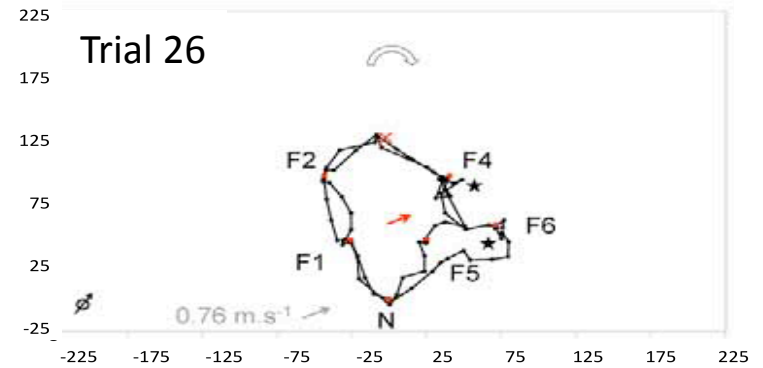
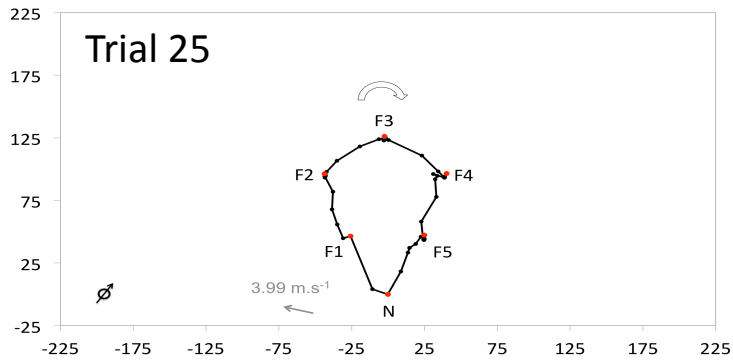




# Large spatial scales

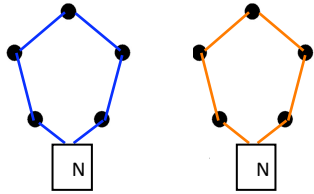


# Large spatial scales

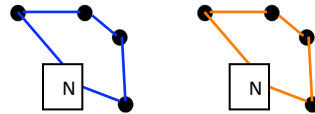


# The traplining model

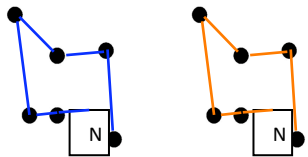
Lihoreau et al. (2011) *Funct Ecol*  
Lihoreau et al. (2012) *PLoS Biol*



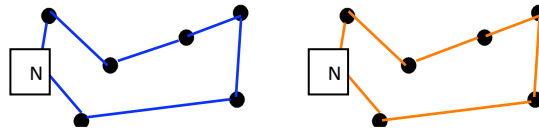
Lihoreau et al. (2010) *Am Nat*



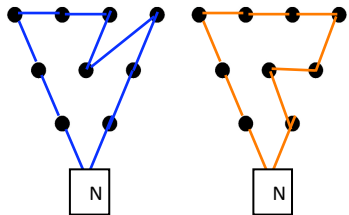
Lihoreau et al. (2012) *Biol Lett*



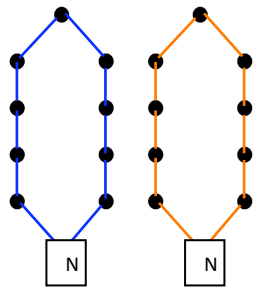
Saleh and Chittka (2007) *Oecologia*



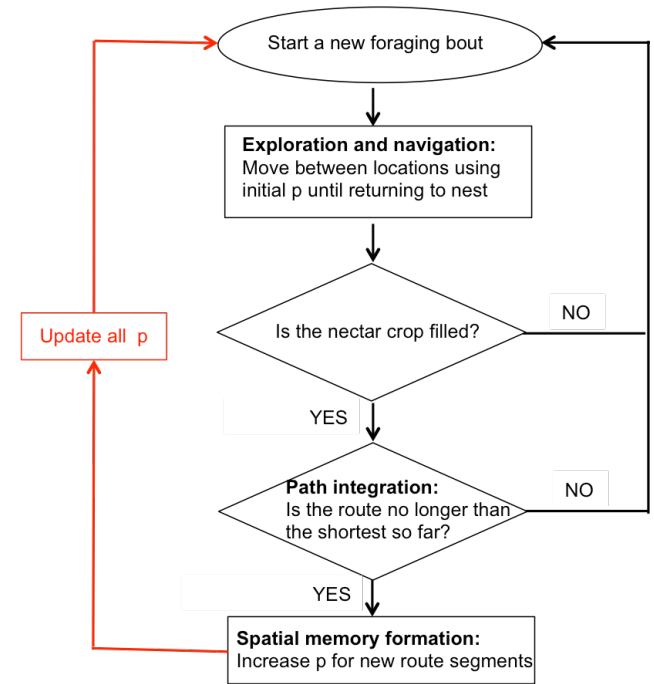
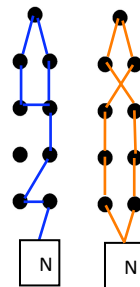
Ohashi et al. (2007) *Behav Ecol*



Ohashi et al. (2010) *BES*



Ohashi et al. (2012) *Behav Ecol*



Accurate replication of trapline formation by bees across spatial scales and flower arrangements.

# Outline

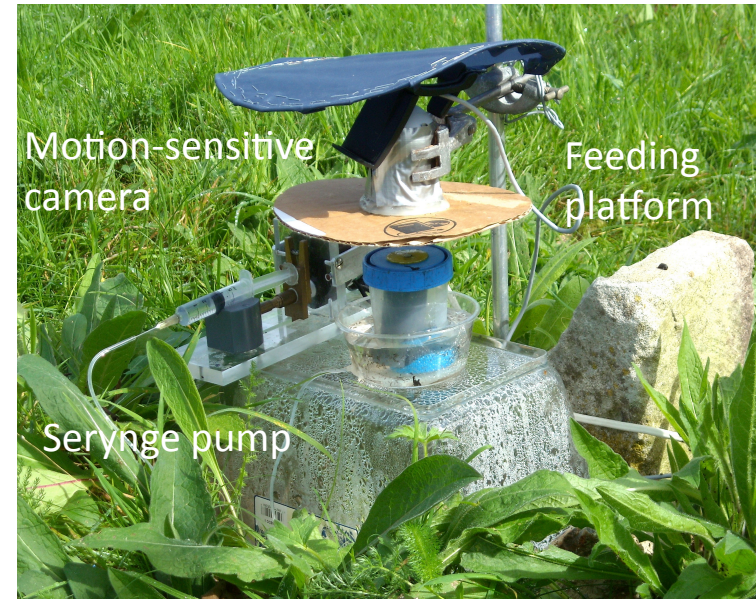


## 1. Forming routes

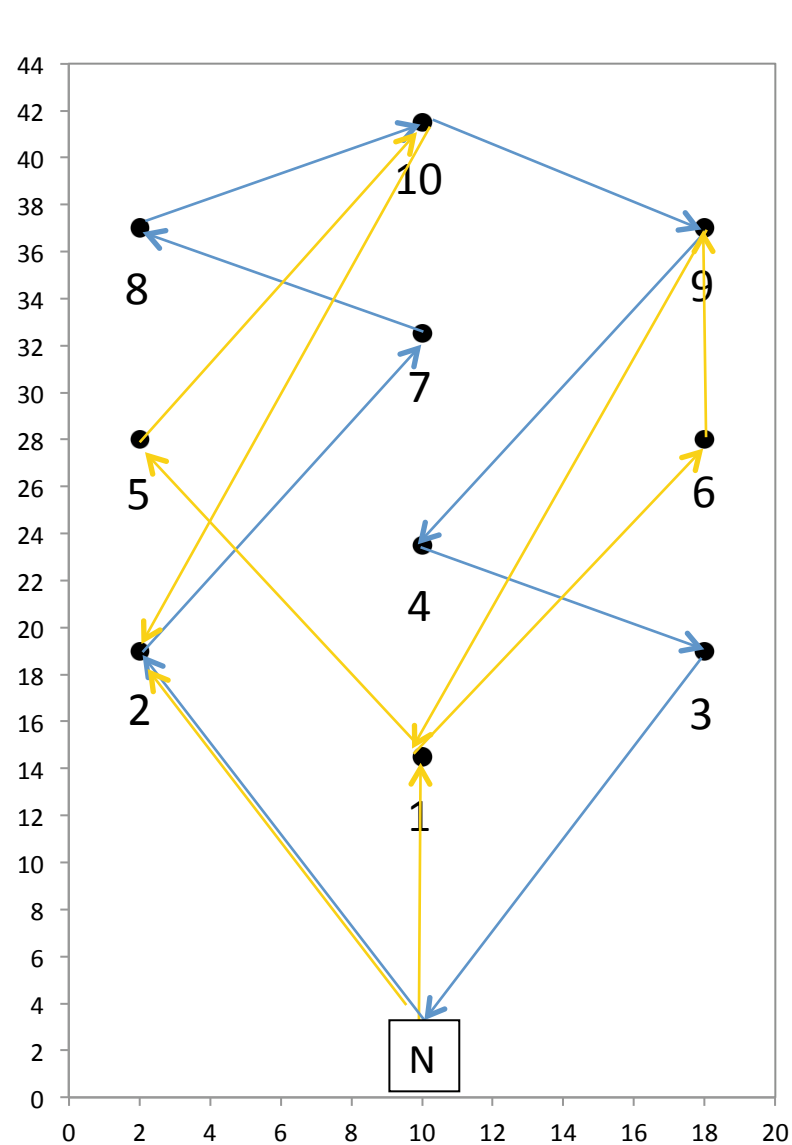
- one forager
- multiple foragers

# Multiple interacting bees

outdoor net cage

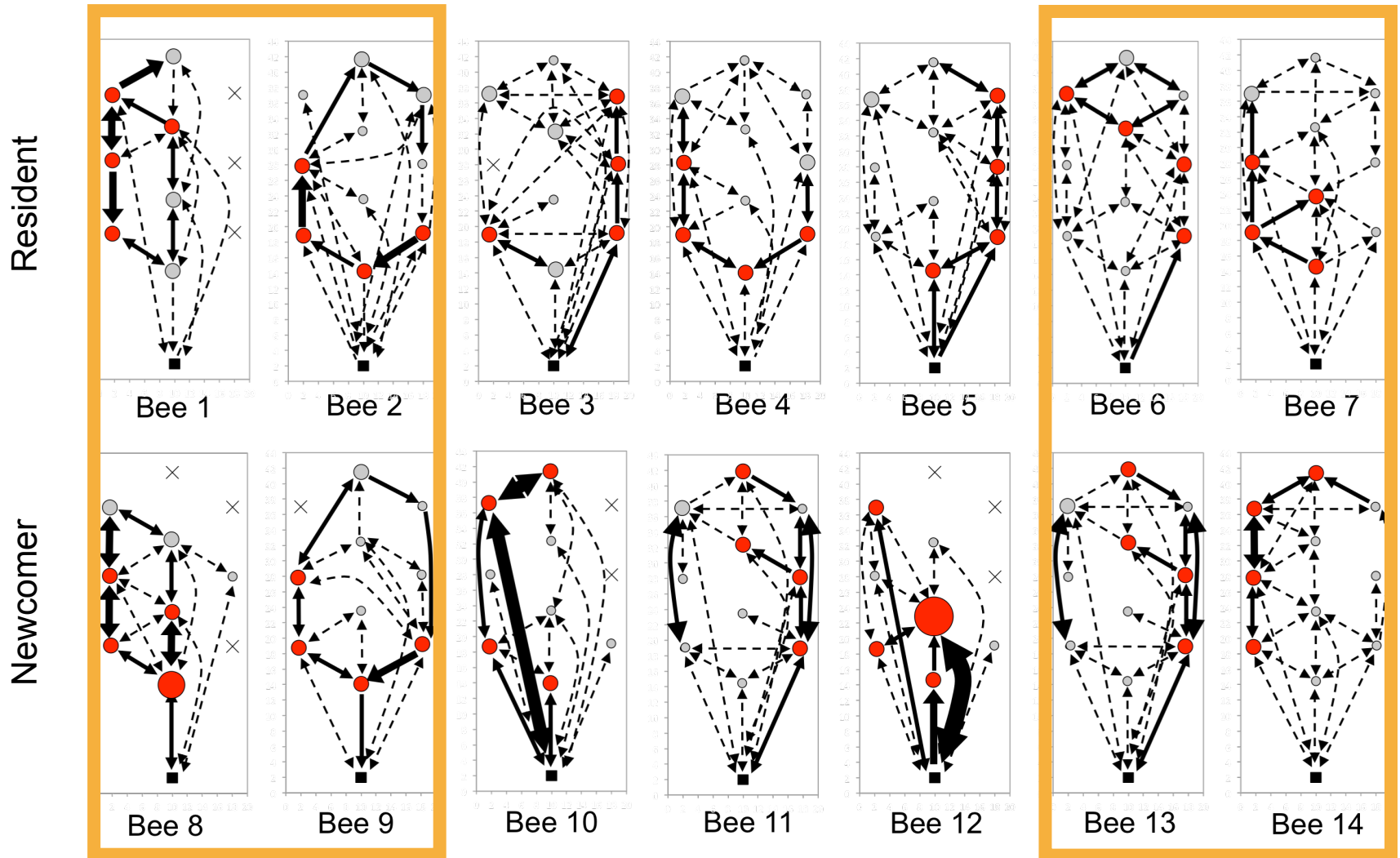


# Resource partitioning between foragers



Phase 1: 1 bee for 25 bouts  
Phase 2: 2 bees for 25 bouts  
N = 7 pairs

# Resource partitioning between foragers



# Resource partitioning between foragers

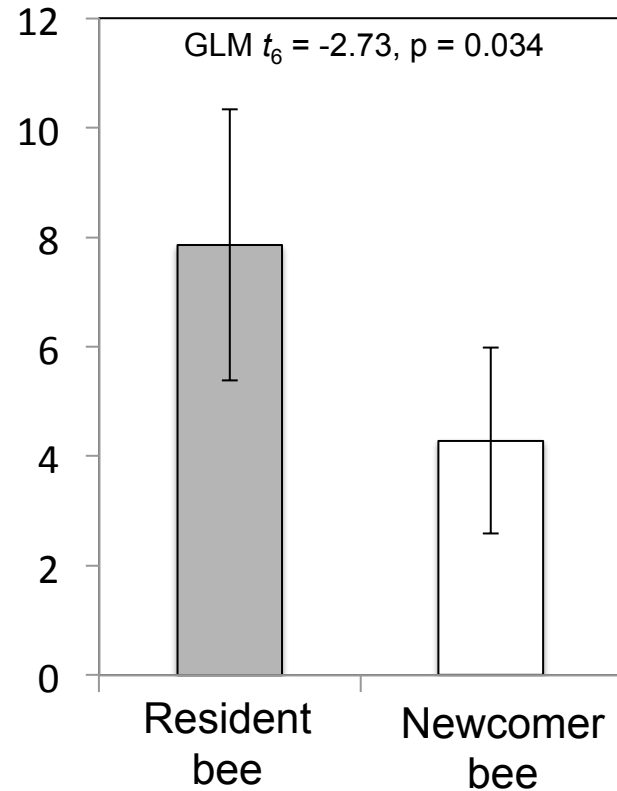
20 % of encounters: no aggression



80 % of encounters: eviction



Number of evictions



Experienced bees defend flowers by evicting newly arrived foragers.



# Outline



## 1. Forming routes

- one forager
- multiple foragers

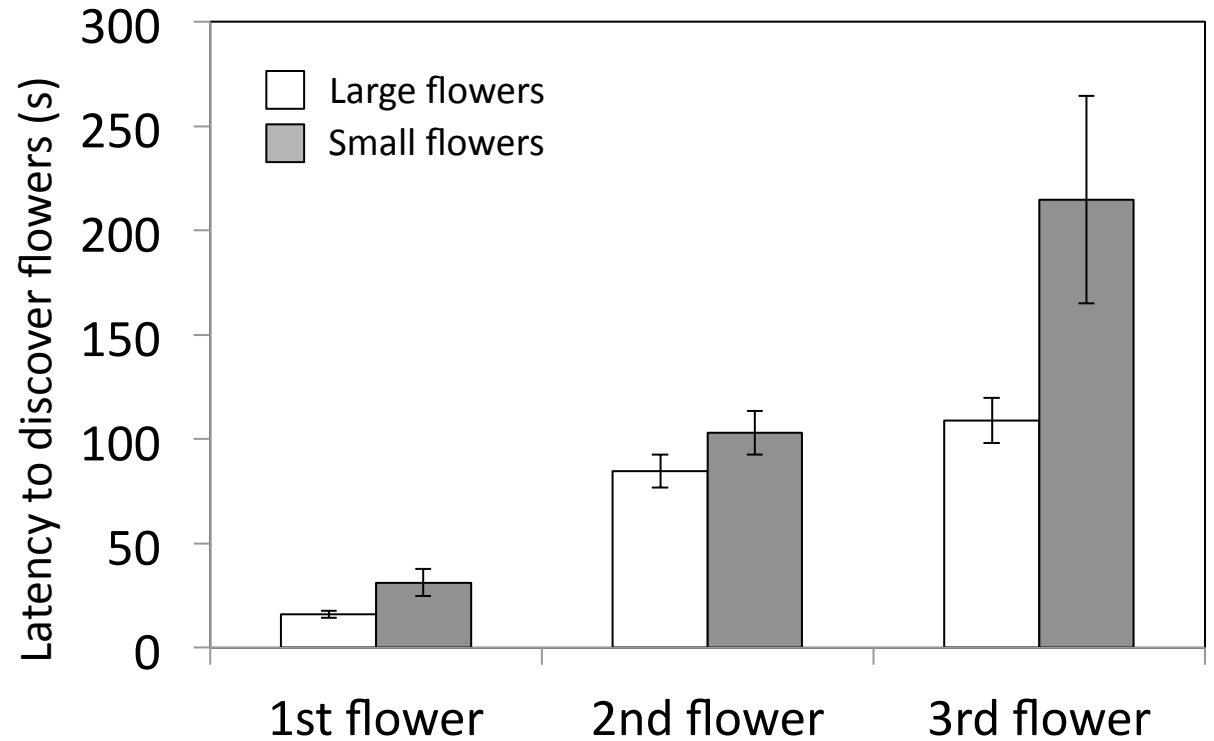
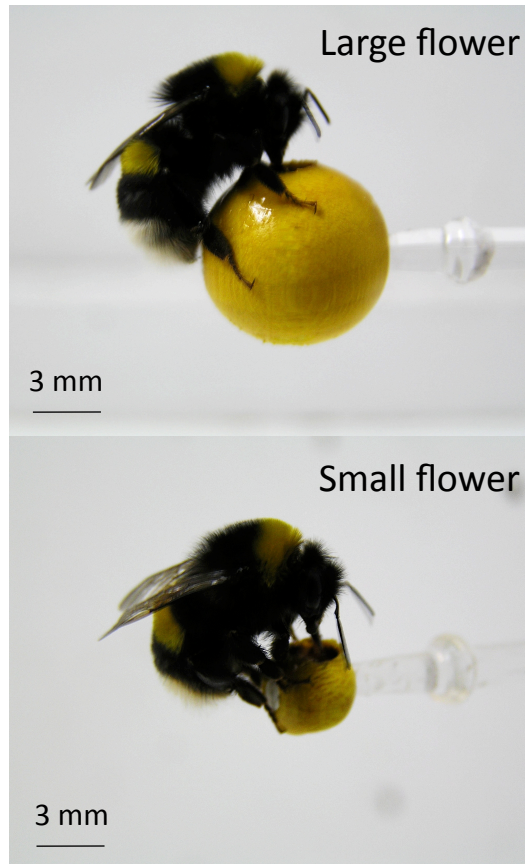
## 2. Locating new flowers

# How do bees search for flowers?

3D tracking of search flights



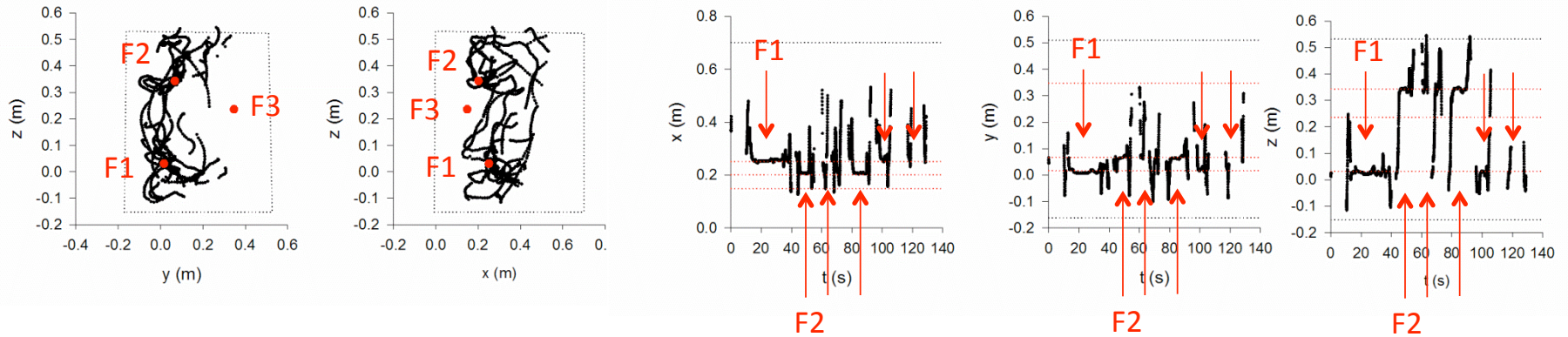
# Search performance



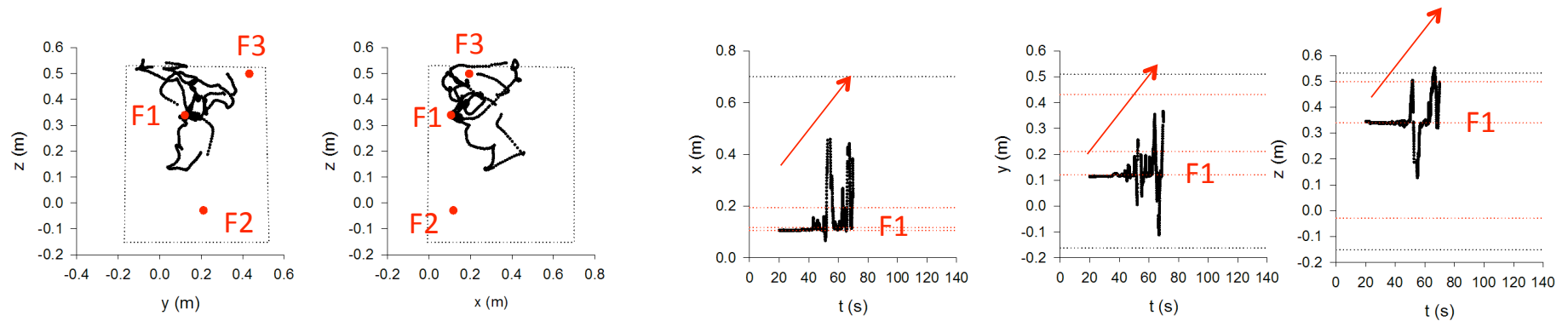
Bees find large flowers faster than smaller ones.

# Search loops of ever increasing sizes

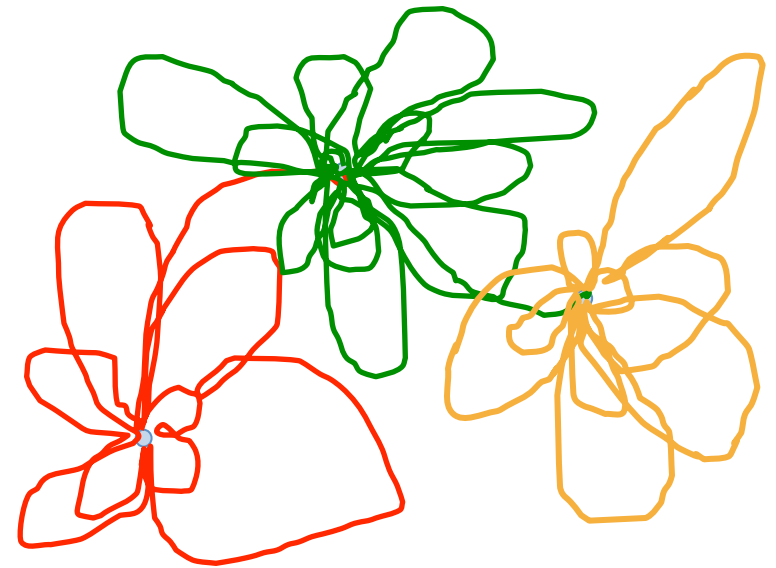
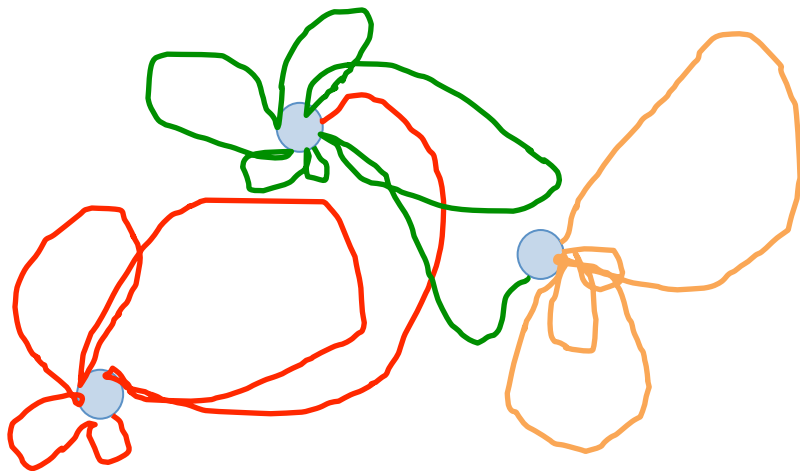
Indiv. B66 with large flowers



Indiv. B66 with small flowers



# Search loops of ever increasing sizes



Signatures of 'simulated annealing' patterns in search flights irrespective of flower size and arrangement.

# Outline



1. Forming routes
  - one forager
  - multiple foragers
2. Locating new flowers
3. Conclusions/projects

# Towards an integrated analysis of pollinator movements

Route learning



Social interactions



Intra sp. competition



Inter sp. competition



Impact on pollination

